



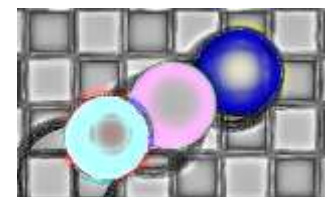
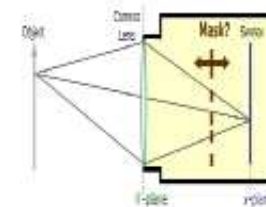
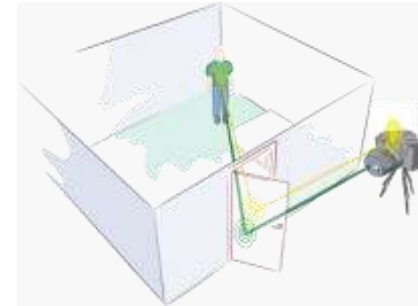
# Computational Light Transport Computational Photography Inverse problems

Ramesh Raskar  
**MIT Media Lab**

<http://raskar.info>  
[raskar@mit.edu](mailto:raskar@mit.edu)

# Inverse Problems

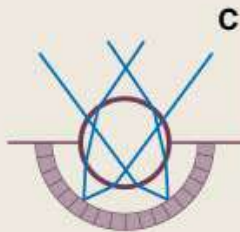
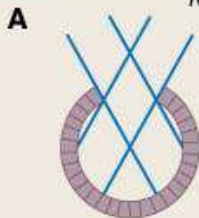
- Co-design of Optics and Computation
  - Photons not just pixels
  - Mid-level cues
- Computational Photography
  - Coded Exposure
  - Compressive Sensing for High Speed Events
    - Limits of CS for general imaging
- Computational Light Transport
  - Looking Around Corners, trillion fps
  - Lightfields:
    - Compressive Campture
    - 3D Displays and Holograms



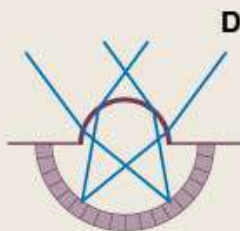
## Chambered eyes



*Nautilus*



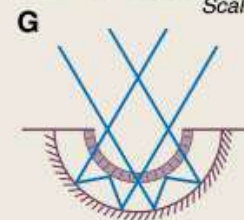
*Octopus*



*Red-tailed hawk*



*Scallop*



# Tools for Visual Computing

## Shadow

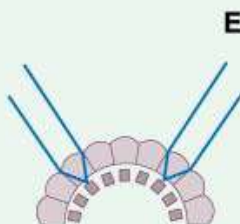
## Refractive

## Reflective

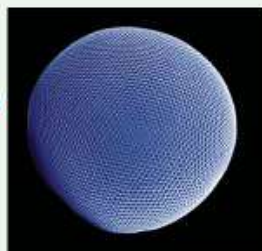
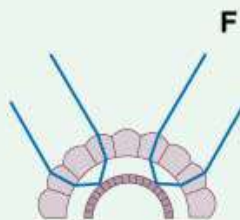
## Compound eyes



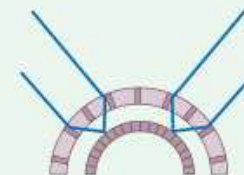
*Sea fan*



*Dragonfly*

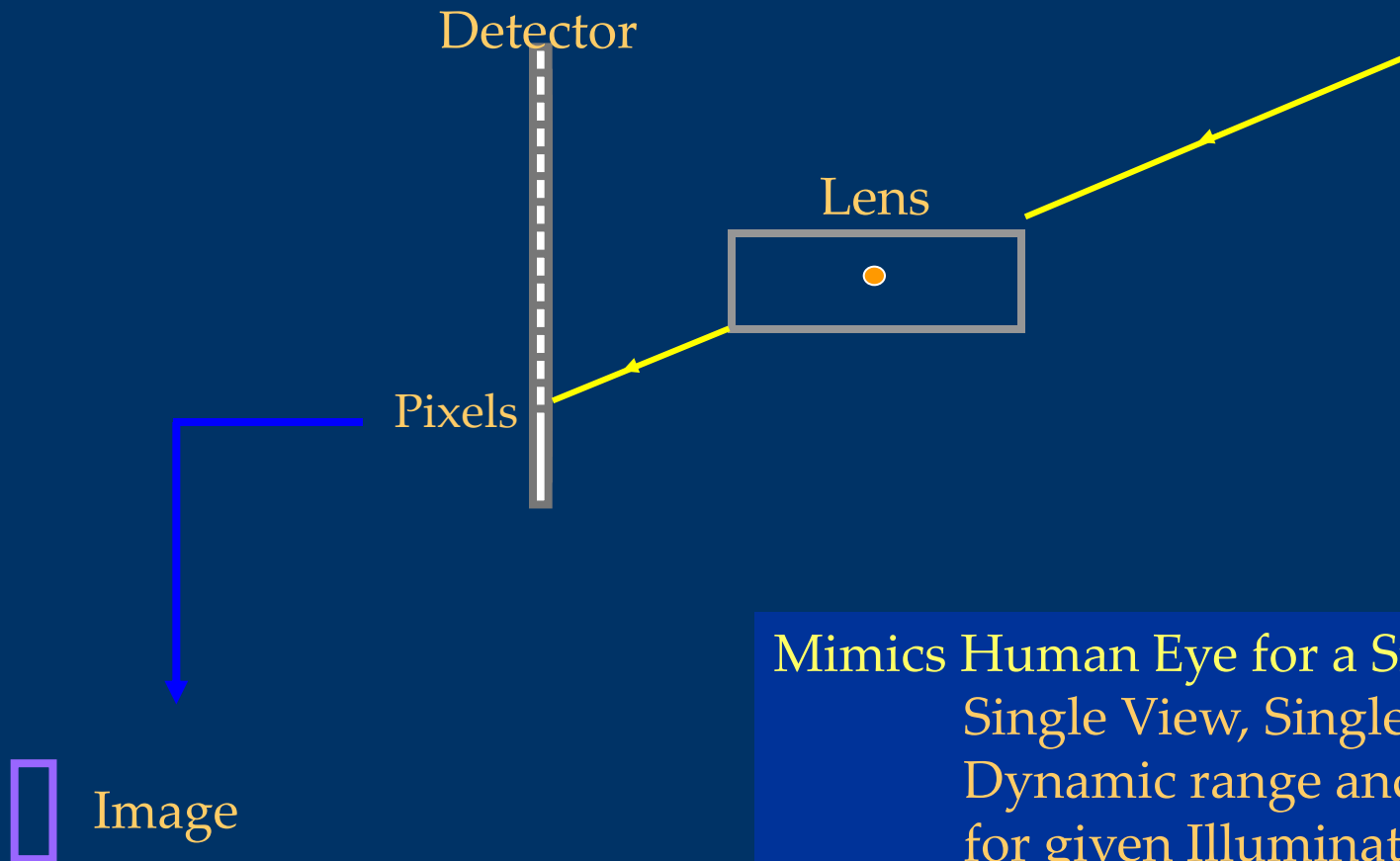


*Krill eye*



*Lobster*

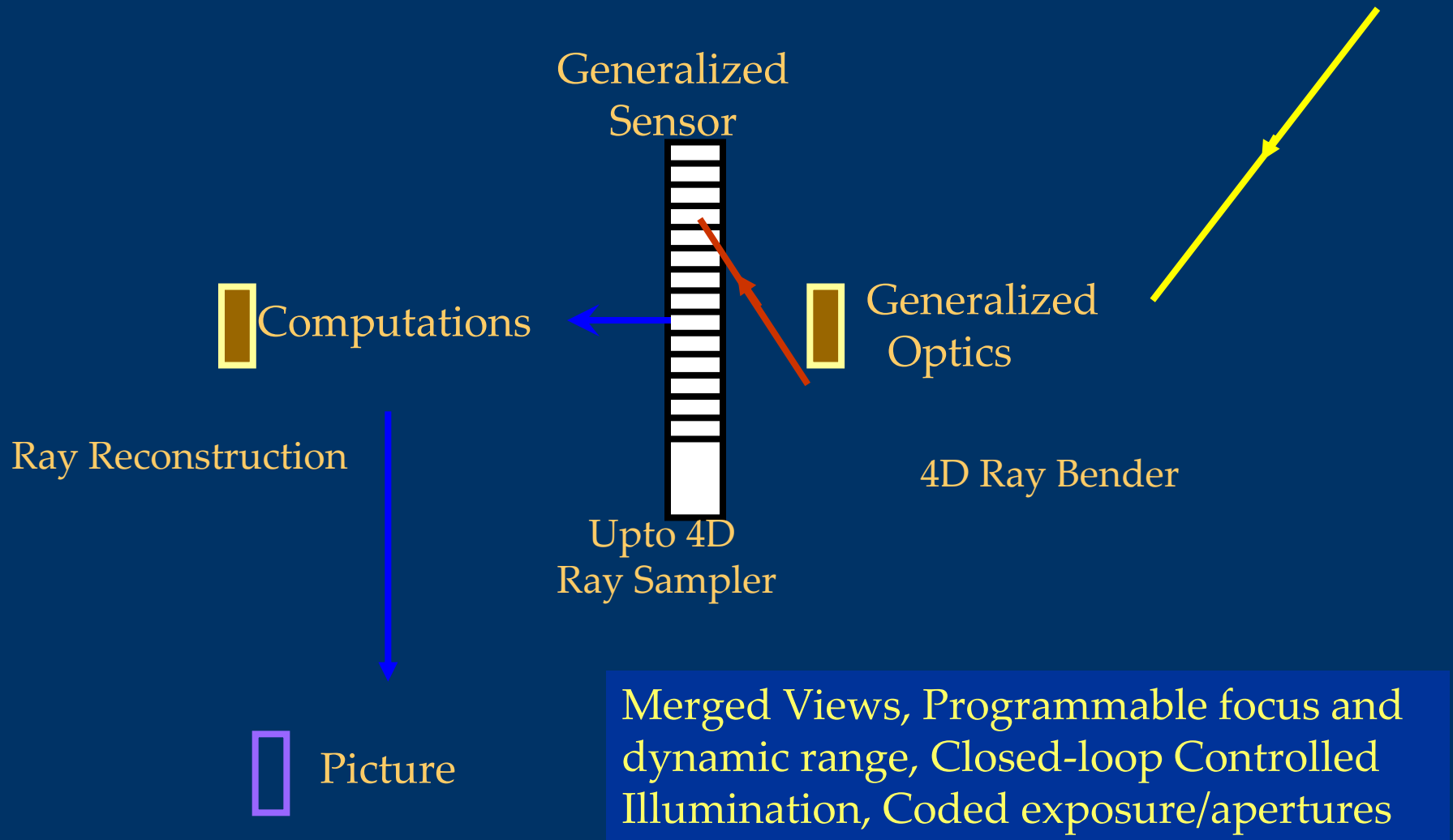
# Traditional Photography



Mimics Human Eye for a Single Snapshot:  
Single View, Single Instant, Fixed  
Dynamic range and Depth of field  
for given Illumination in a Static  
world

Courtesy: Shree Nayar

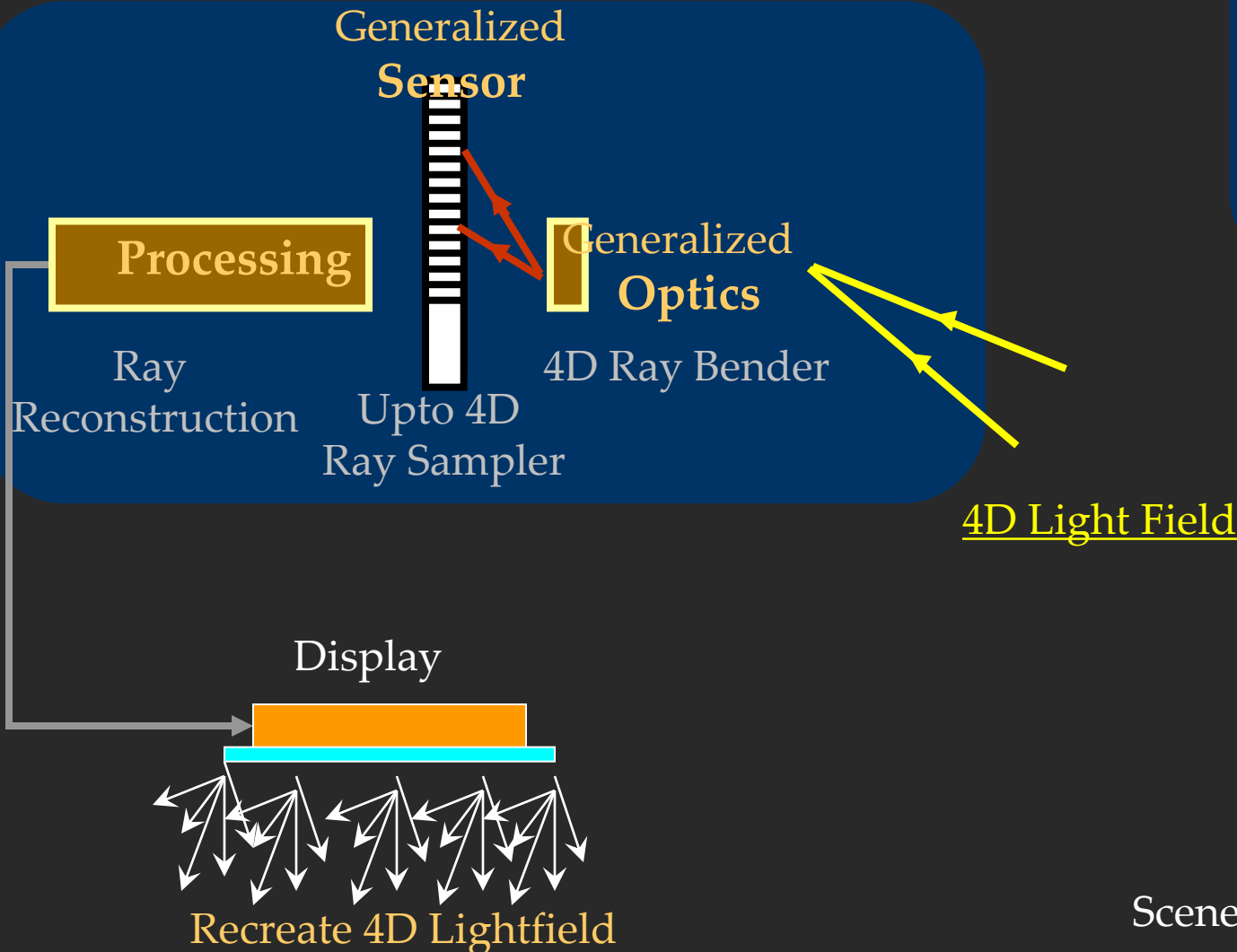
# Computational Camera + Photography: Optics, Sensors and Computations



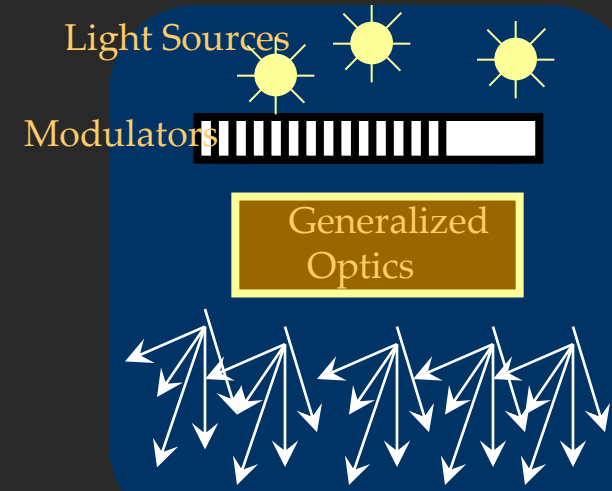


# Computational Photography

## Computational Cameras



## Novel Illumination



## 4D Incident Lighting



Scene: 8D Ray Modulator

# Camera Culture

Creating new ways to capture and share visual information

MIT Media Lab

Ramesh Raskar

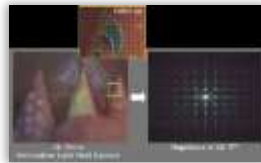
<http://cameraculture.info>

[Facebook.com/cameraculture](https://www.facebook.com/cameraculture)

## Computational Photography

### 1. Light-Field Camera

A new camera design exploiting the fundamental dictionary of light-fields for a single-capture capture of light-fields with full-resolution refocusing effects.



### 2. Color Primaries

A new camera design with switchable color filter arrays for optimal color fidelity and picture quality on scene geometry, color and illumination.



### 3. Flutter-Shutter

A camera that codes the exposure time with a binary pseudo-sequence to de-convolve and remove motion blur in textured backgrounds and partial occluders.



### 4. Compressive Capture

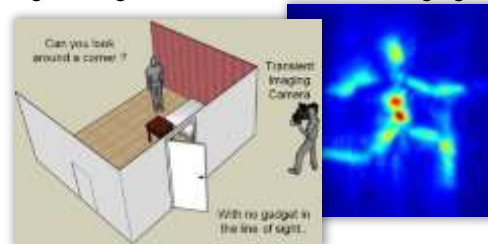
We analyze the gamut of visual signals from low-dimensional images to light-fields and propose non-adaptive projections for efficient sparsity exploiting reconstruction.



## Femtosecond Imaging

### 1. Looking around corners

Using short laser pulses and fast detector, we aim to build a device that can look around corners with no imaging device in the line of sight using time resolved transient imaging.

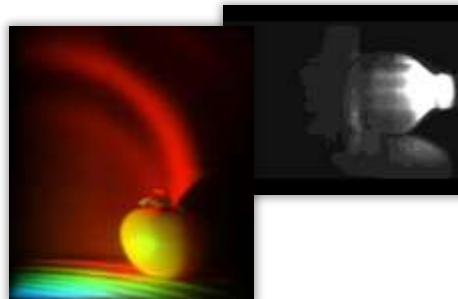


### 2. Reflectance Recovery

We demonstrate a new technique that allows a camera to rapidly acquire reflectance properties of objects 'in the wild' from a single viewpoint, over relatively long distances and without encircling equipment.

### 3. Trillion Frames per Second Imaging

A camera fast enough to capture light pulses moving through objects. We can use such a camera to understand reflectance, absorption and scattering properties of materials.



## 3D Displays

### 1. Tensor Display

A family of compressive light field displays comprising all architectures employing a stack of time-multiplexed, light-attenuating layers illuminated by uniform or directional backlighting



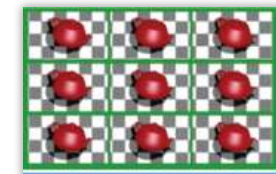
### 2. Layered 3D

Tomographic techniques for image synthesis on displays composed of compact volumes of light-attenuating material. Such volumetric attenuators recreate a 4D light field or high-contrast 2D image when illuminated by a uniform backlight.



### 3. Glasses-free 3D HDTV

Light field displays with increased brightness and refresh rate by stacking a pair of modified LCD panels, exploiting rank and constraint of 3D displays



### 4. BIDI Screen

A thin, depth-sensing LCD for 3D interaction using light fields which supports both 2D multi-touch and unencumbered 3D gestures.



### 5. Living Windows 6D Display

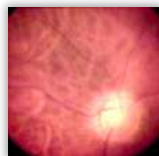
A completely passive display



## Health & Wellness

### 1. Retinal Imaging

With simplified optics and clever illumination we visualize images of the retina in a standalone device easily operated by the end user.



### 2. NETRA/CATRA

Low-cost cell-phone attachments that measures eye-glass prescription and cataract information from the eye.



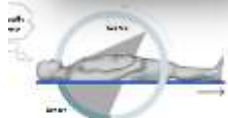
### 3. Cellphone Microscopy

A platform for computational microscopy and remote healthcare



### 4. High-speed Tomography

A compact, fast CAT scan machine using no mechanical moving parts or synchronization.



### 5. Shield Fields

3D reconstruction of objects from a single shot photo using spatial heterodyning.



### 6. Second Skin

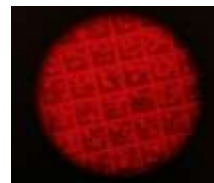
Using 3D motion tracking with real-time vibrotactile feedback aids the correct of movement and position errors to improve motor learning.



## Human Computer Interaction

### 1. Bokode

Low-cost, passive optical design so that bar codes can be shrunk to fewer than 3mm and read by ordinary cameras several meters away.



### 2. Specklesense

Set of motion-sensing configurations based on laser speckle sensing. The underlying principles allow interactions to be fast, precise, extremely compact, and low cost.



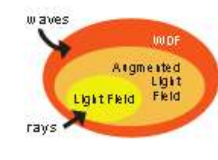
### 3. Sound Around

Soundaround is a multi-viewer interactive audio system, designed to be integrated into multi-view displays presenting localized audio/video channels with no need for glasses or headphones.

## Light Propagation Theory and Fourier Optics

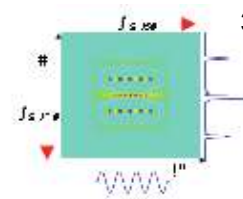
### 1. Augmented Light Fields

Expands light field representations to describe phase and diffraction effects by using the Wigner Distribution Function



### 2. Hologram v Parallax Barrier

Defines connections between parallax barrier displays and holographic displays by analyzing their operations and limitations in phase space



### 3. Ray-Based Diffraction Model

Simplified capture of diffraction model for computer graphics applications.



## Visual Social Computing

### 1. Photocloud

A near real-time system for interactively exploring a collectively captured moment without explicit 3D reconstruction.



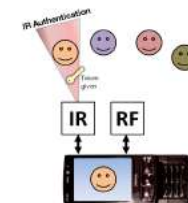
### 2. Vision Blocks

On-demand, in-browser, customizable, computer-vision application-building platform for the masses. Without any prior programming experience, users can create and share computer vision applications.



### 3. Lenschat

LensChat allows users to share mutual photos with friends or borrow the perspective and abilities of many cameras.



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**Cameraculture.info**



**fb.com/cameraculture**

Post-Doctoral Researchers: Doug Lanman, Gordon Wetzstein, Alex Olwal, Christopher Barsi

Research Assistants: Matthew Hirsch, Otkrist Gupta, Nikhil Naik, Jason Boggess, Everett Lawson, Aydin Arpa, Kshitij Marwah

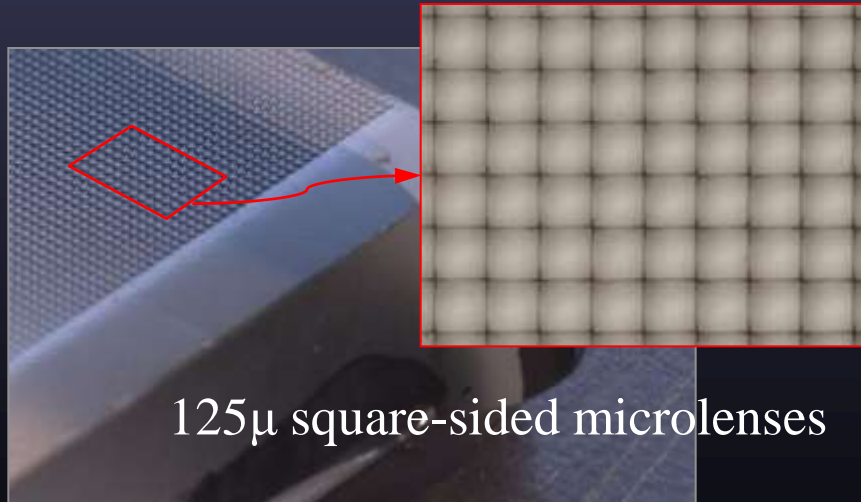
Visiting Researchers & Students: Di Wu, Daryl Lim





# Digital Refocusing using Light Field Camera

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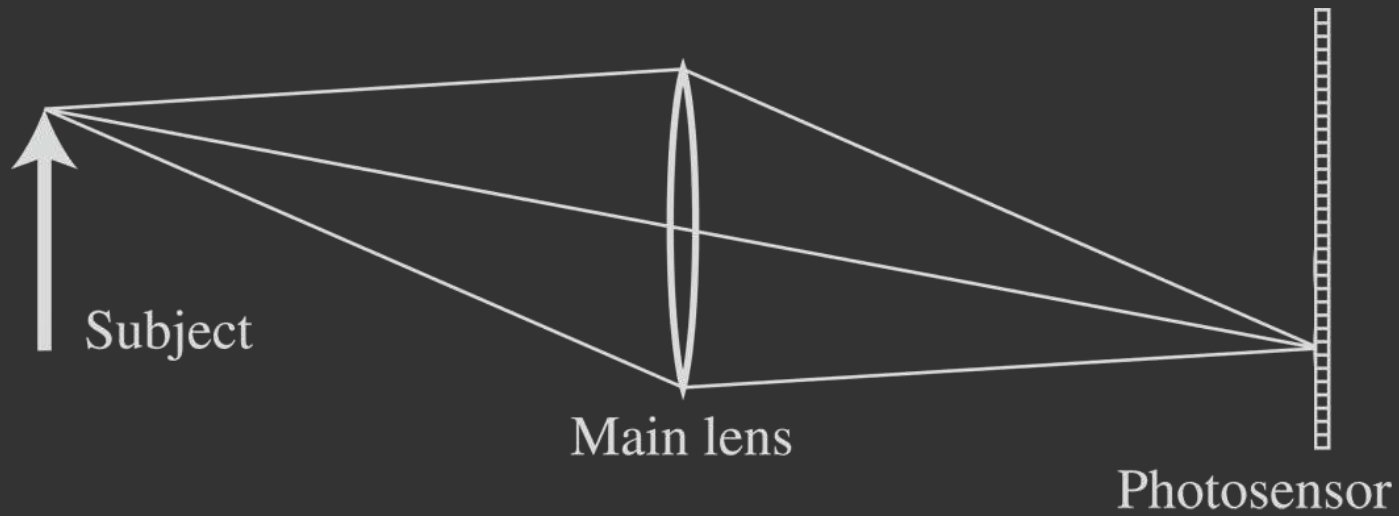


125μ square-sided microlenses

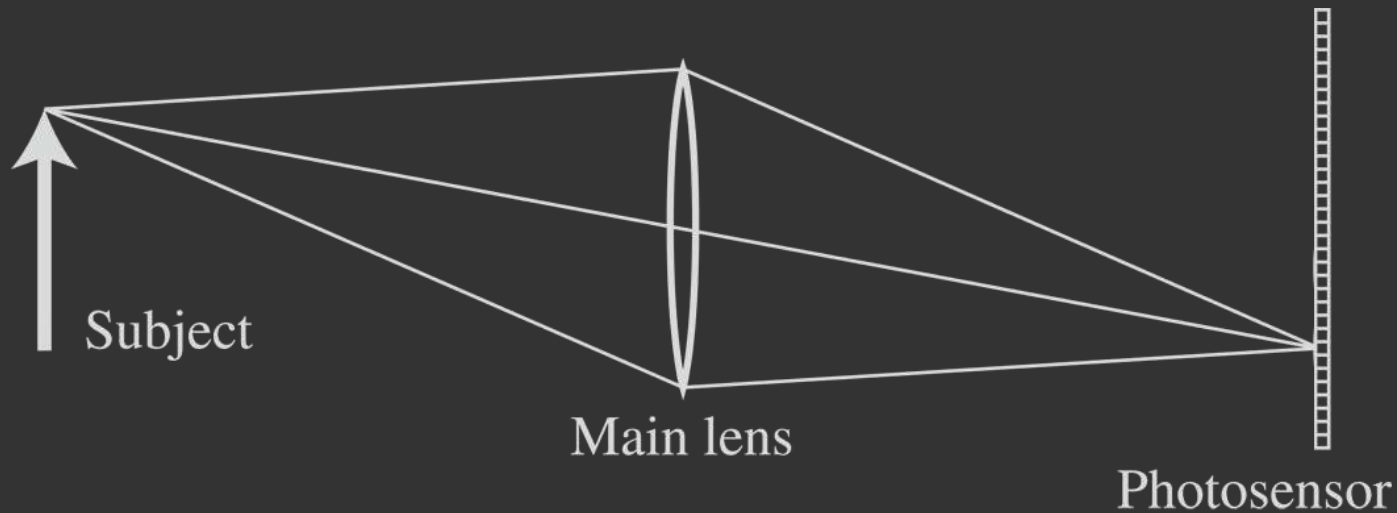


[Ng et al 2005]

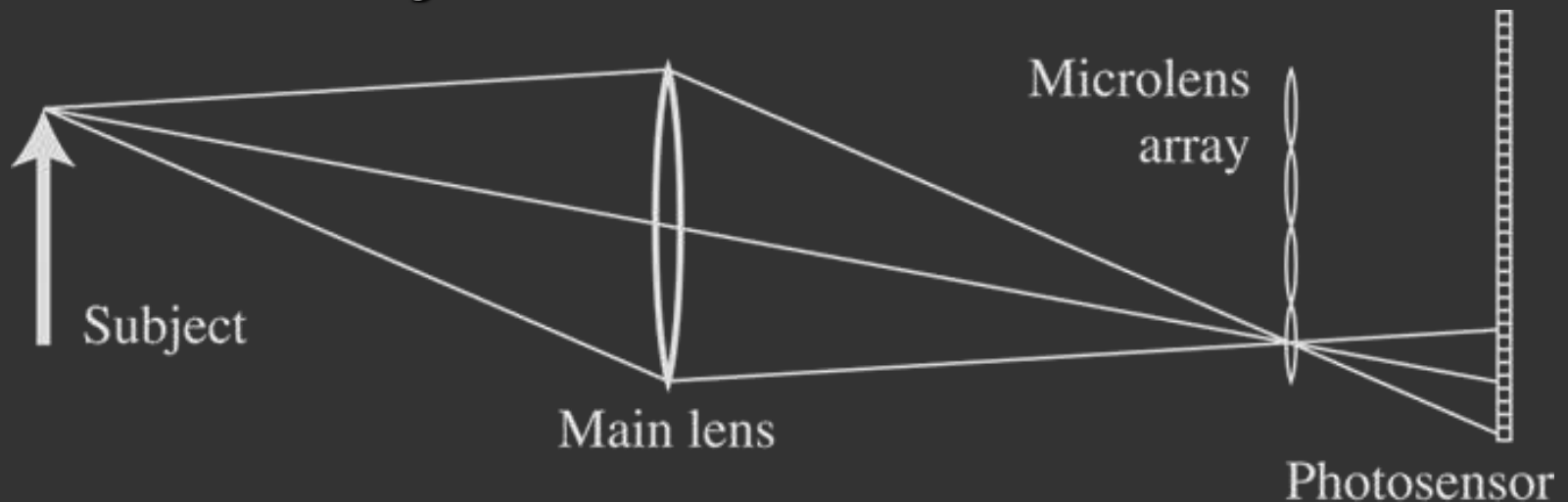
# Light Field Inside a Camera



# Light Field Inside a Camera

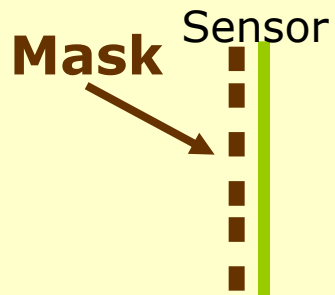


## Lenslet-based Light Field camera



[Adelson and Wang, 1992, Ng et al. 2005 ]

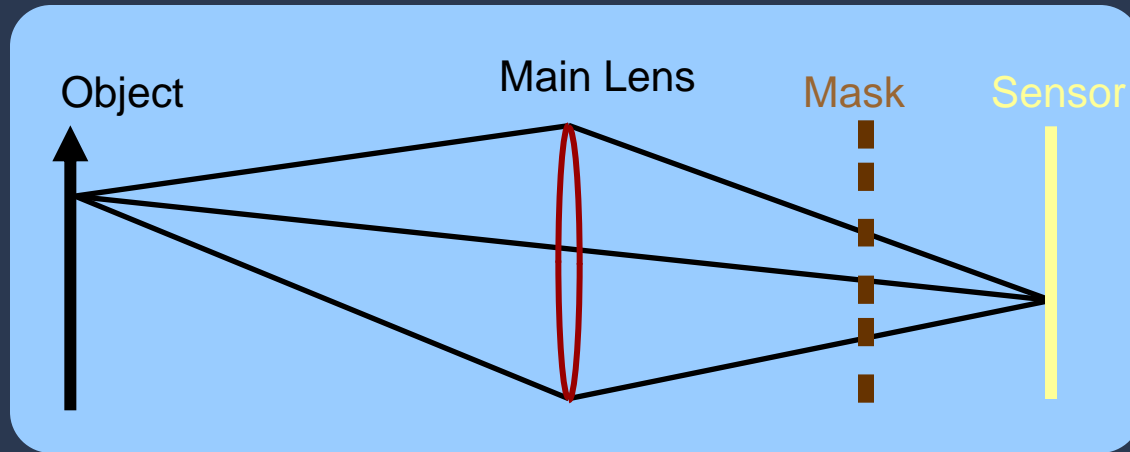
# Mask based Light Field Camera



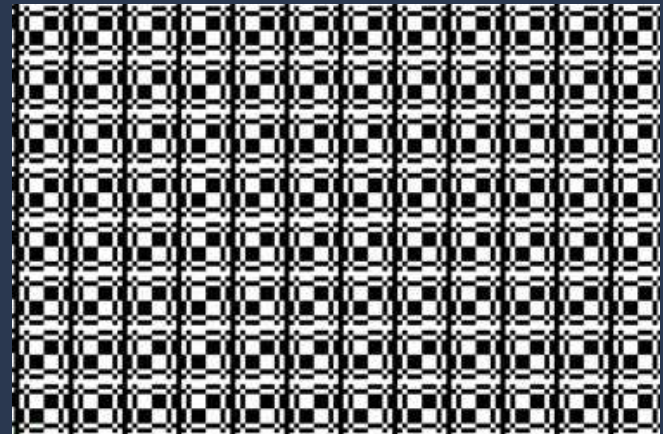
[Veeraraghavan, Raskar, Agrawal, Tumblin, Mohan, Siggraph 2007 ]



# Spatial Heterodyning with Masks



- Mask == Light Field Modulator
- Intensity of ray gets **multiplied** by Mask
- Convolution** in Frequency domain
- Lightfield without additional lenslets



**Wavefront Analysis for ANY wavelength**

Captured 2D Photo



Encoding due to  
Mask

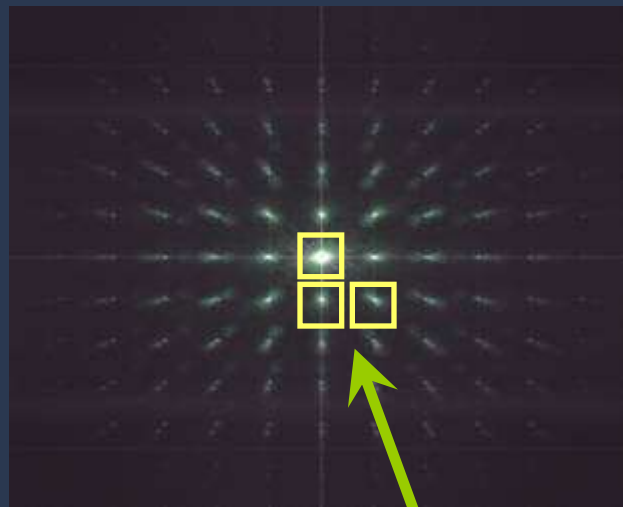
# Mask-based 4D Light Field

2D Sensor Photo, 1800\*1800



2D  
FFT

2D Fourier Transform, 1800\*1800



$9 \times 9 = 81$  spectral copies



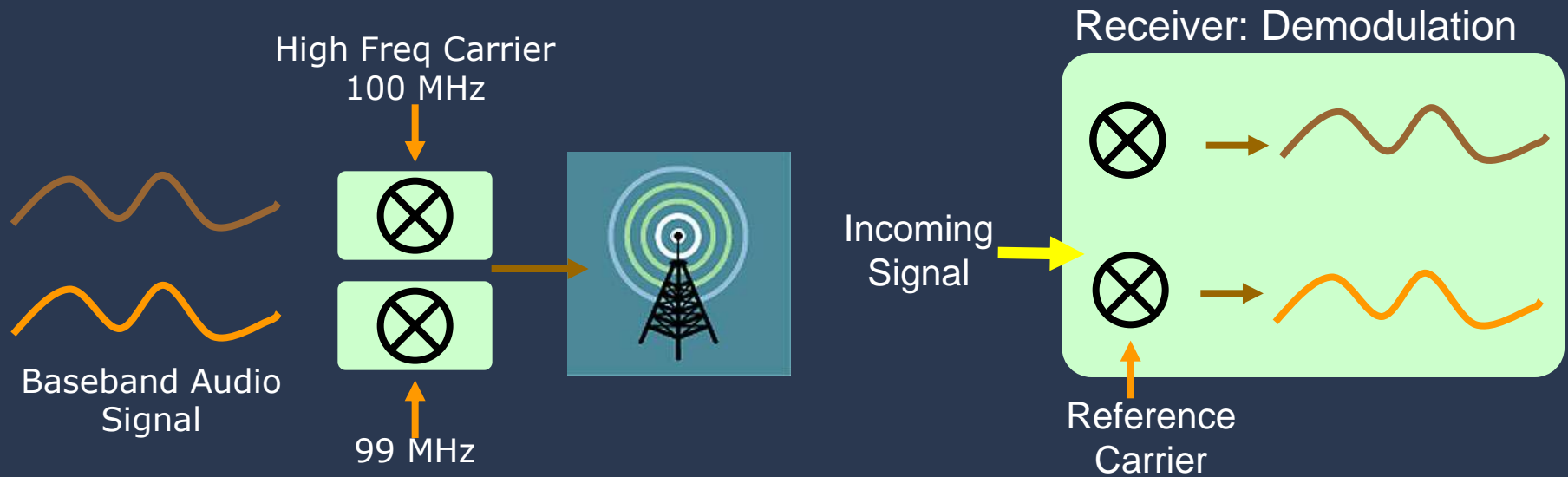
Rearrange 2D tiles into 4D planes  
 $200 \times 200 \times 9 \times 9$

4D IFFT



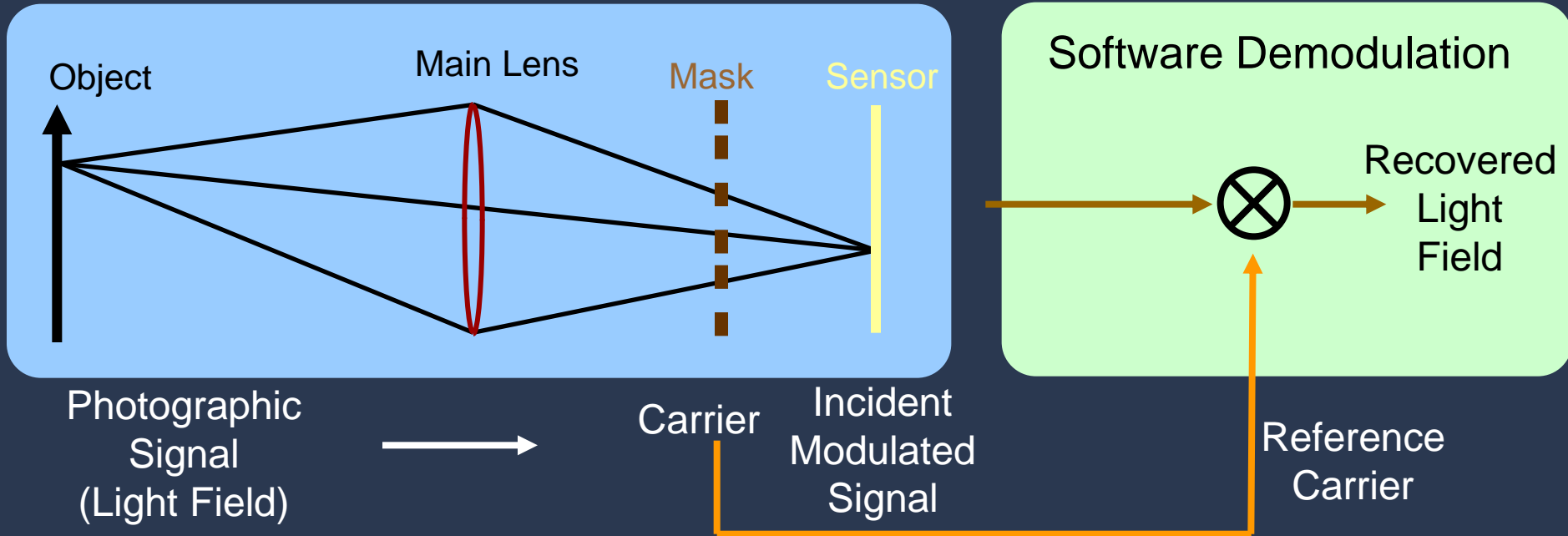
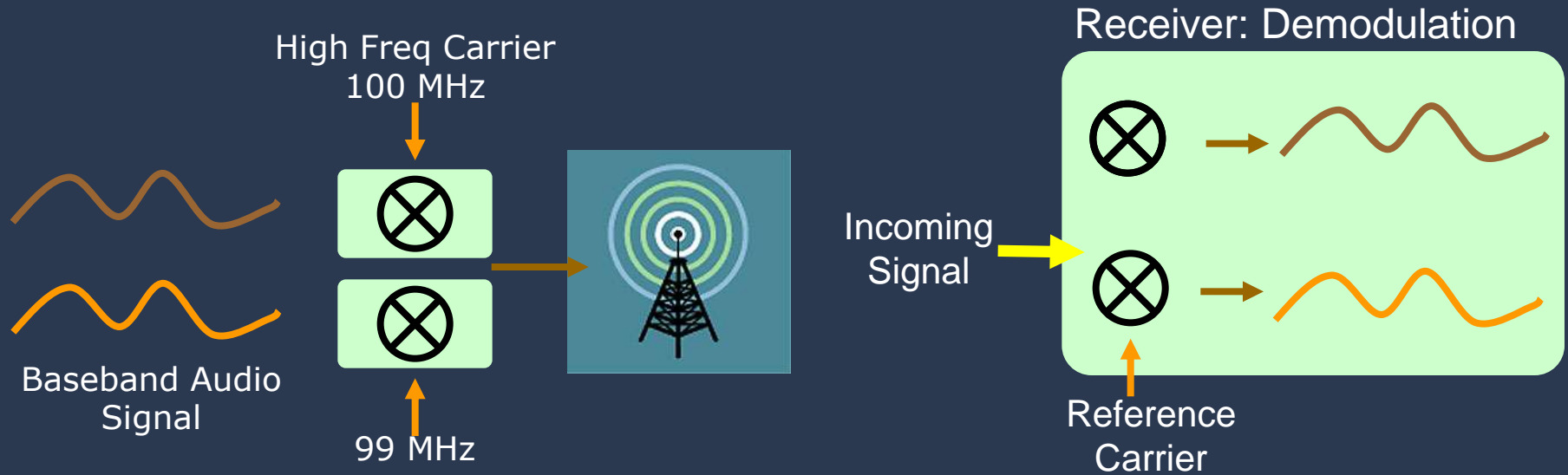
4D Light Field  $\rightarrow$  Depth  
 $200 \times 200 \times 9 \times 9$

# Radio Frequency Heterodyning



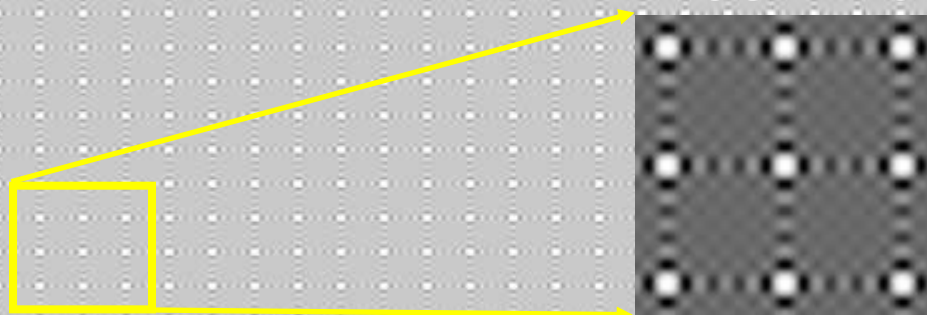


# Optical Heterodyning



Cosine Mask Used

Mask Tile



$1/f_0$

# Captured 2D Photo

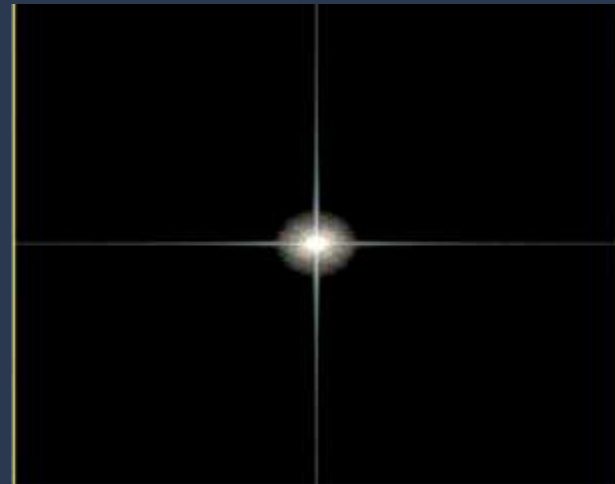


Encoding due to  
Mask



Traditional Camera Photo

2D  
FFT  
→

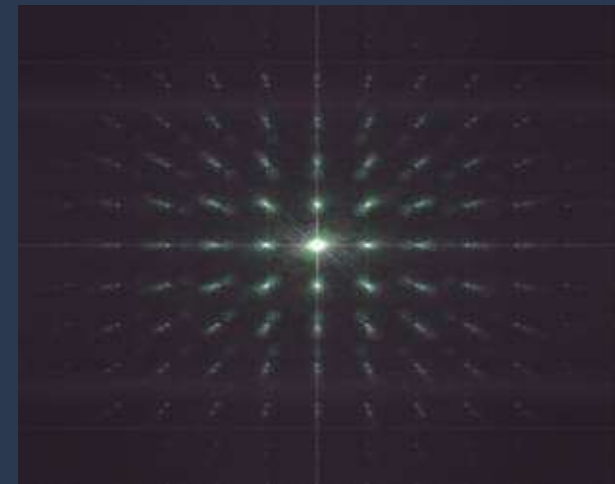


Magnitude of 2D FFT



Heterodyne Camera Photo

2D  
FFT  
→



Magnitude of 2D FFT



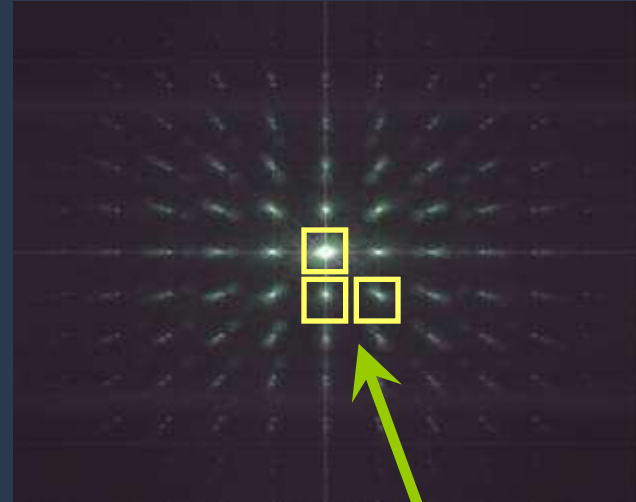
# Computing 4D Light Field

2D Sensor Photo,  $1800 \times 1800$



2D  
FFT

2D Fourier Transform,  $1800 \times 1800$



$9 \times 9 = 81$  spectral copies



Rearrange 2D tiles into 4D planes  
 $200 \times 200 \times 9 \times 9$

4D IFFT



4D Light Field  
 $200 \times 200 \times 9 \times 9$

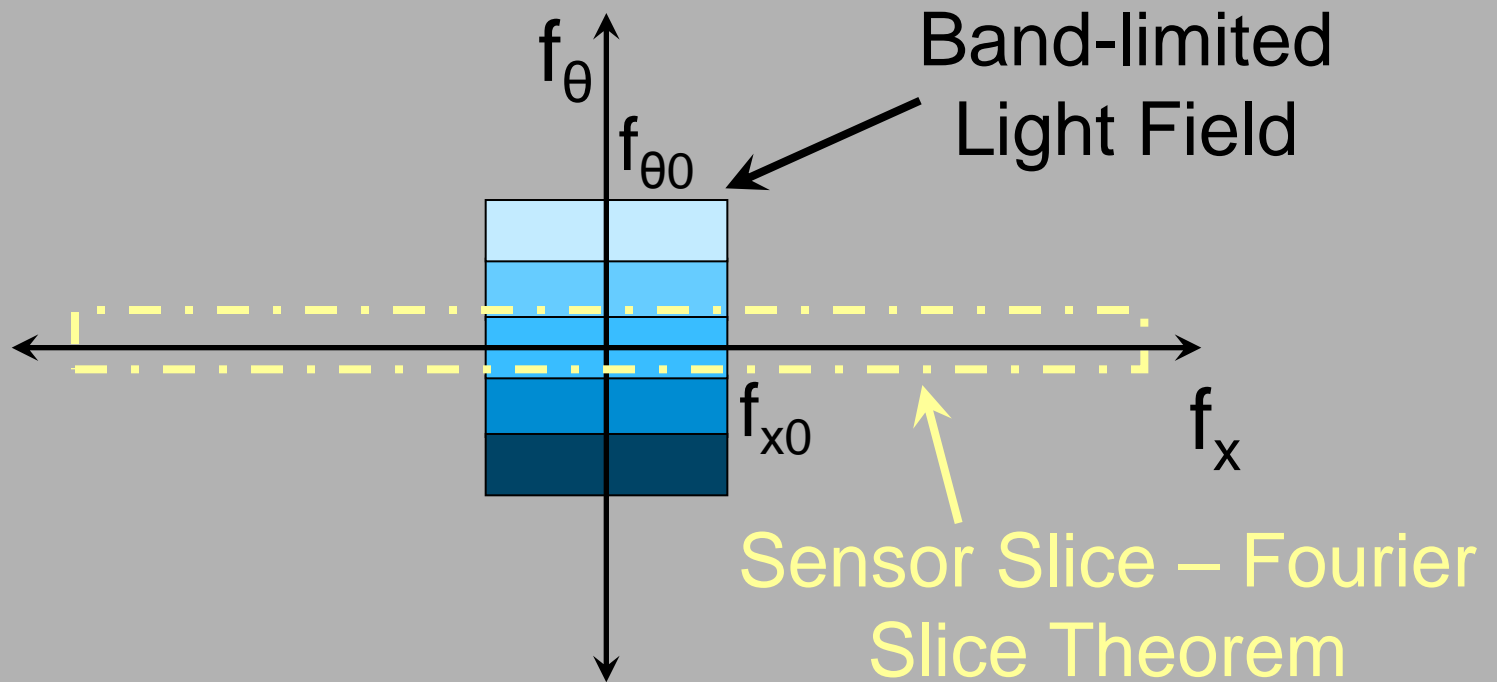
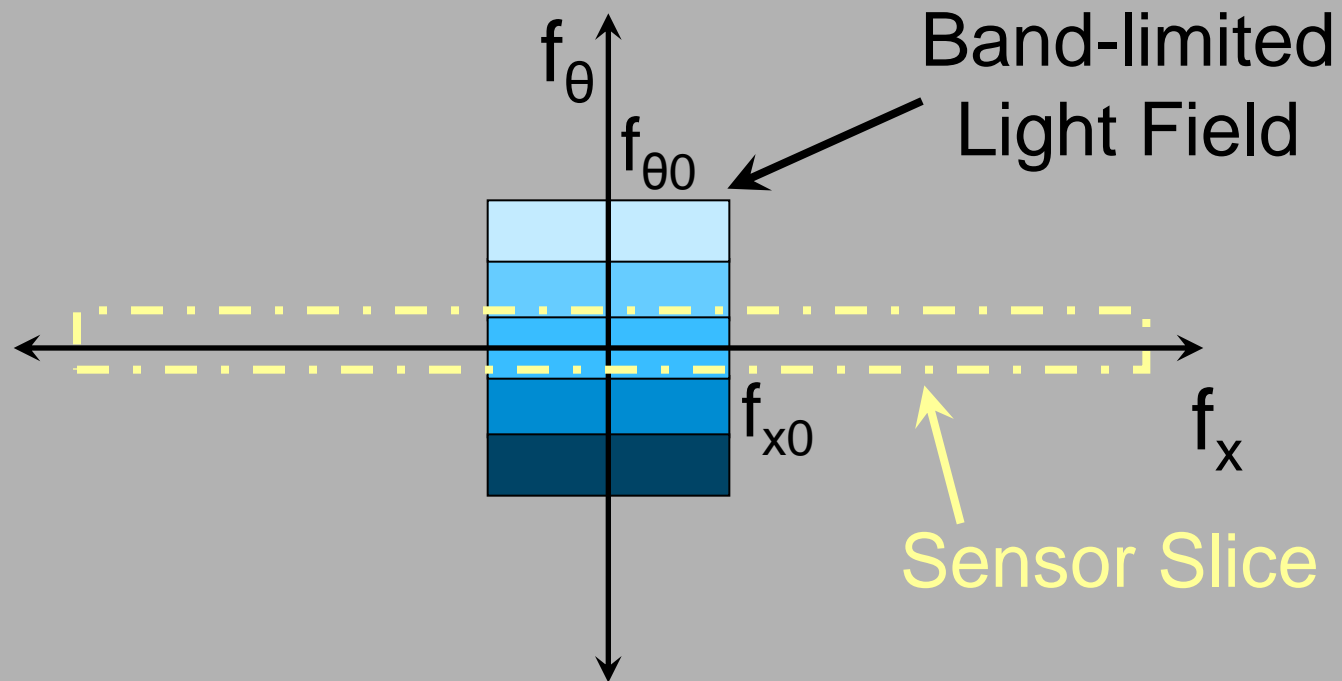


Photo = Slice of Light Field in Fourier Domain

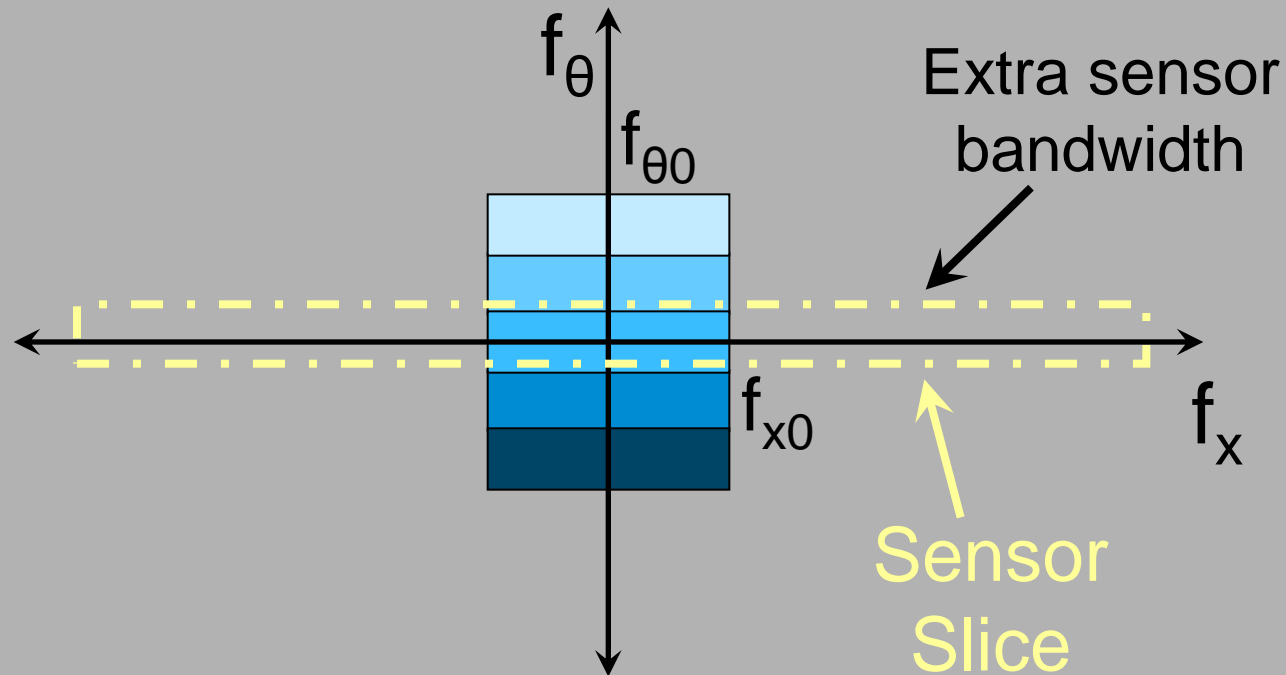
[Ren Ng, SIGGRAPH 2005]

# How to Capture 2D Light Field with 1D Sensor ?

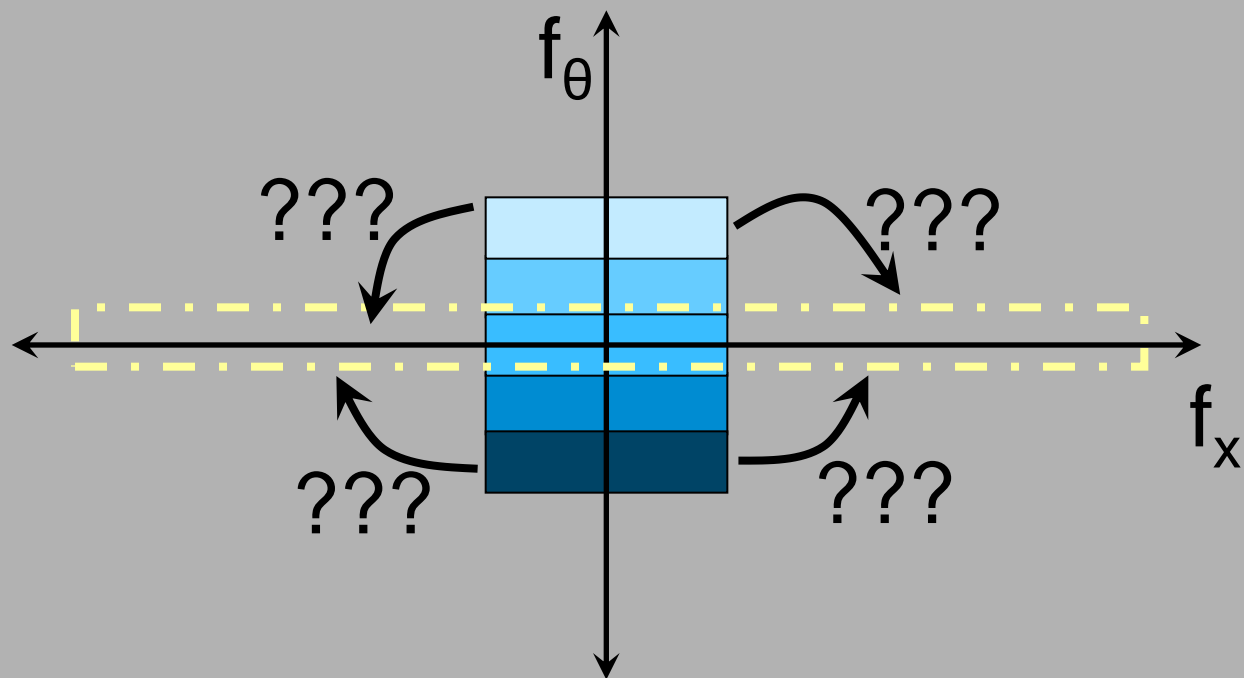


## Fourier Light Field Space

Extra sensor bandwidth cannot capture extra *dimension* of the light field

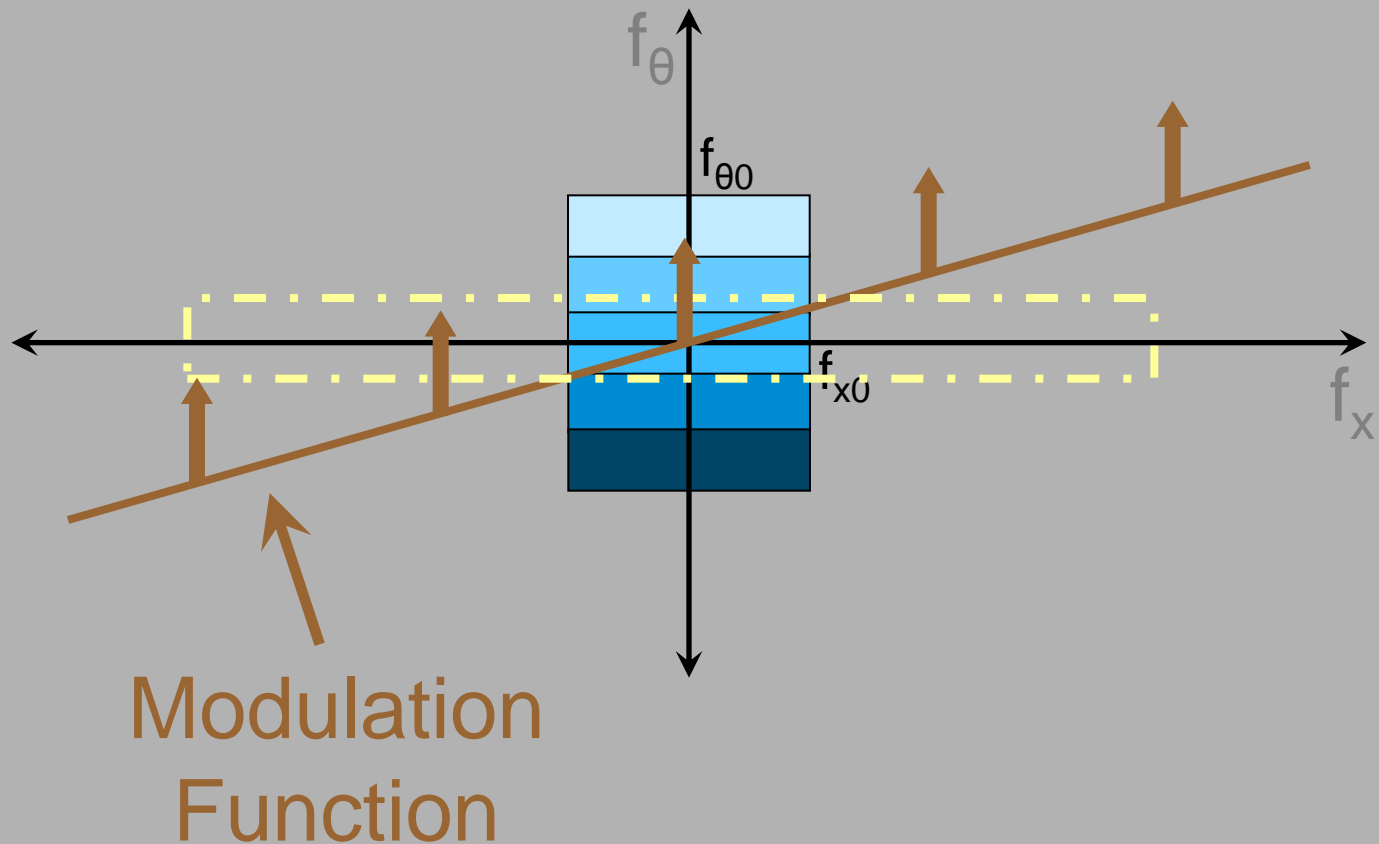




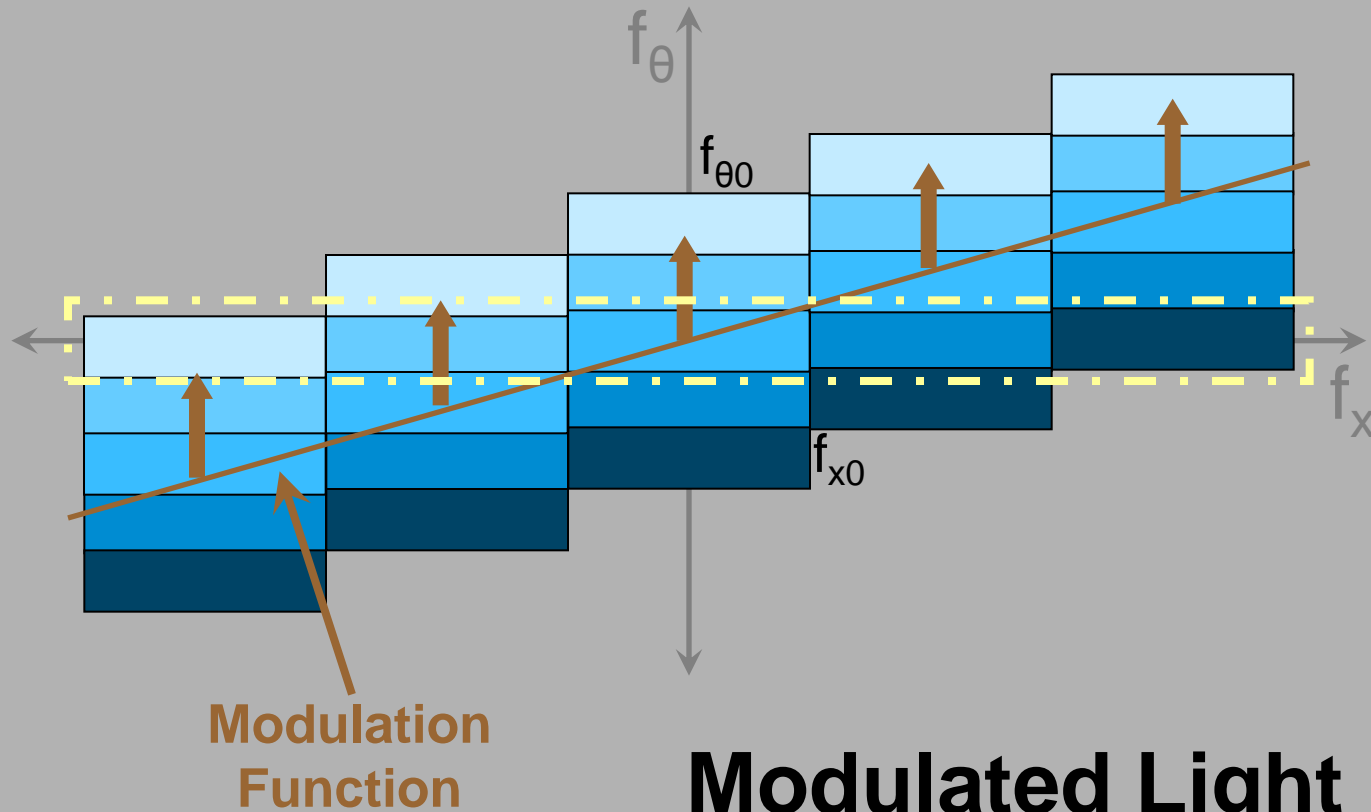


# Solution: Modulation Theorem

Make spectral copies of 2D light field

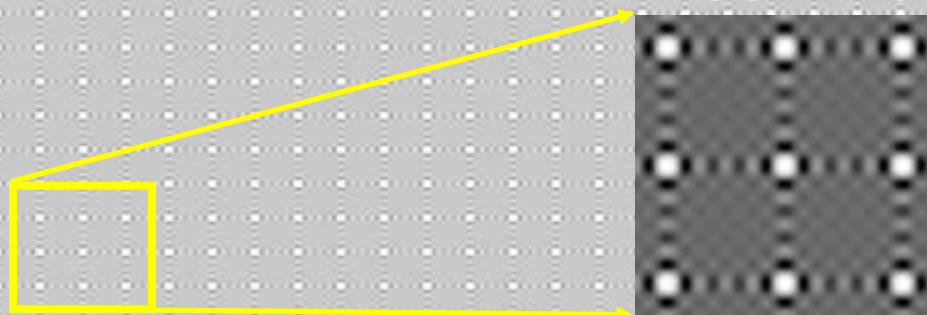


# Sensor Slice captures entire Light Field



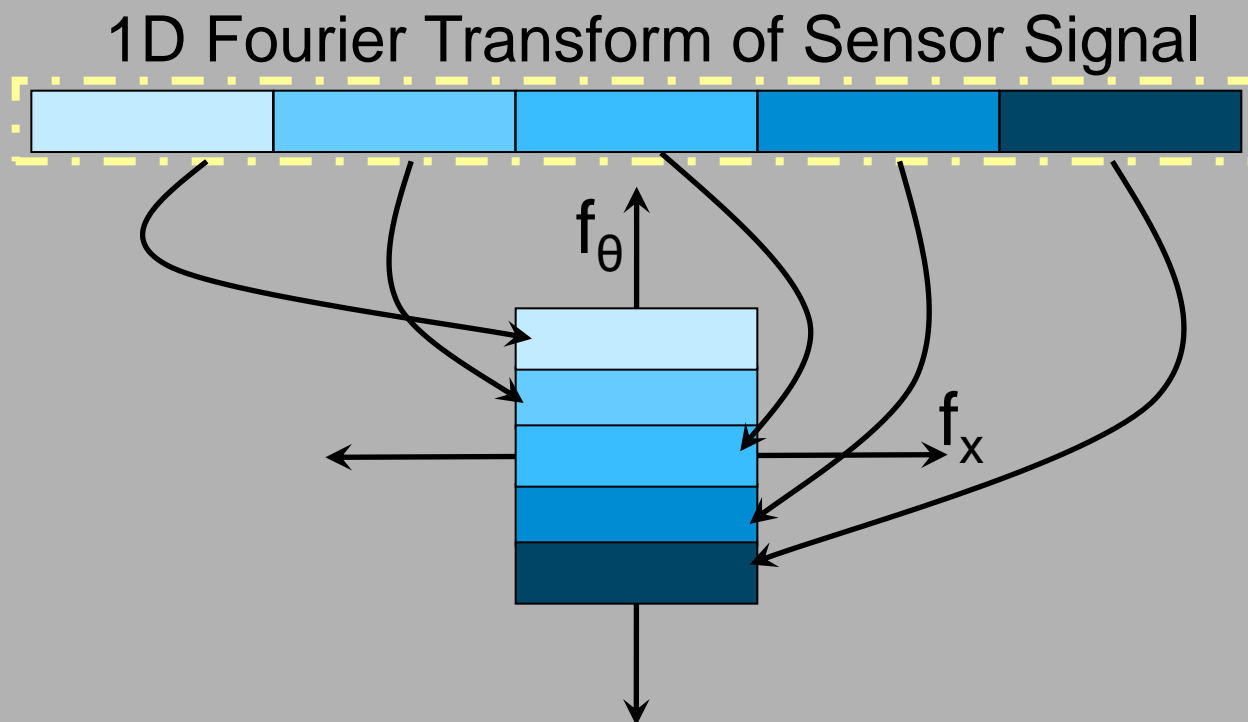
Cosine Mask Used

Mask Tile



$1/f_0$

# Demodulation to recover Light Field

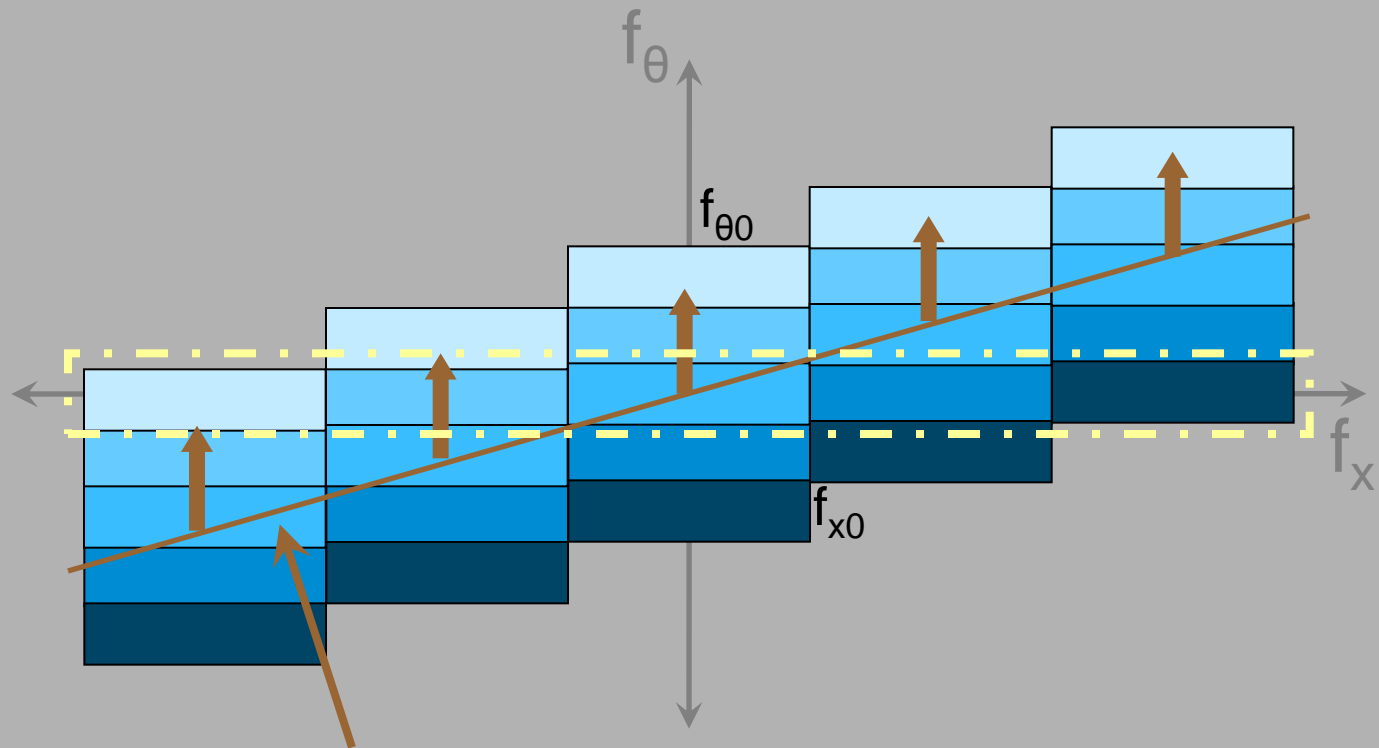


*Reshape* 1D Fourier Transform into 2D

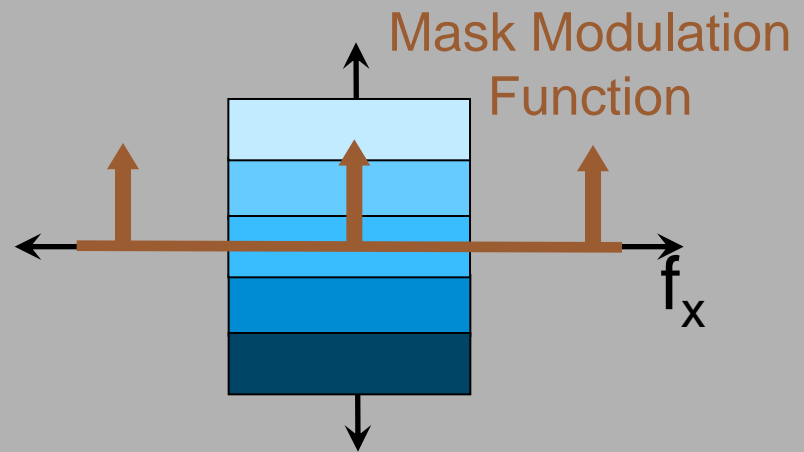
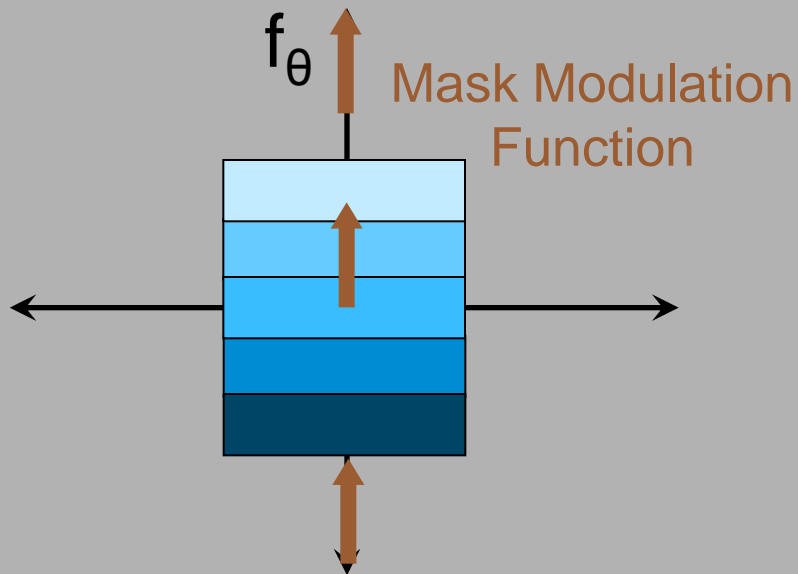
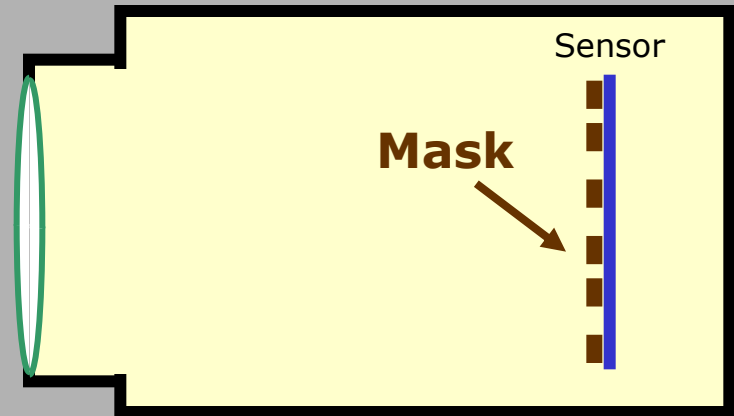
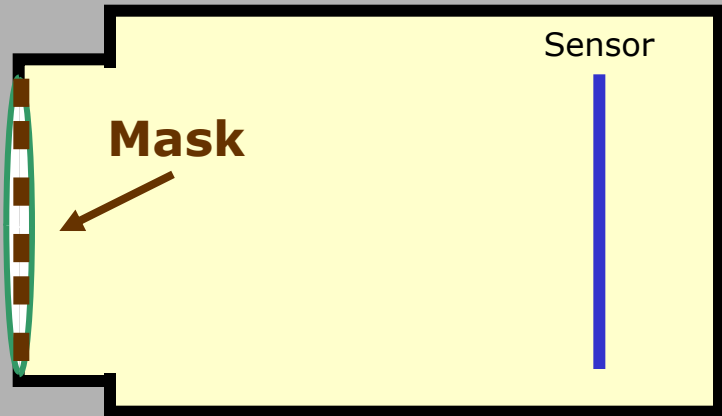


Modulation Function == Sum of Impulses

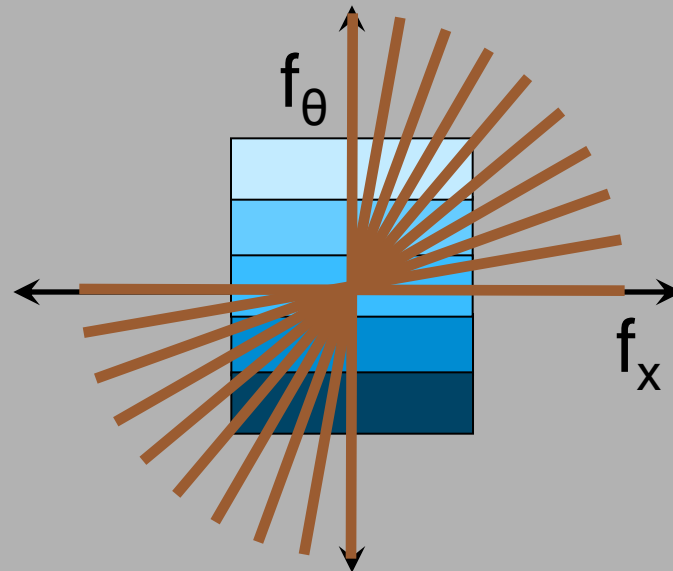
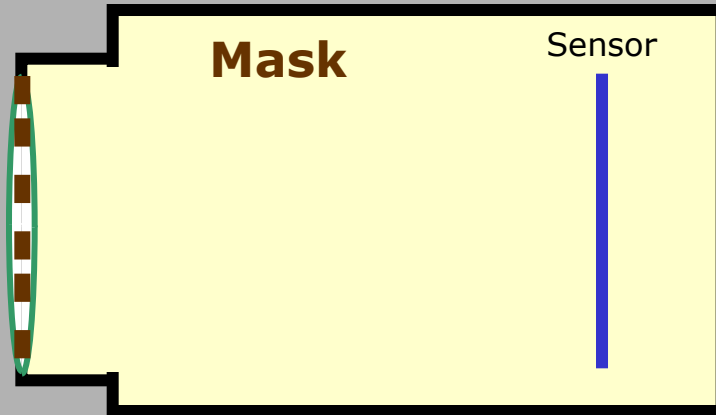
Physical Mask = Sum of Cosines



# Where to place the Mask?



# Where to place the Mask?



Mask  
Modulation  
Function

# Captured 2D Photo



Encoding due to  
Cosine Mask

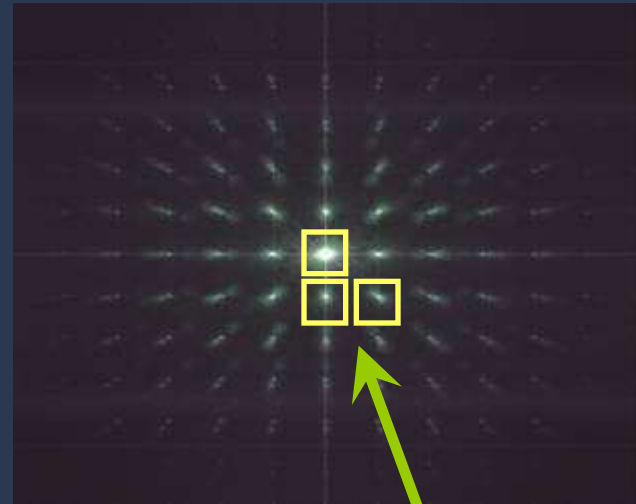
# Computing 4D Light Field

2D Sensor Photo, 1800\*1800



2D  
FFT

2D Fourier Transform



$9 \times 9 = 81$  spectral copies



Rearrange 2D tiles into 4D planes  
 $200 \times 200 \times 9 \times 9$

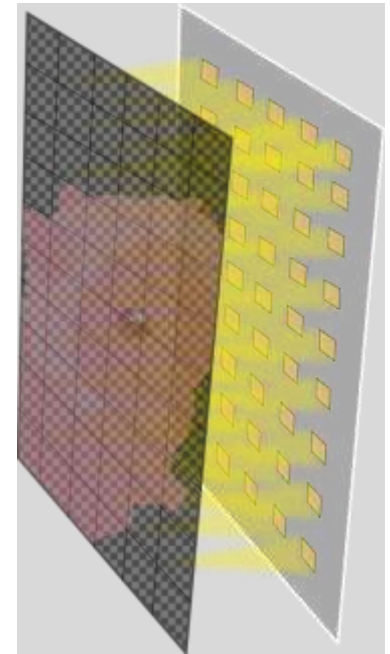
4D IFFT



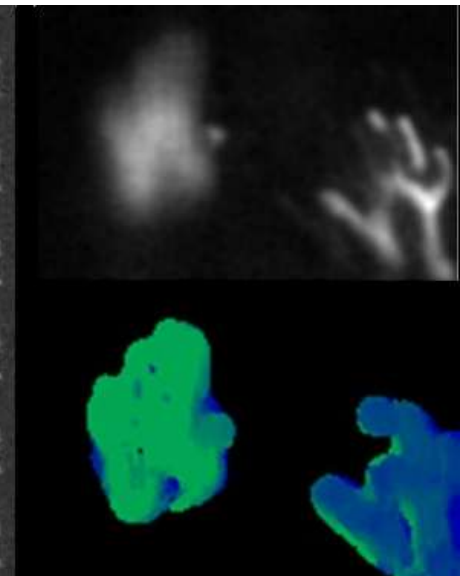
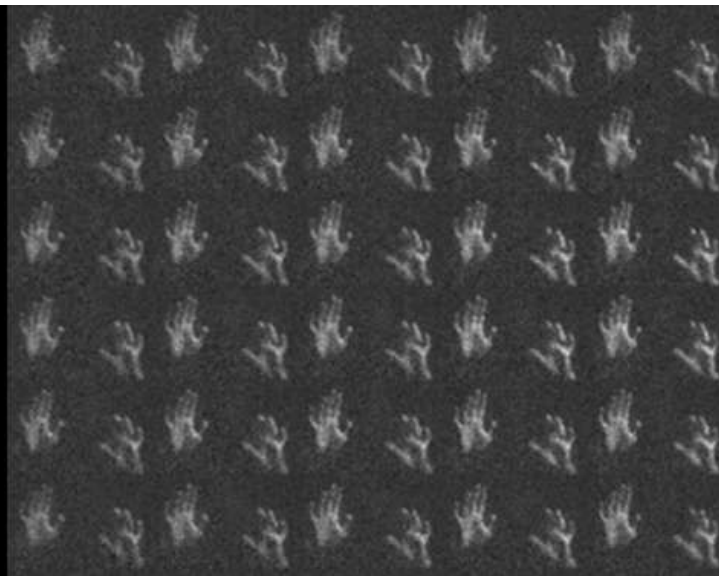
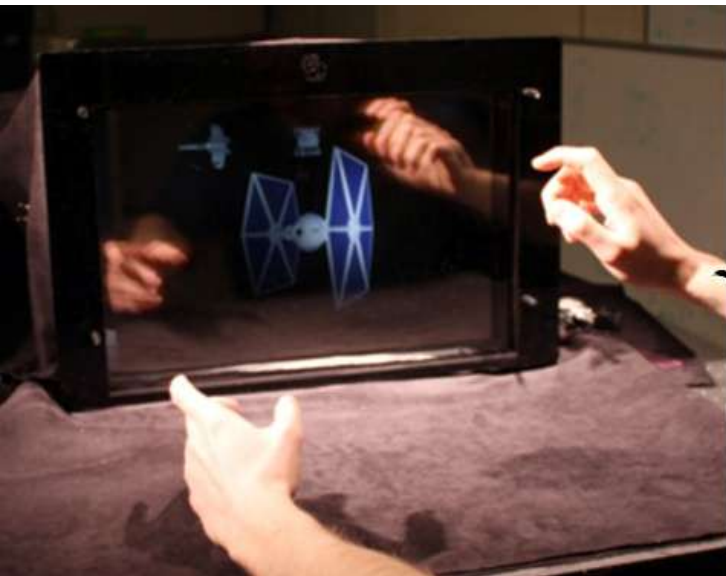
4D Light Field  
 $200 \times 200 \times 9 \times 9$



# BiDi Screen: Thin LCD for touch+hover



Sensing Depth from Light Sensing LCD  
By creating Array of Virtual Cameras in LCD

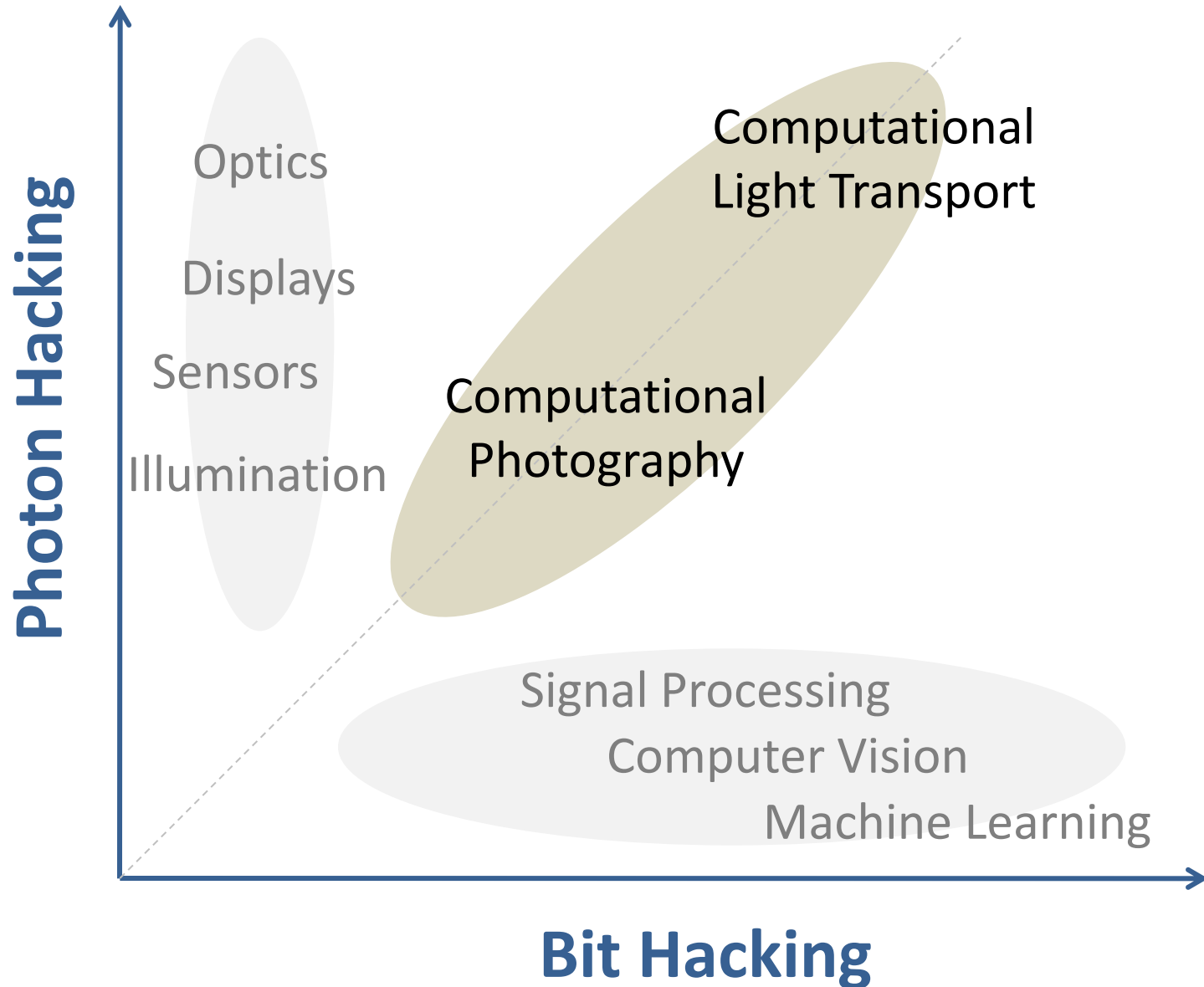


# BiDi Screen: Multi-touch + Hover 3D interface

LCD = Large Lensless Camera



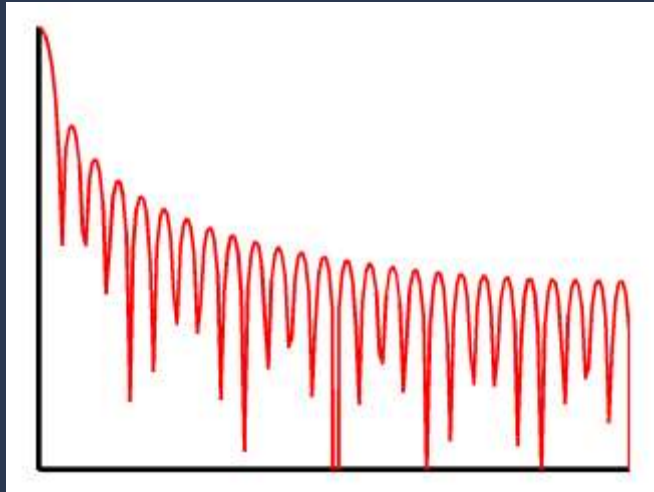
# Co-designing Optical and Digital Processing



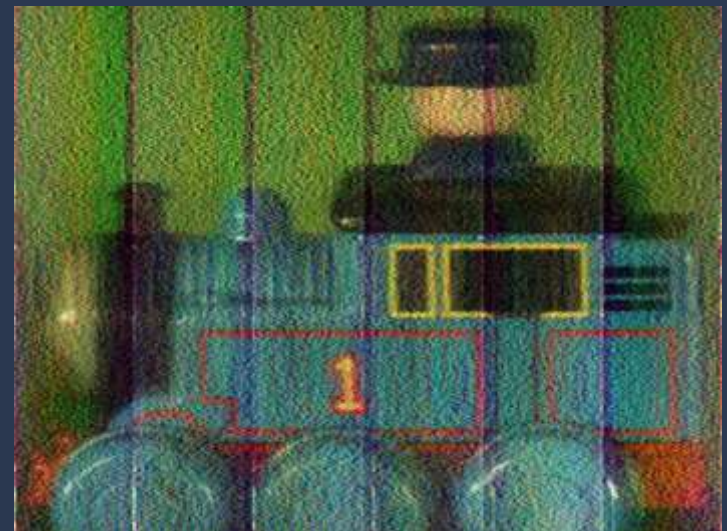
# Motion Blur in Low Light



Traditional



Blurred Photo



Deblurred Image



# Fluttered Shutter Camera

Raskar, Agrawal, Tumblin Siggraph2006

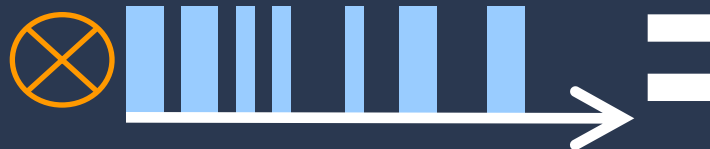


Ferroelectric shutter in front of the lens is turned opaque or transparent in a rapid binary sequence





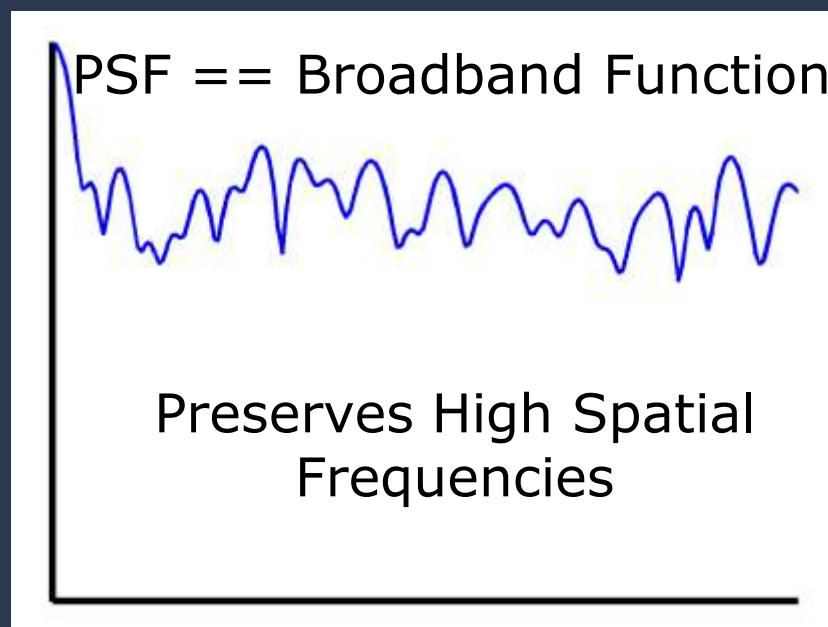
Sharp  
Photo



Fourier  
Transform

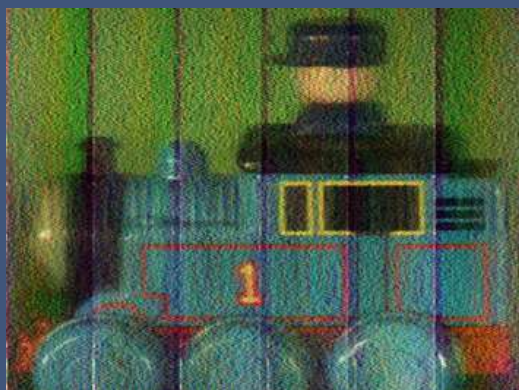
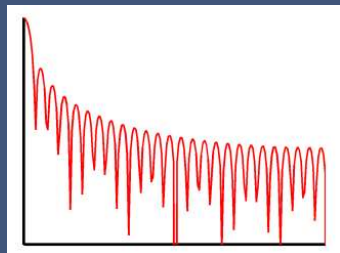


Blurred  
Photo



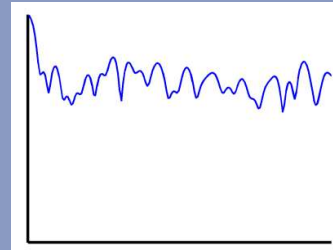
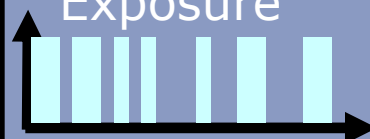
Flutter Shutter: Shutter is OPEN and CLOSED

Traditional



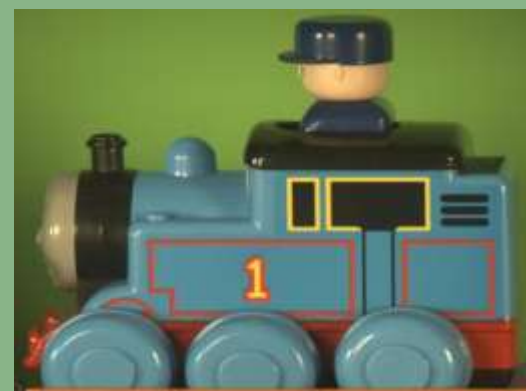
Deblurred  
Image

Coded  
Exposure

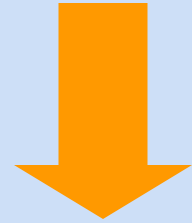


Deblurred  
Image

Image of  
Static  
Object

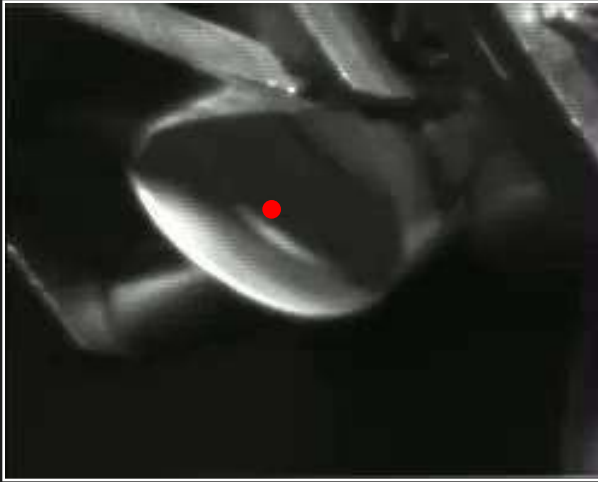


# Motion Blur in Low Light



# Fast periodic phenomena

Bottling line



500 fps hi-speed camera

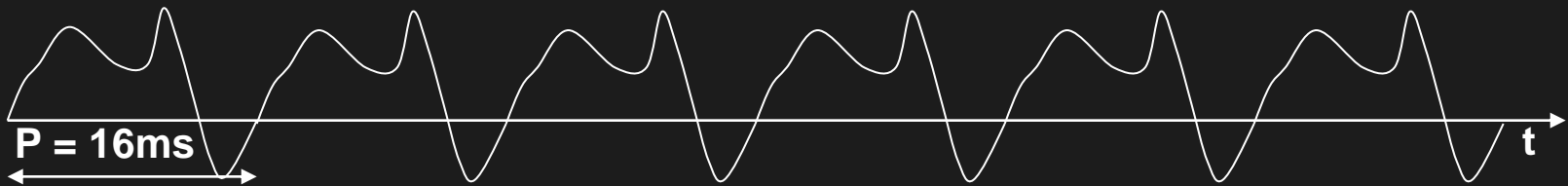
Vocal folds flapping at 40.4 Hz



4000 fps hi-speed camera

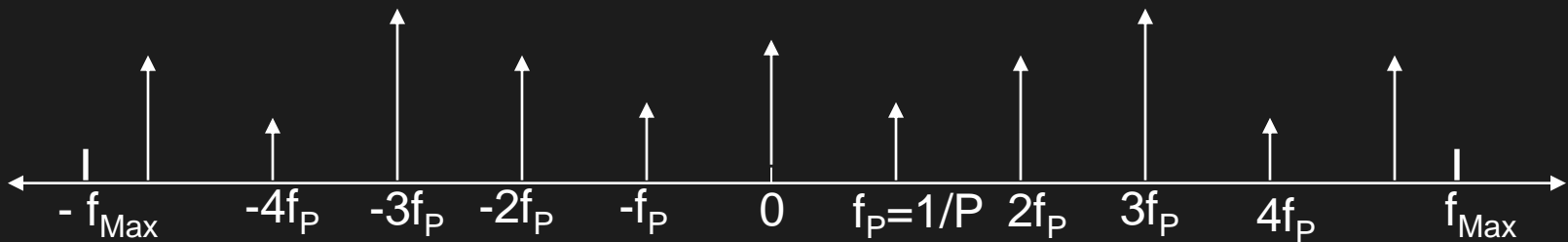
# Periodic signals

Periodic signal  $x(t)$  with period  $P$



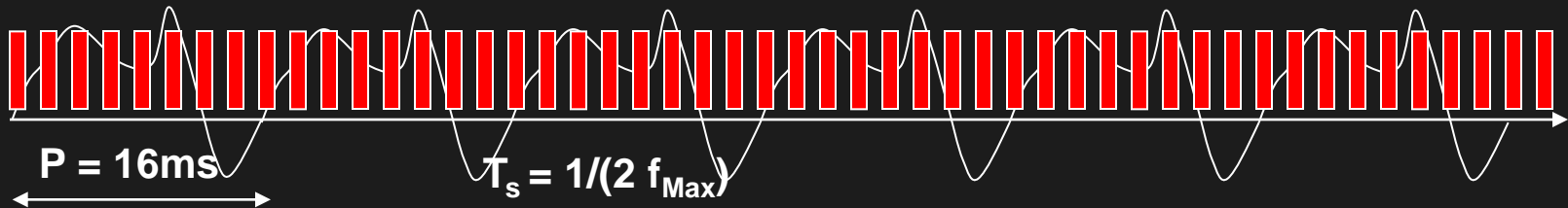
Periodic signal with period  $P$  and **band-limited to  $f_{\text{Max}} = 500\text{ Hz}$ .**

Fourier transform is non-zero only at **multiples of  $f_P = 1/P \sim 63\text{Hz}$ .**



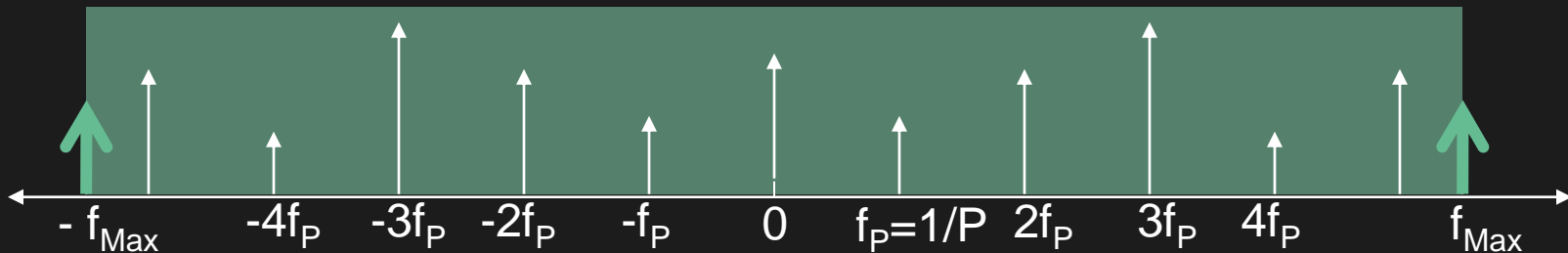
# High speed camera

## Nyquist Sampling of $x(t)$



Periodic signal has **regularly spaced, sparse** Fourier coefficients.

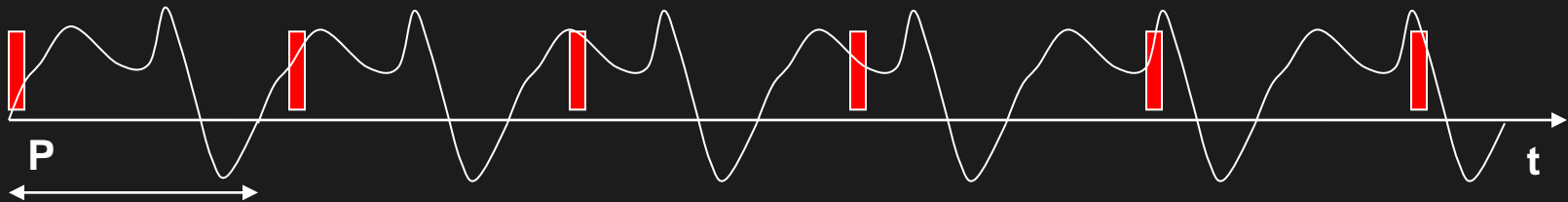
Is it necessary to use a high-speed video camera? Why **waste bandwidth**?





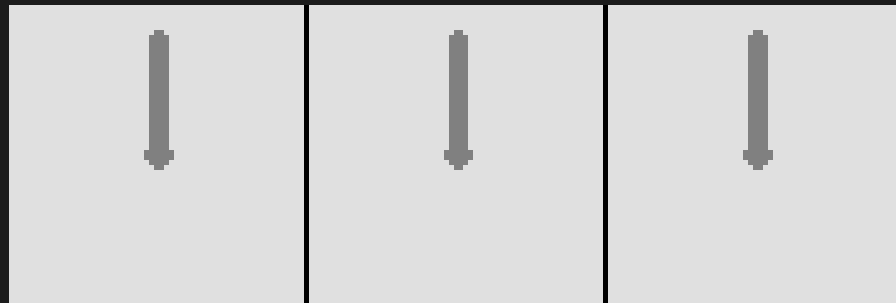
# Traditional Strobbing

Use low frame-rate camera and **generate beat frequencies.**



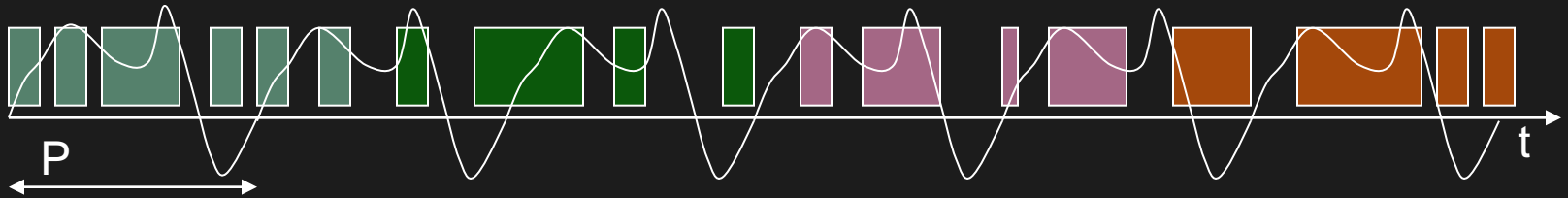
Low exposure to avoid blurring. **Low light throughput.**

Period known **apriori.**



# Random Projections Per Frame of Camera using Coded Strobing Photography

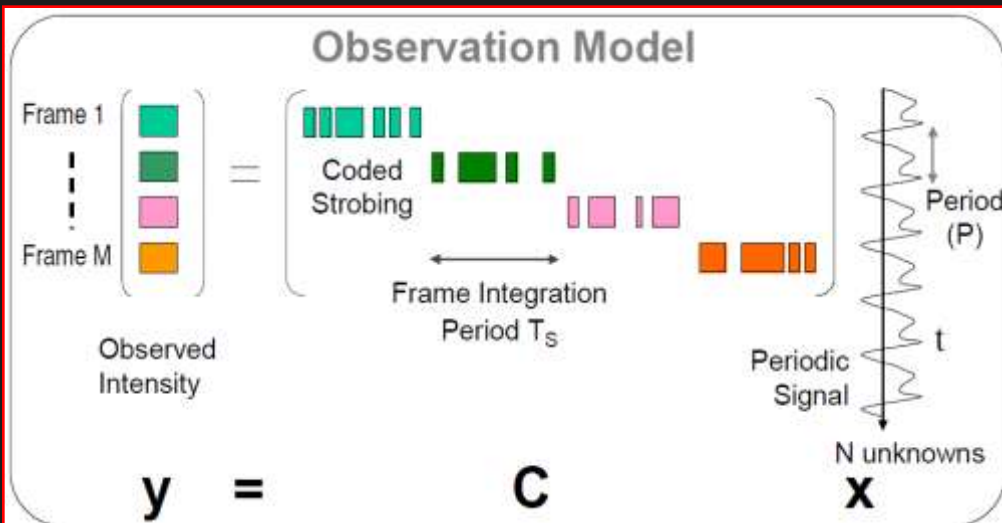
In every exposure duration observe different linear combinations of the periodic signal.



## Advantage of the design

- Exposure coding independent of the frequency
- On an average, light throughput is 50%

# Observation Model

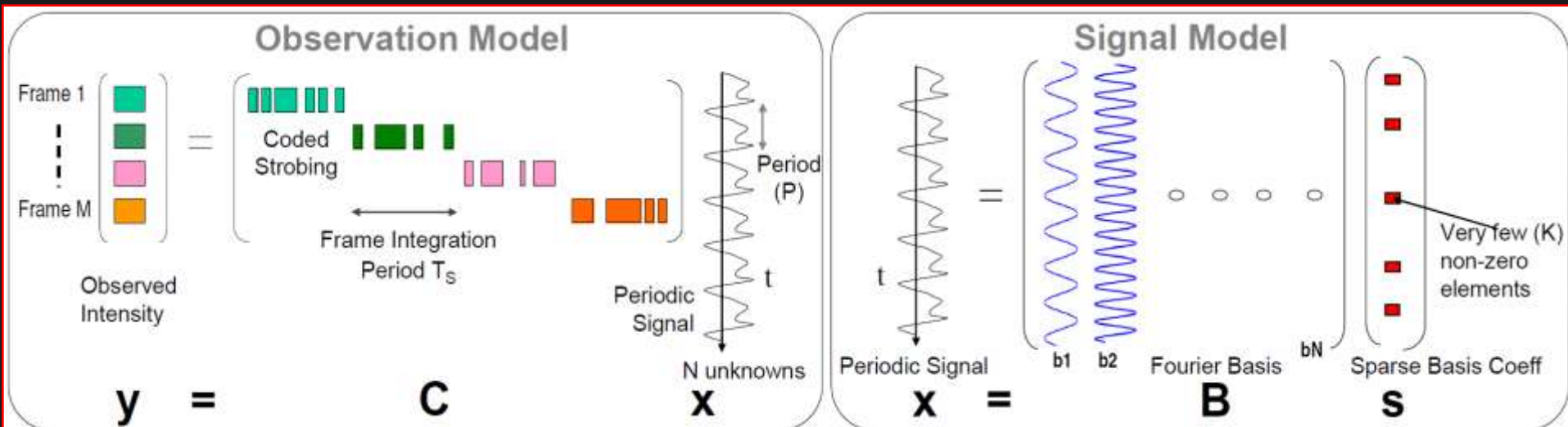


**y at 25fps**



**x at 2000fps**

# Signal Model

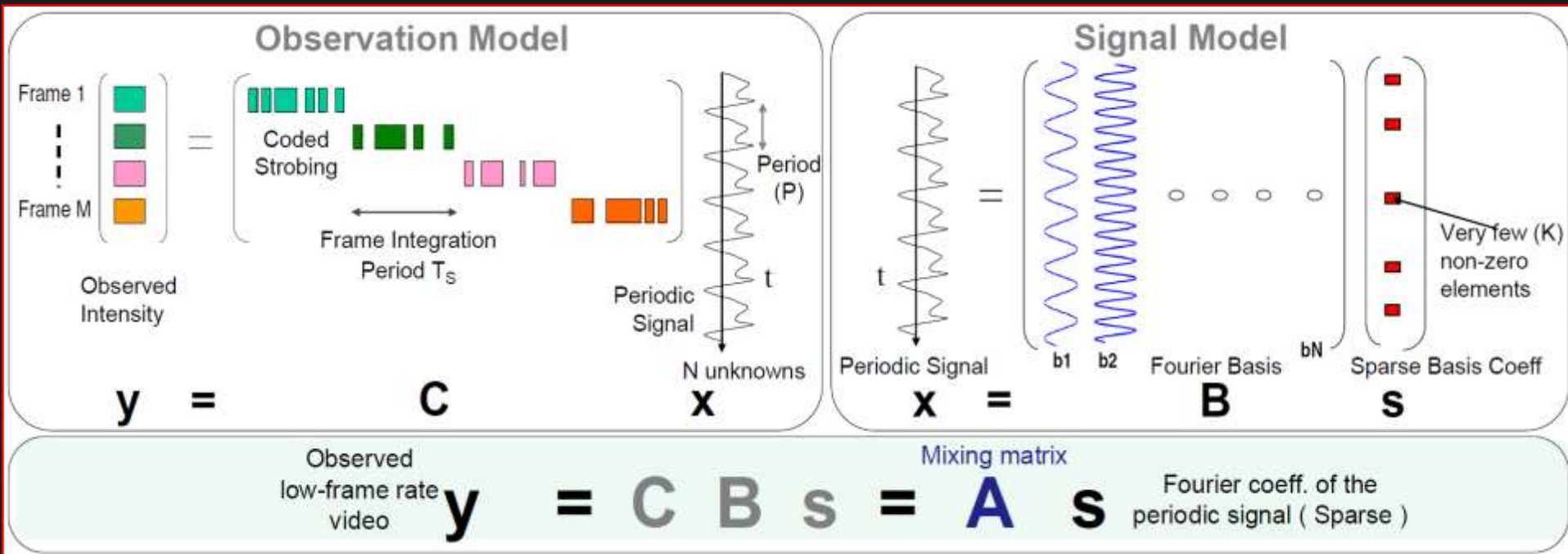


$y$  at 25fps



$x$  at 2000fps

# Signal & Observation Model



$y$  at 25fps

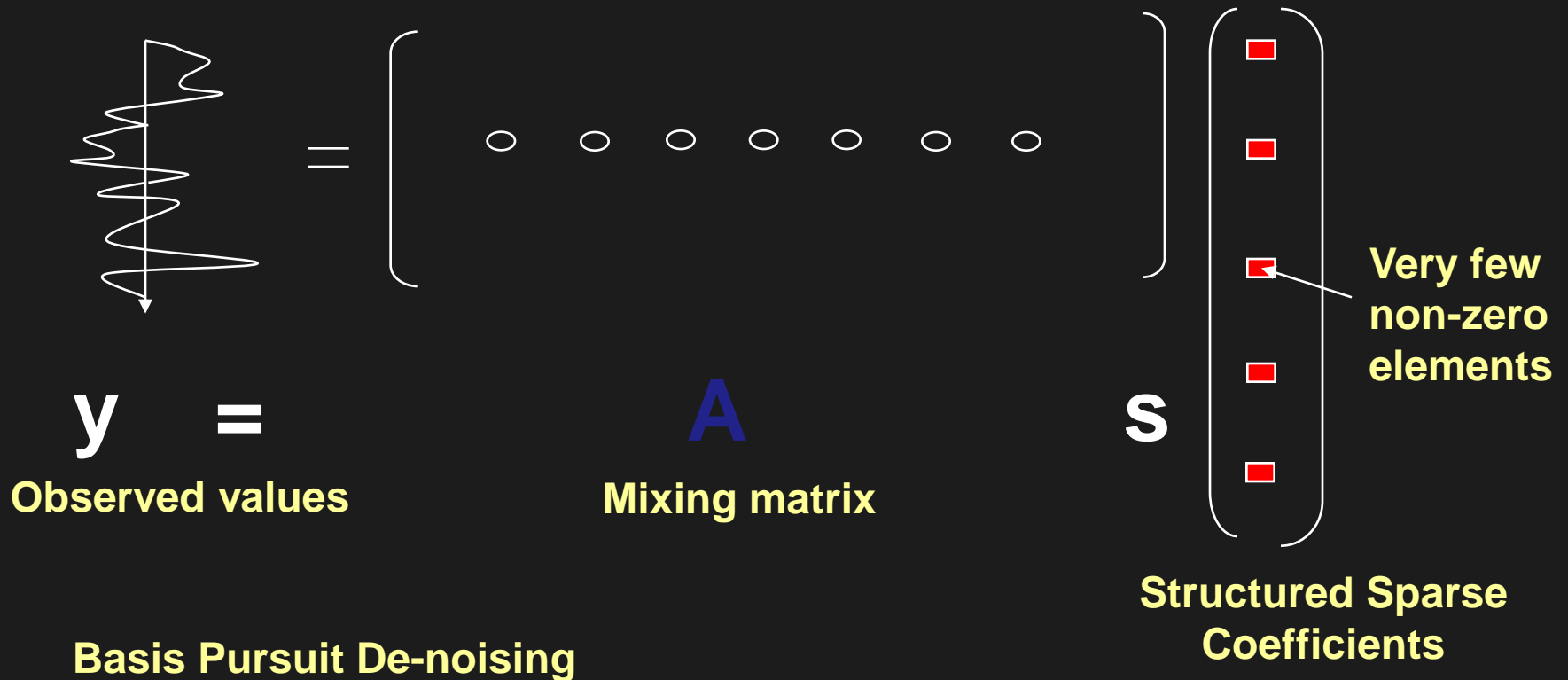


$x$  at 2000fps

$$N / M = 2000 / 25 = 80$$

$A$  is  $M \times N$ ,  $M \ll N$

# Recovery: Sparsity



$$\min \|s\|_1 \quad s.t. \quad \|y - As\| \leq \varepsilon$$



# Simulation on hi-speed toothbrush



**25fps normal camera**



**25fps coded strobing camera**



**Reconstructed frames**



**2000fps hi-speed camera**

~100X speedup

# Rotating mill tool

Mill tool rotating at 50Hz



Reconstructed Video at 2000fps



Normal Video: 25fps



Coded Strobing Video: 25fps

Blur increases as rotational velocity increases

rotating at 100Hz



rotating at 150Hz



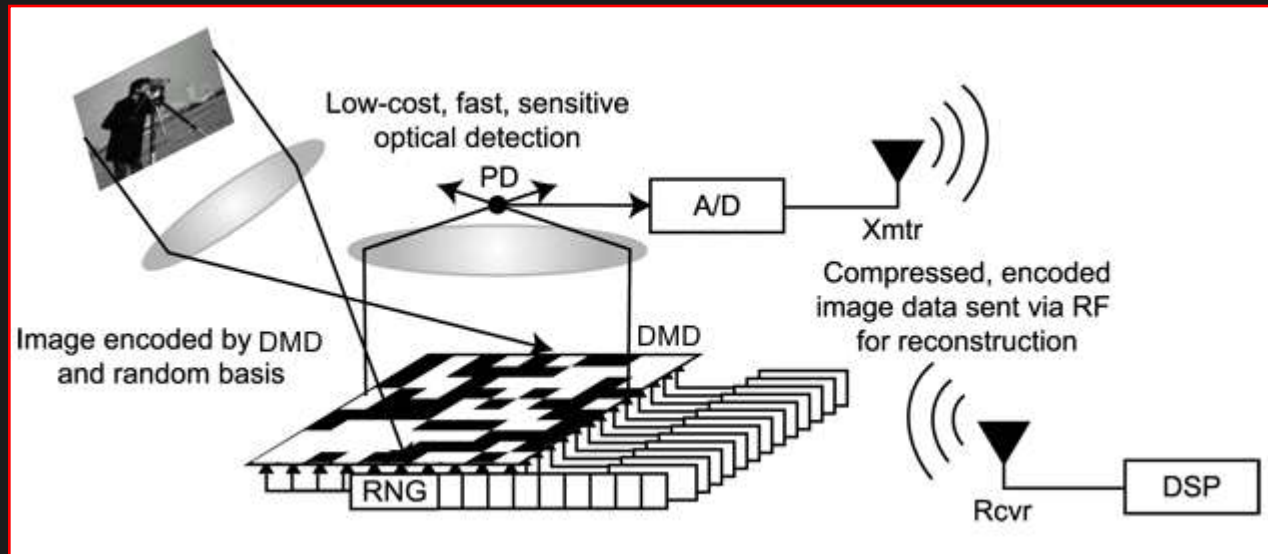
rotating at 200Hz



→  
increasing blur

# Compressive Sensing for Images .. A good idea?

## Single Pixel Camera

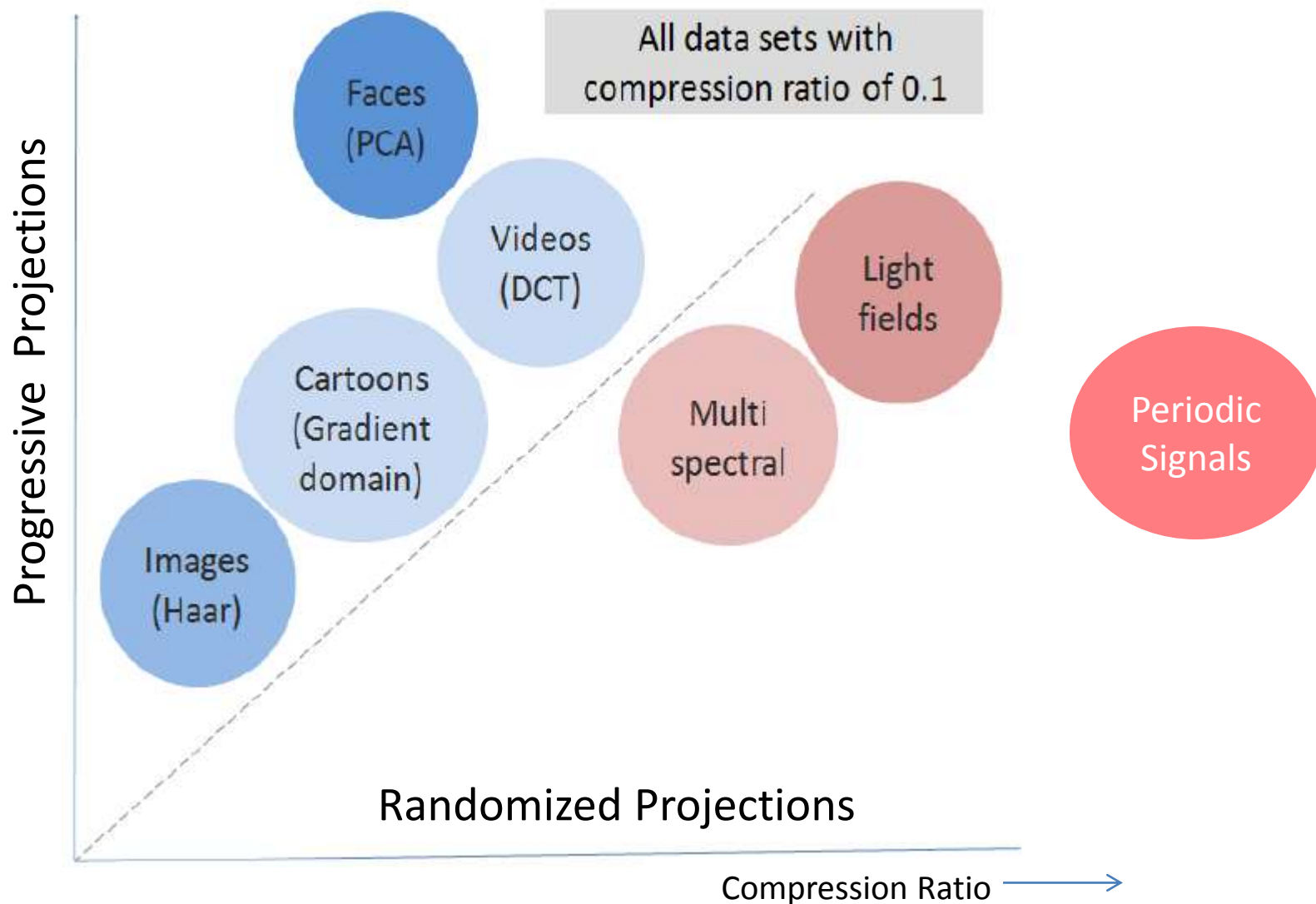


**compressive image**  $\rightarrow y = \Phi x$   $\rightarrow$  **image**

$\uparrow$  **measurement matrix**

$\Phi_{M \times N}$  where  $M < N$

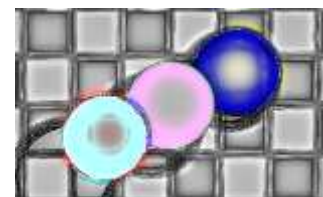
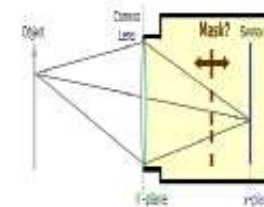
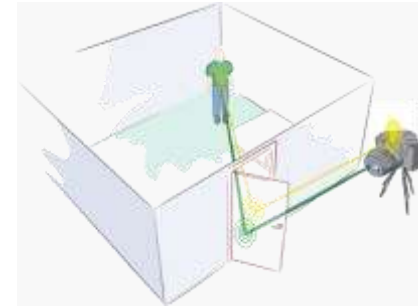
# Is Randomized Projection-based Capture apt for Natural Images ?



[Pandharkar, Veeraraghavan, Raskar 2009]

# Inverse Problems

- Co-design of Optics and Computation
  - Photons not just pixels
  - Mid-level cues
- Computational Photography
  - Coded Exposure
  - Compressive Sensing for High Speed Events
    - Limits of CS for general imaging
- Computational Light Transport
  - Looking Around Corners, trillion fps
  - Lightfields:
    - Compressive Campture
    - 3D Displays and Holograms

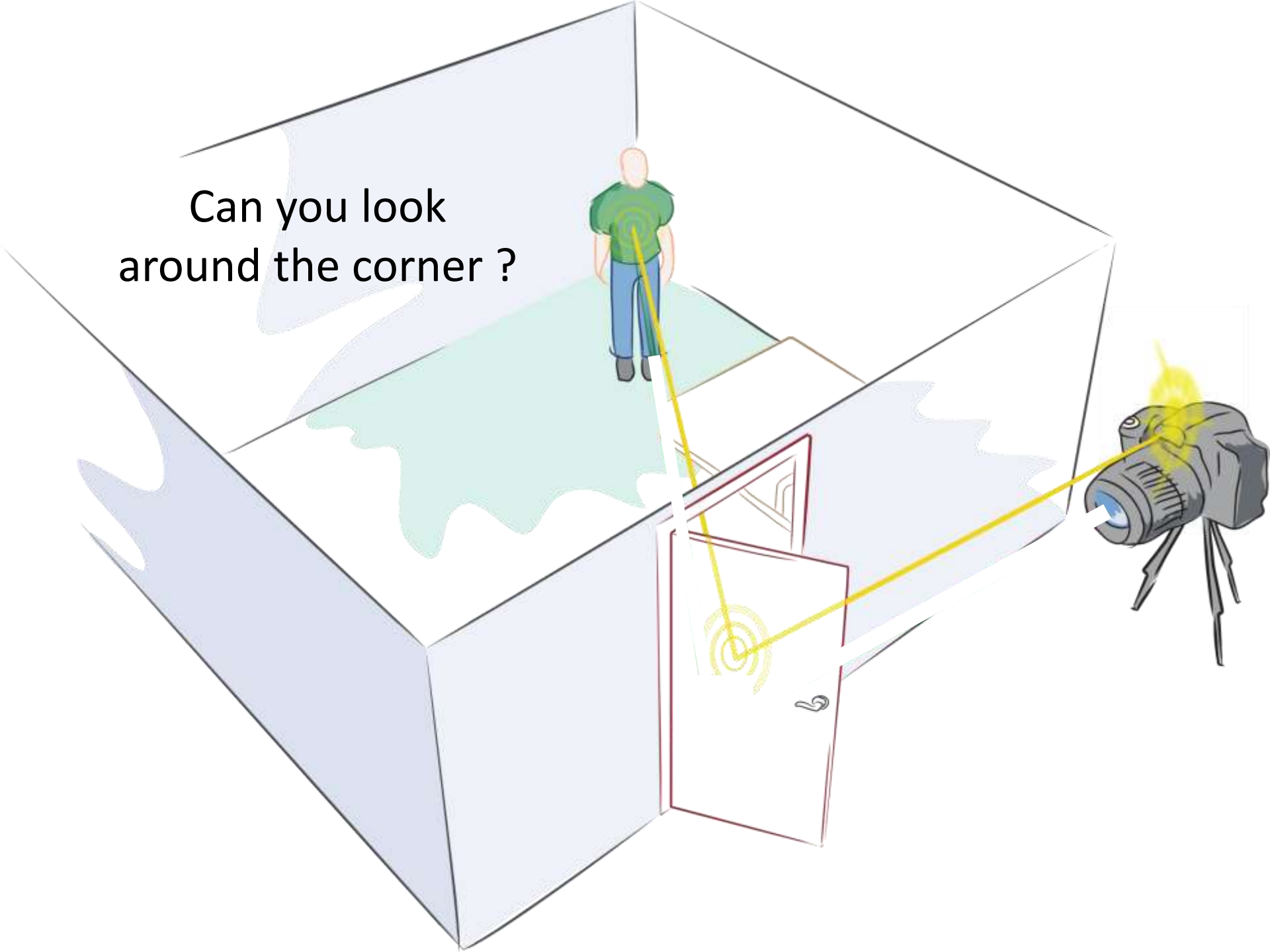


What is  
around the corner ?

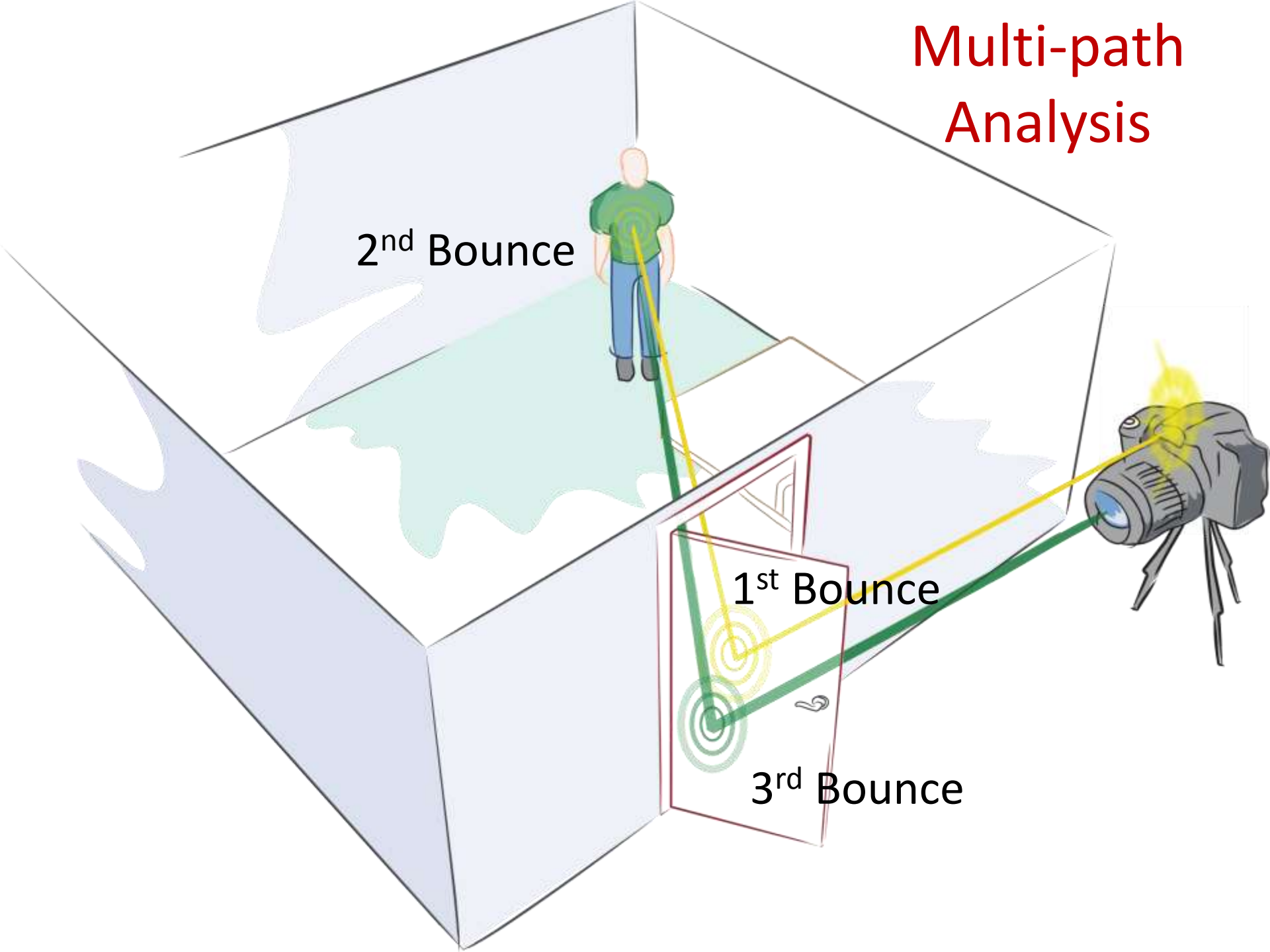




Can you look  
around the corner ?



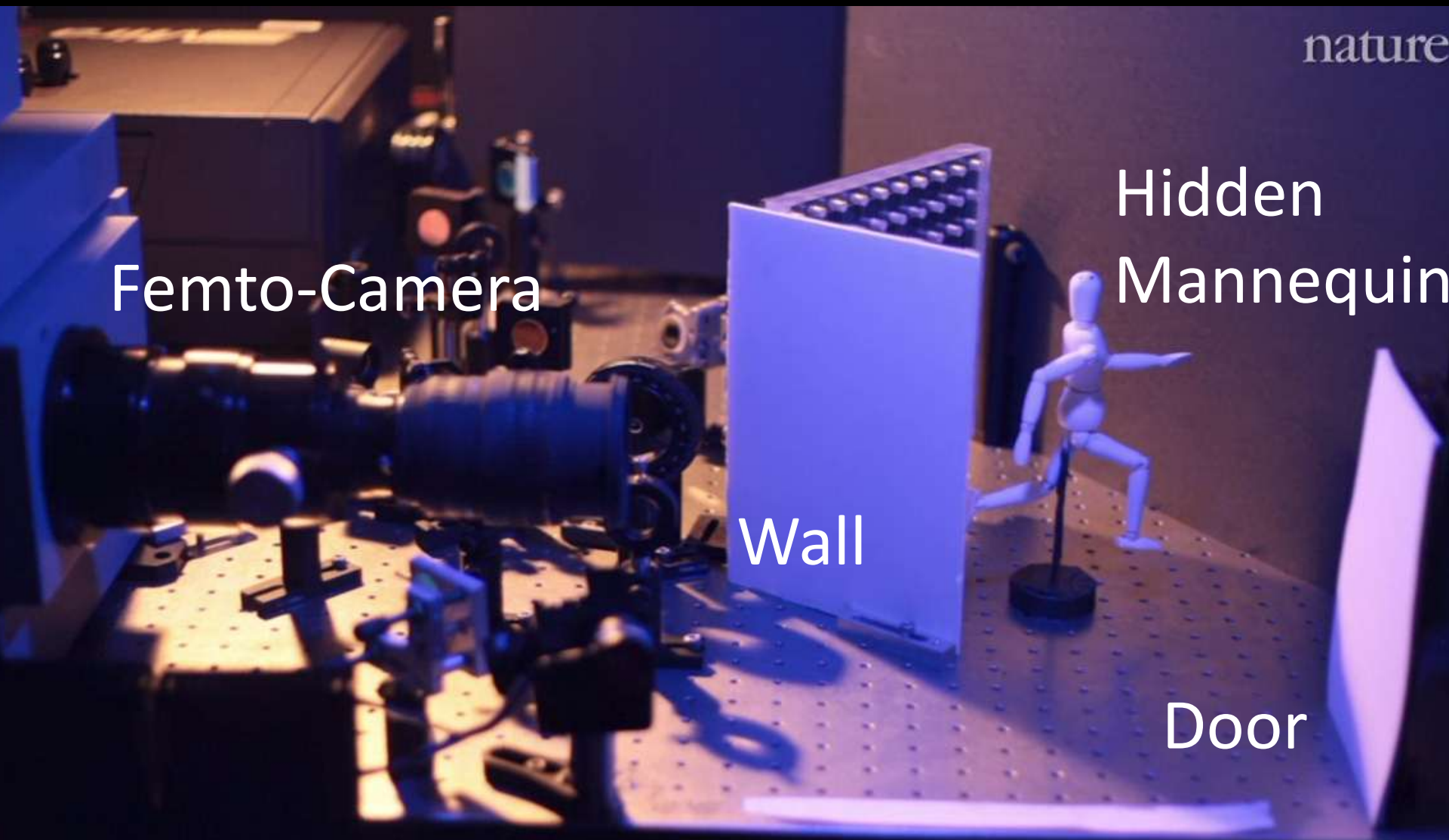
# Multi-path Analysis



# Light in Slow Motion ..



10 Billion x Slow



Femto-Camera

Hidden  
Mannequin

Wall

Door

Velten et al, **Nature Communications** 2012



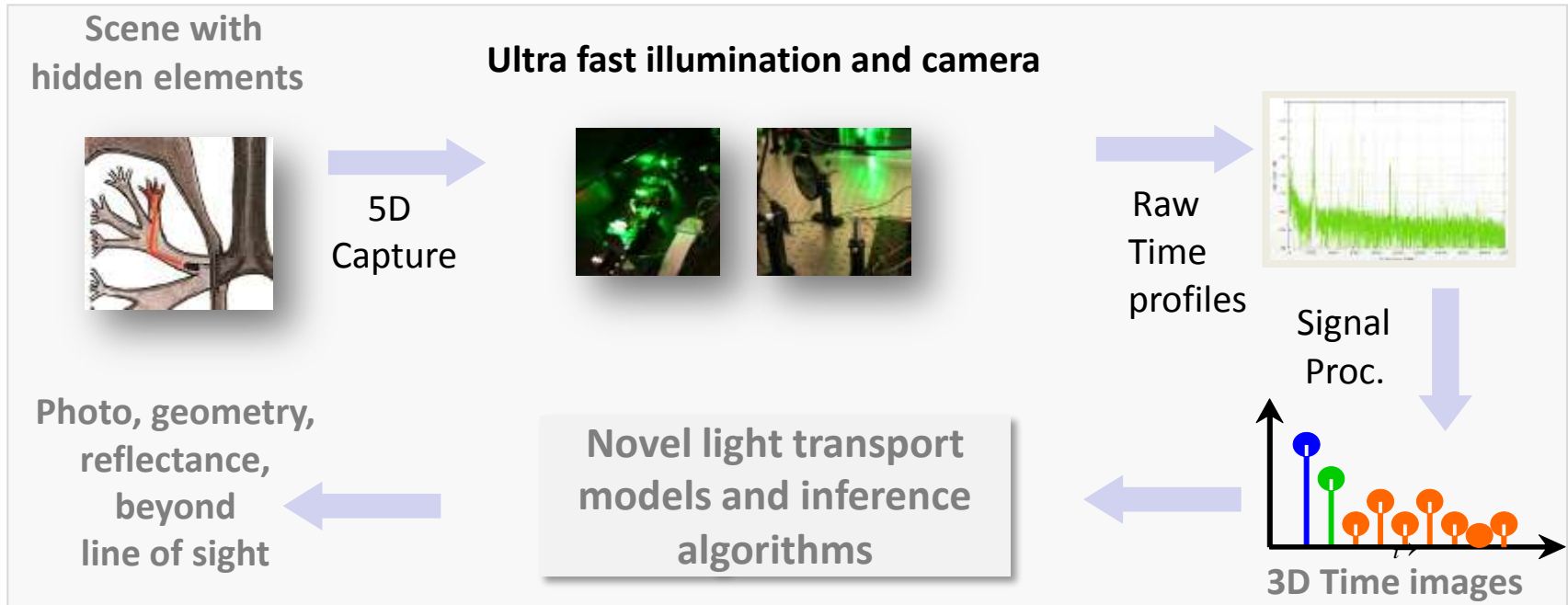






# Femto Photography

## Time Resolved Multi-path Imaging



**Tasks:**

Non-line of sight, Motion estimation, Material sensing, Volumetric

**Inversion:**

Sparsity, Rank, Bounded Approx, Scene Priors, Transforms

**Signal Processing:**

Compressive, SNR, Bandwidth, Noise models

**Illumination:**

Coding space/time/wavelength, Semicondctr lasers, nonlinear optics

**FormFactors:**

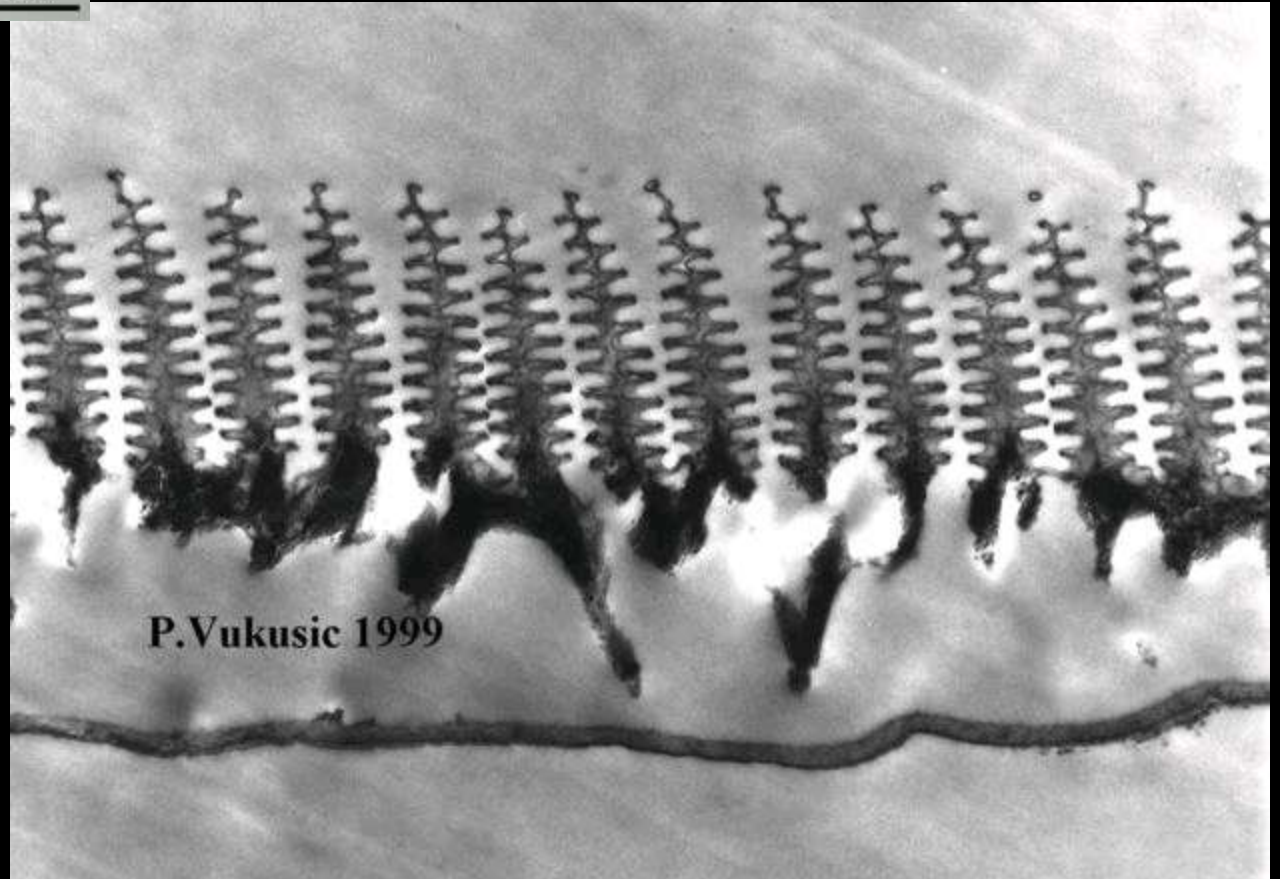
Endoscopy, OCT, Bench-top, Room size, Outdoors

**Applications:**

ComputerVision, MedicalImaging, Biochemistry, Rescue/Planning,  
IndustrialInspection, Robotics, Spectroscopy  
Art/Education

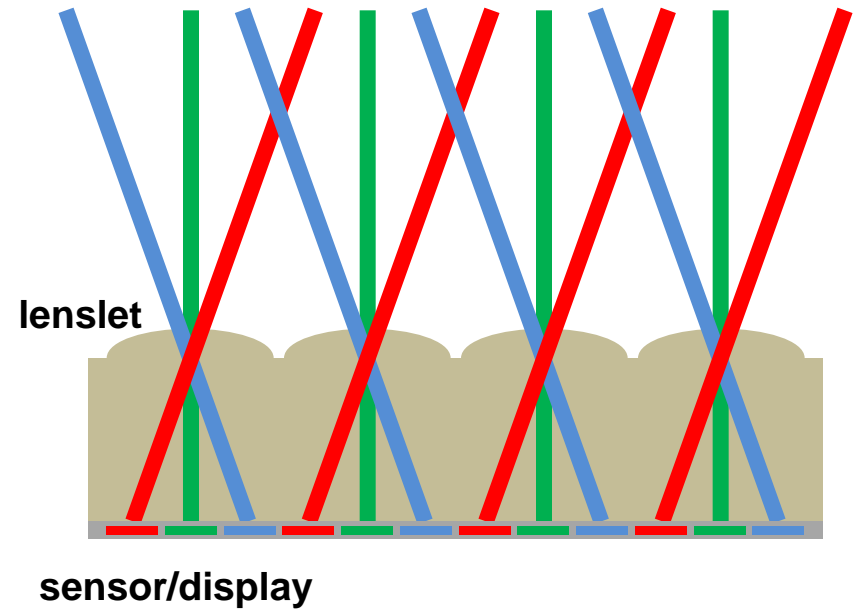
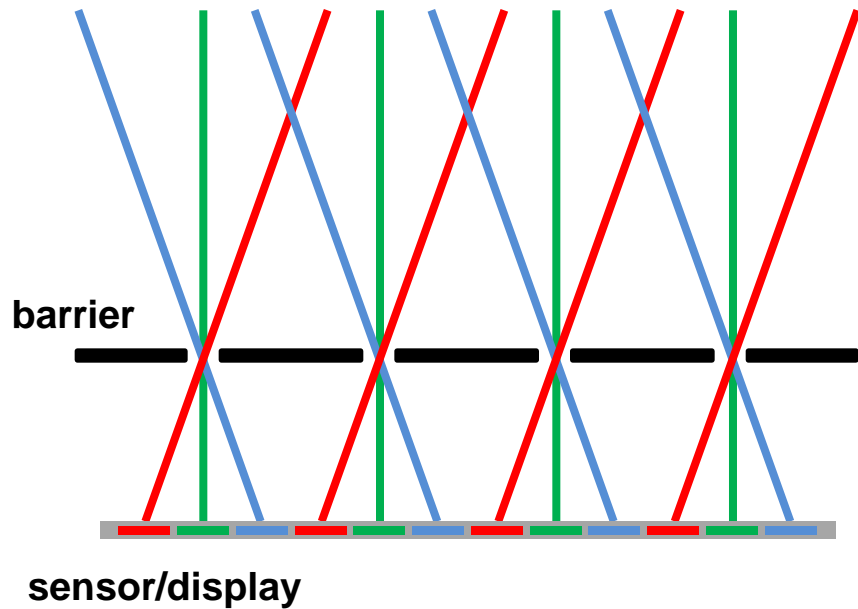
Collaborations Welcome/ Apply for internships





View Dependent Appearance and Iridescent color  
Cross section through a single *M. rhetenor* scale

# Two Layer Displays

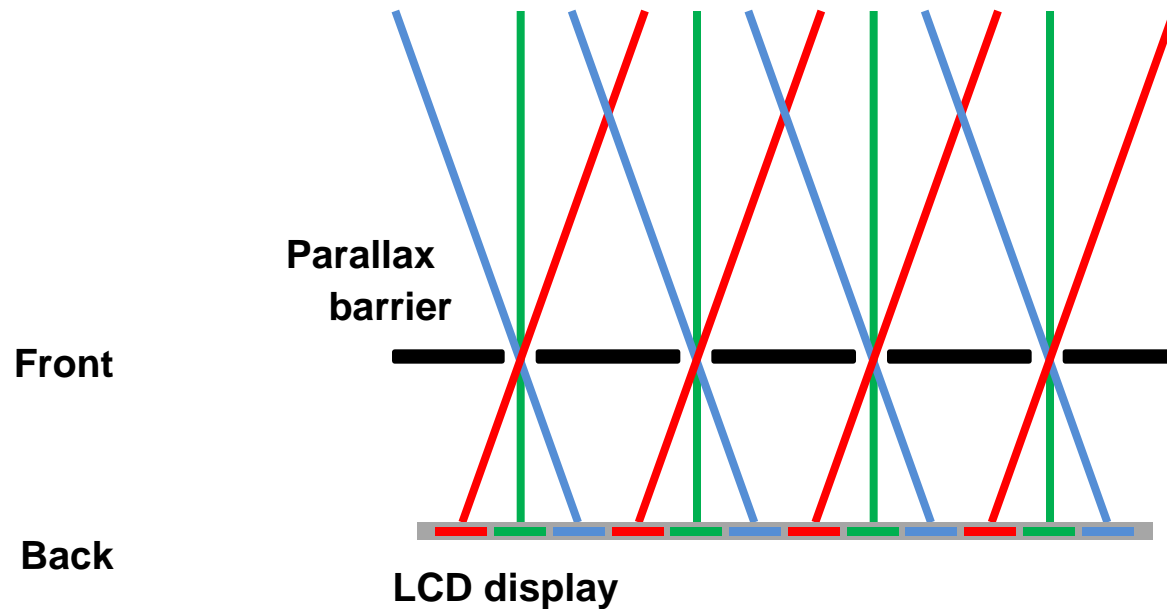


PB = dim displays

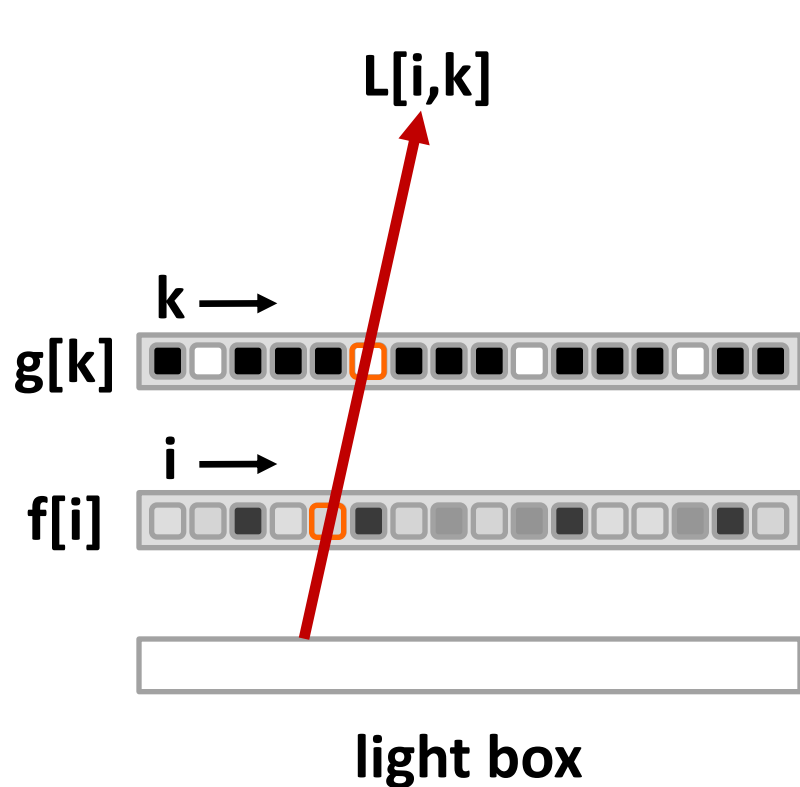
Lenslets = fixed spatial and angular resolution

Dynamic Masks = Brighter, High spatial resolution

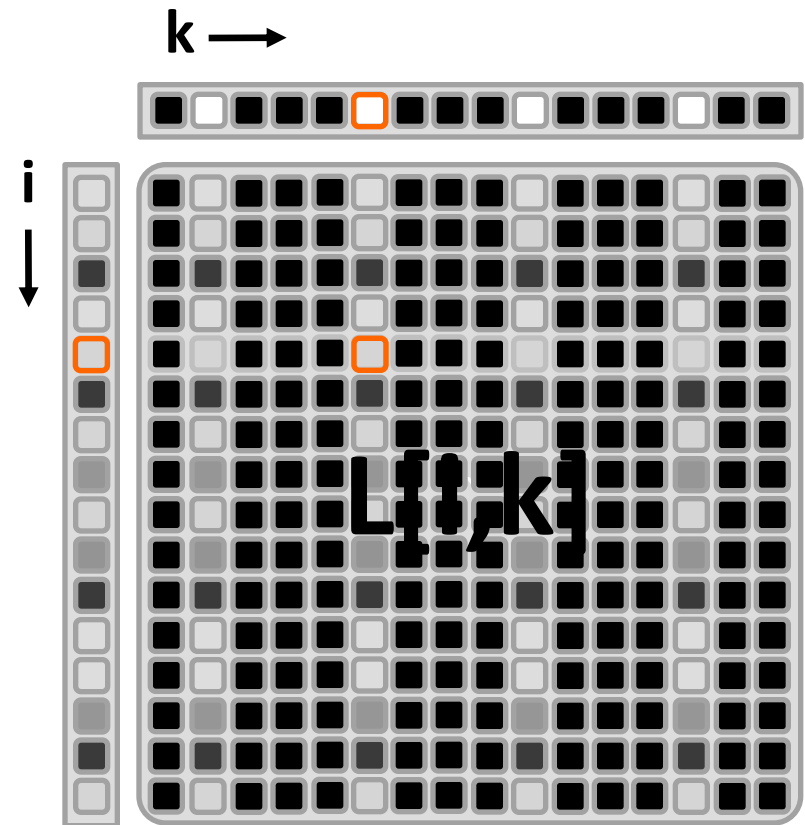
# Limitations of 3D Display



# Light Field Analysis of Barriers



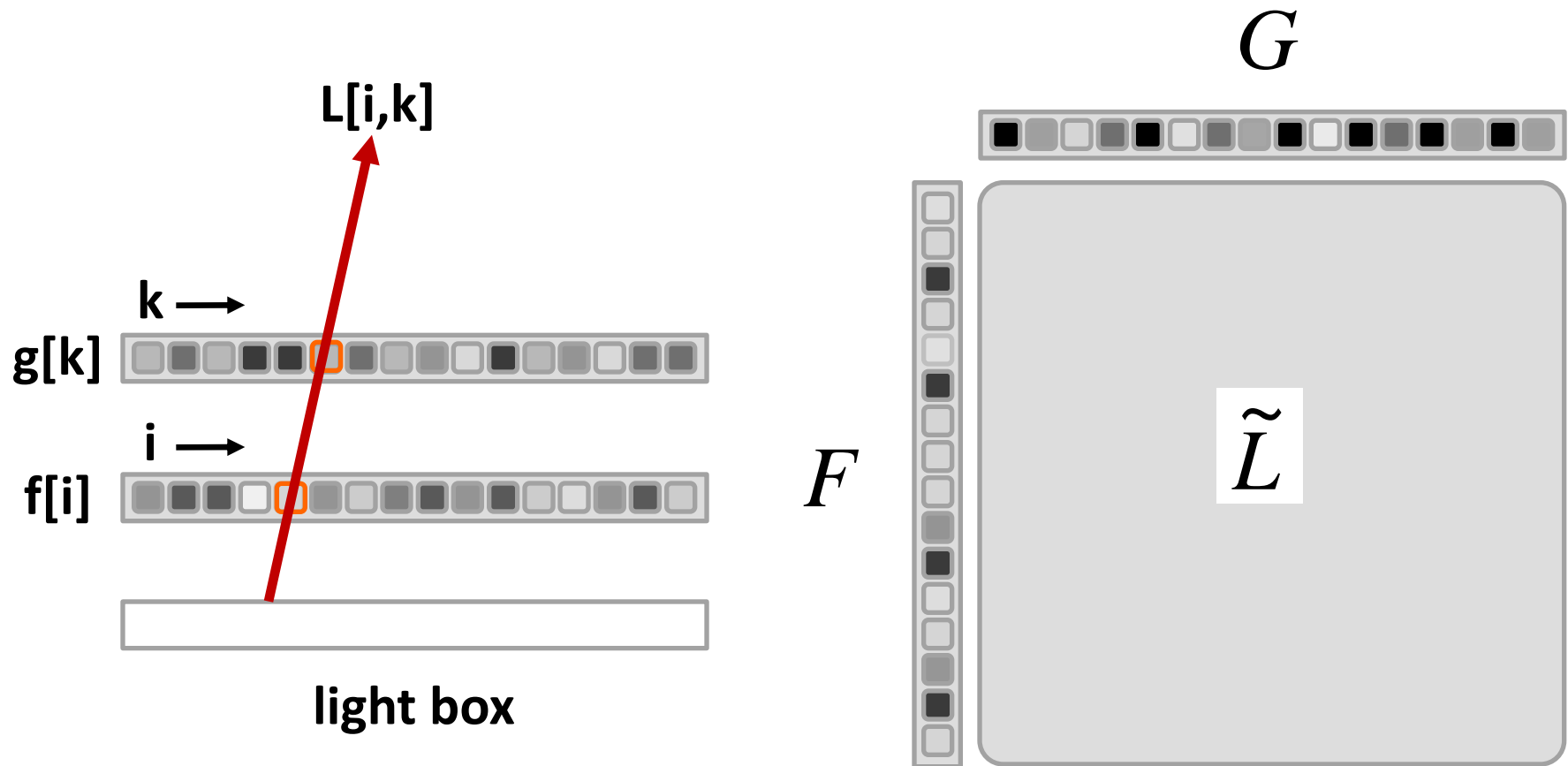
$$L[i,k] = f[i] \cdot g[k]$$



$$L = f \otimes g$$

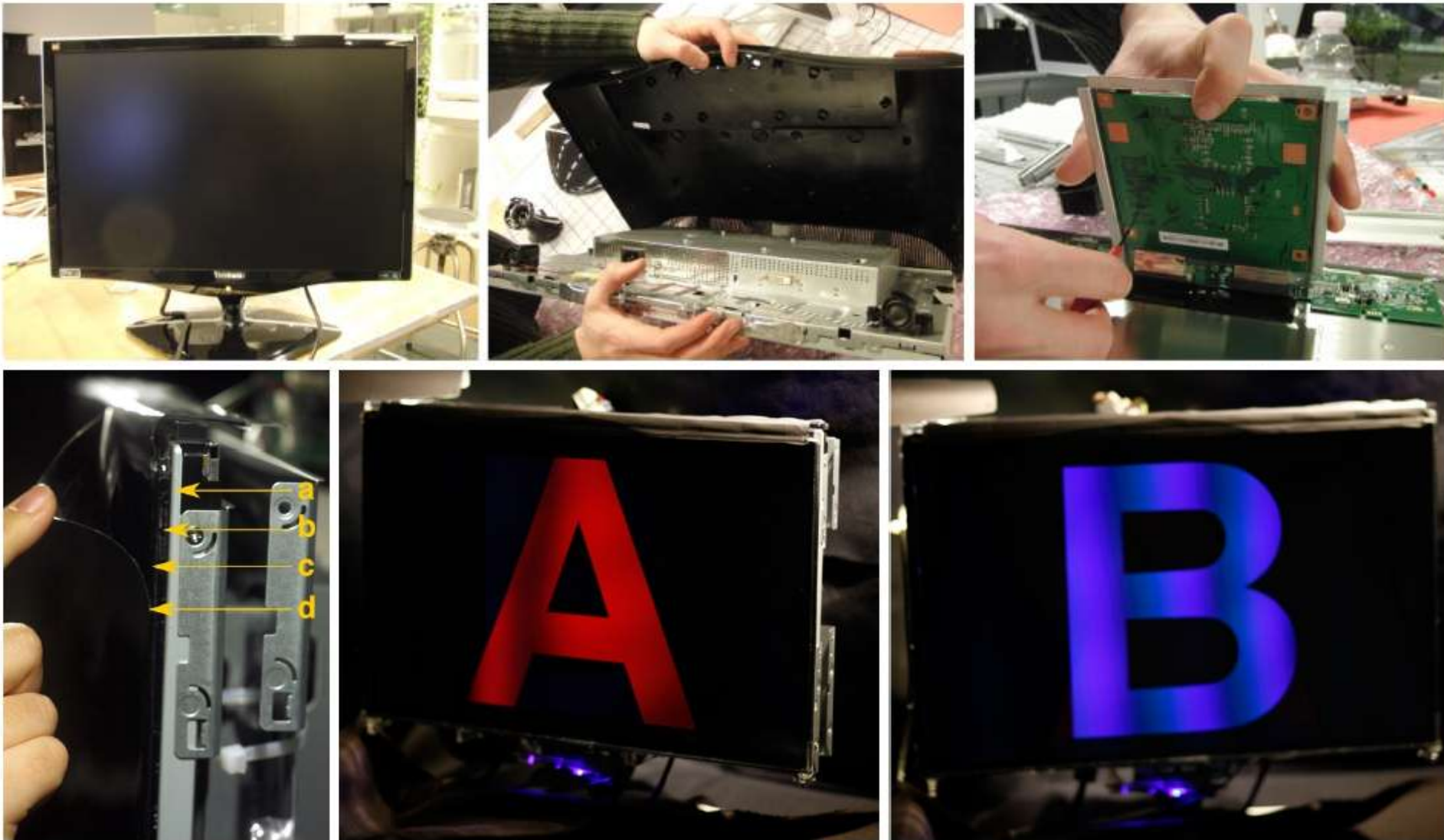


# Content-Adaptive Parallax Barriers



$$\tilde{L} = FG$$

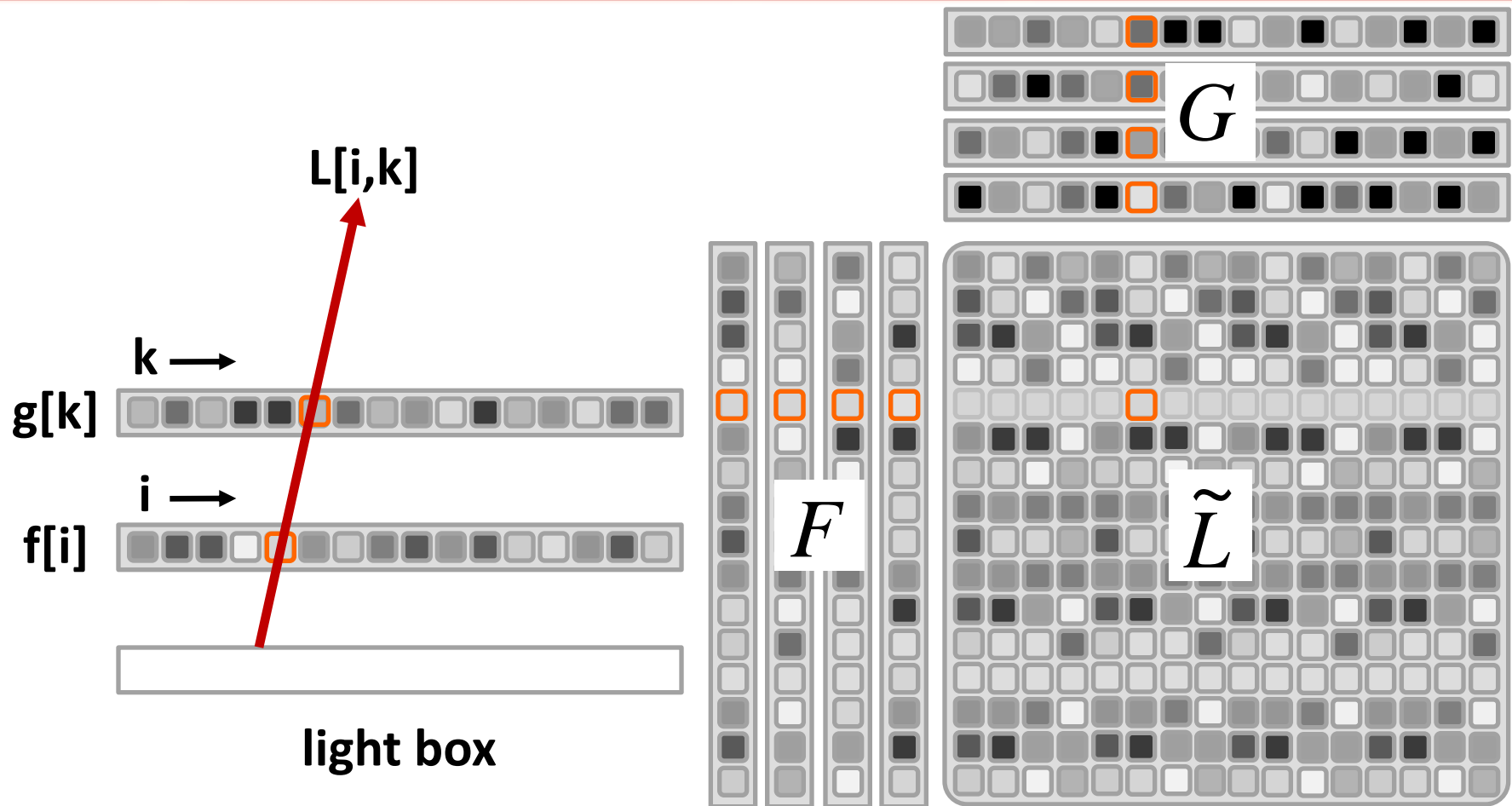
# Implementation



## Components

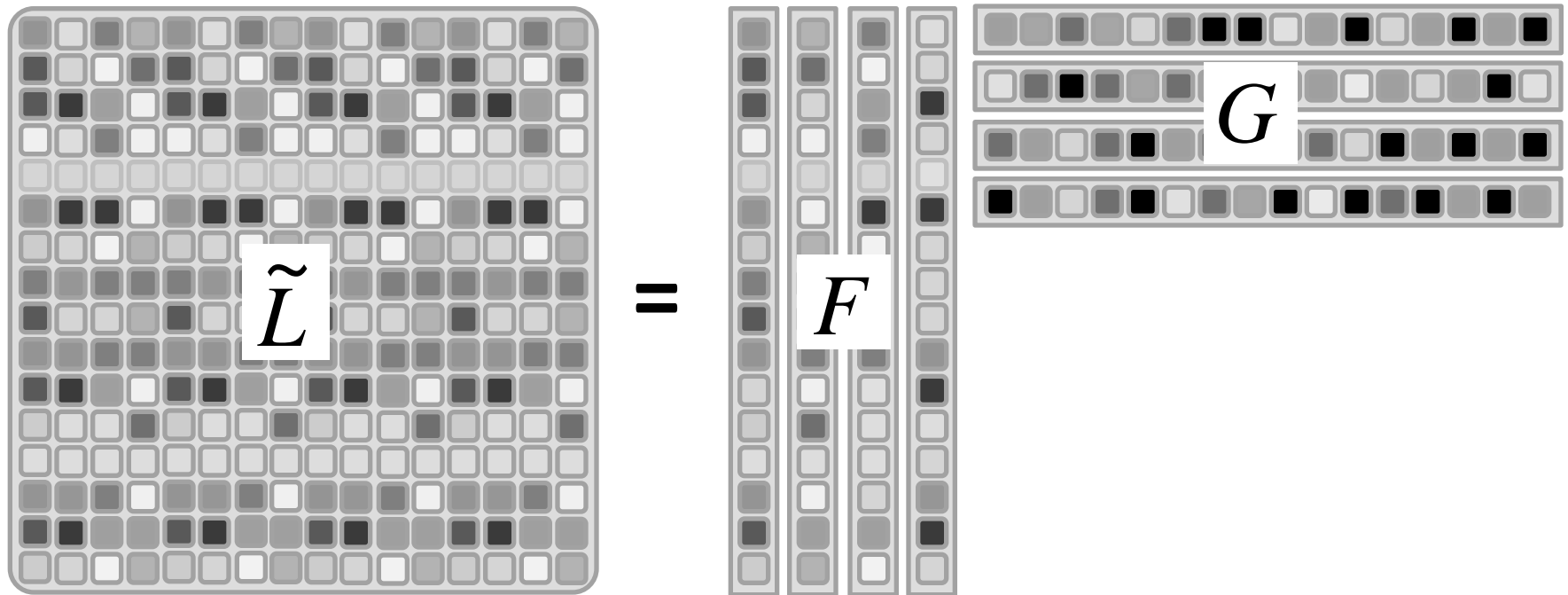
- 22 inch ViewSonic FuHzion VX2265wm LCD [1680 × 1050 @ 120 fps]

# Content-Adaptive Parallax Barriers



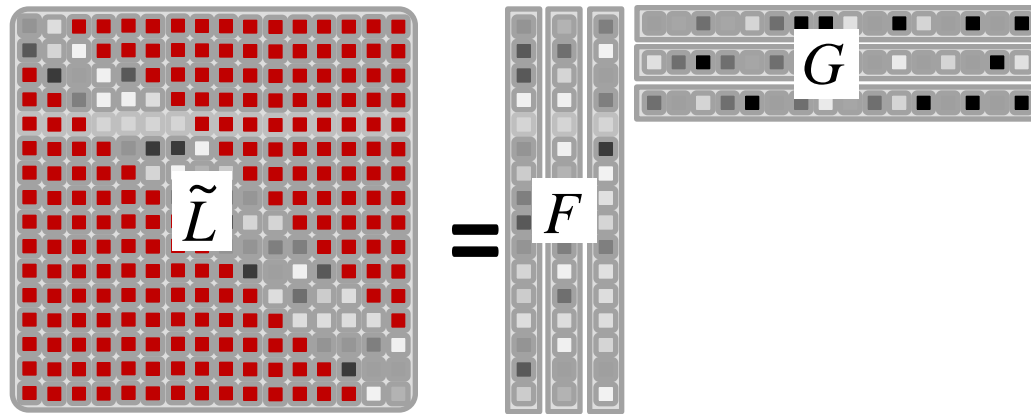
$$\tilde{L} = FG$$

# Content-Adaptive Parallax Barriers

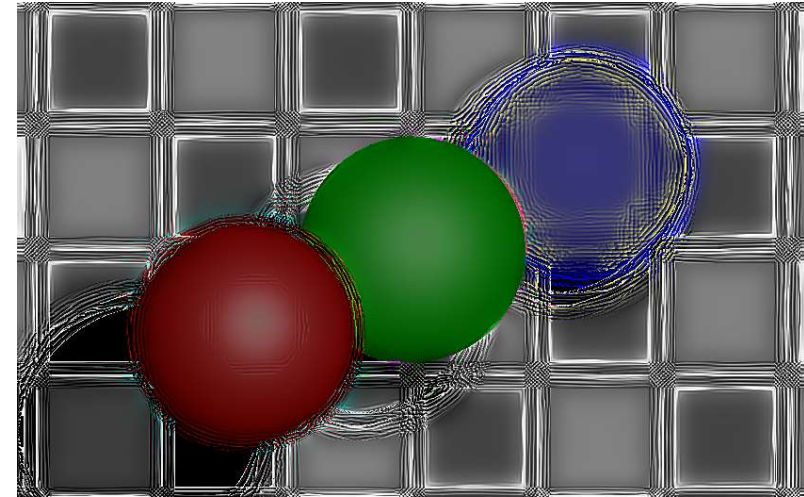


$$\arg \min_{F, G} \frac{1}{2} \|L - FG\|^2, \text{ for } F, G \geq 0$$

# Rank-Constrained Displays and LF Adaptation



$$\arg \min_{F,G} \frac{1}{2} \|L - FG\|_w^2, \text{ for } F, G \geq 0$$



**Content-Adaptive Parallax Barriers**

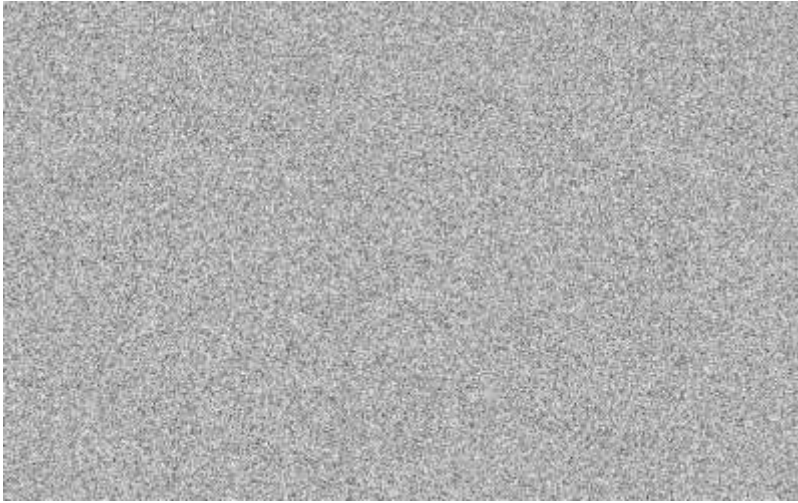
All dual layer display = *rank-1 constraint*

Light field display is a *matrix approximation problem*

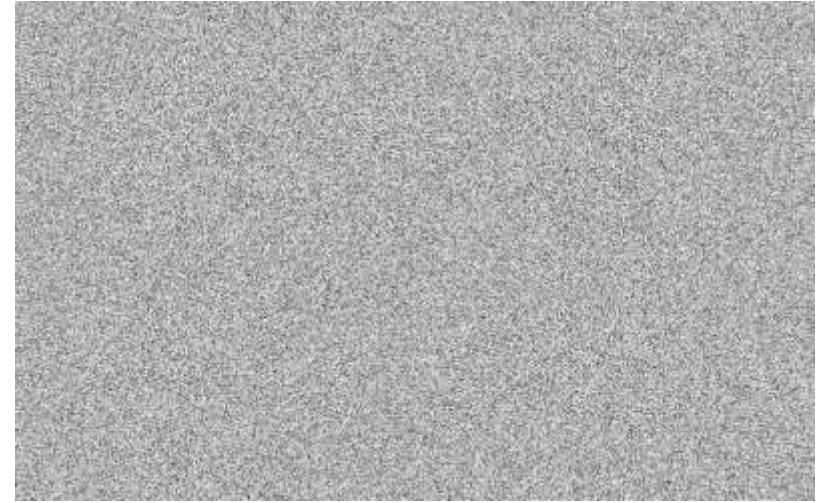
Exploit *content-adaptive parallax barriers*



# Optimization: Iteration 1



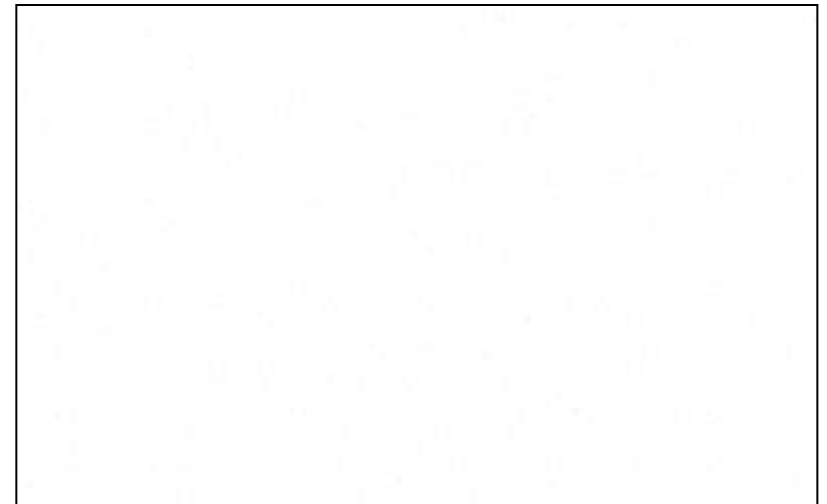
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

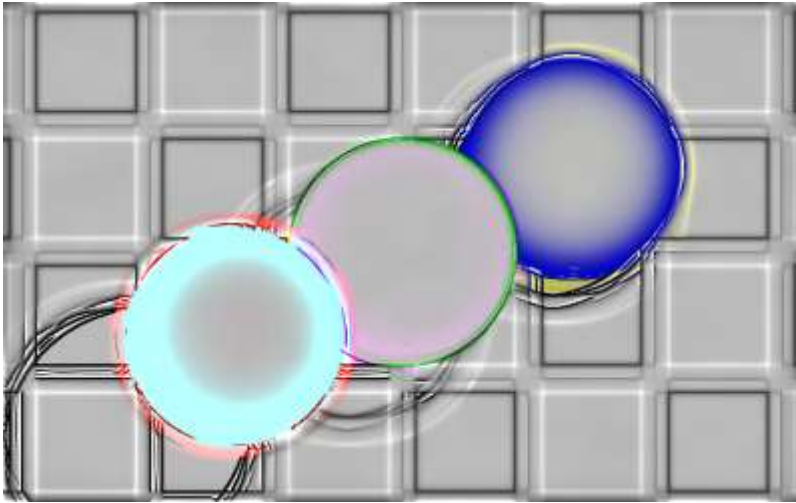
$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$



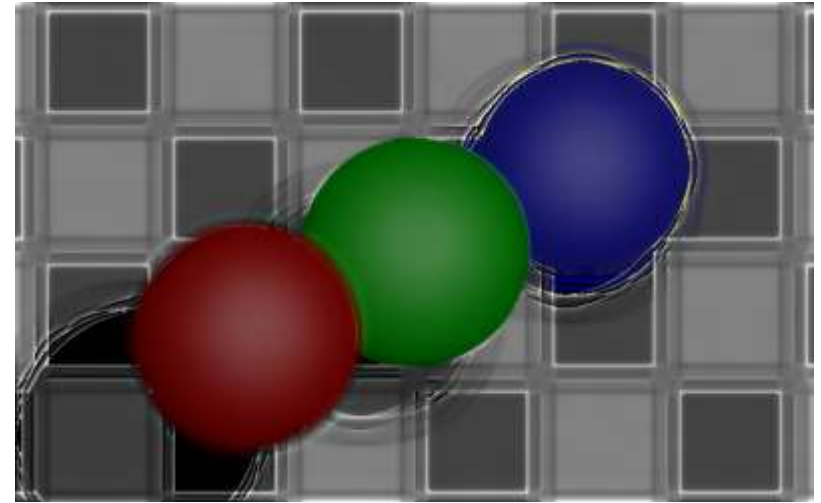
reconstruction (central view)



# Optimization: Iteration 10



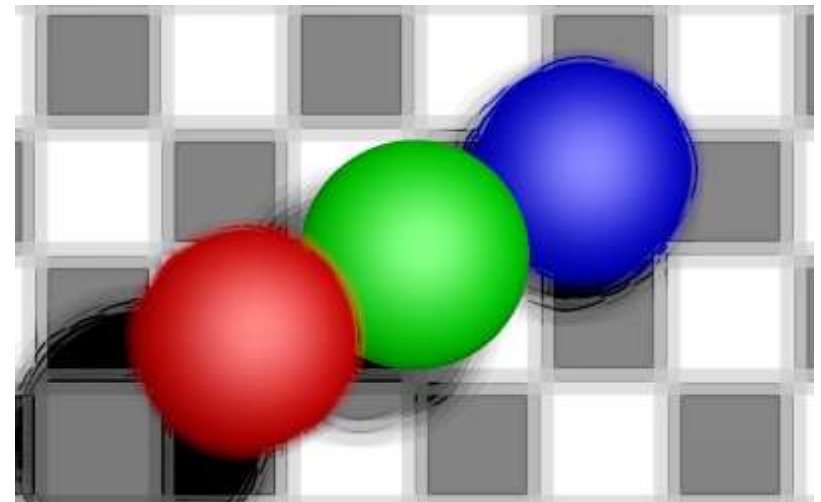
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

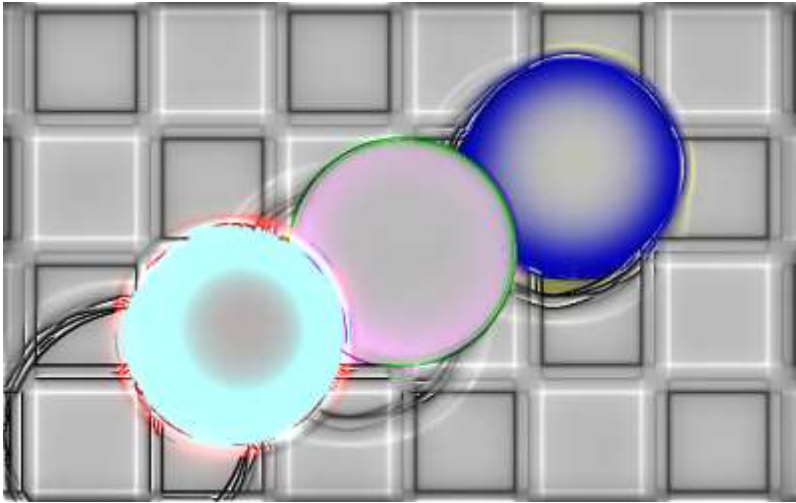
$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$

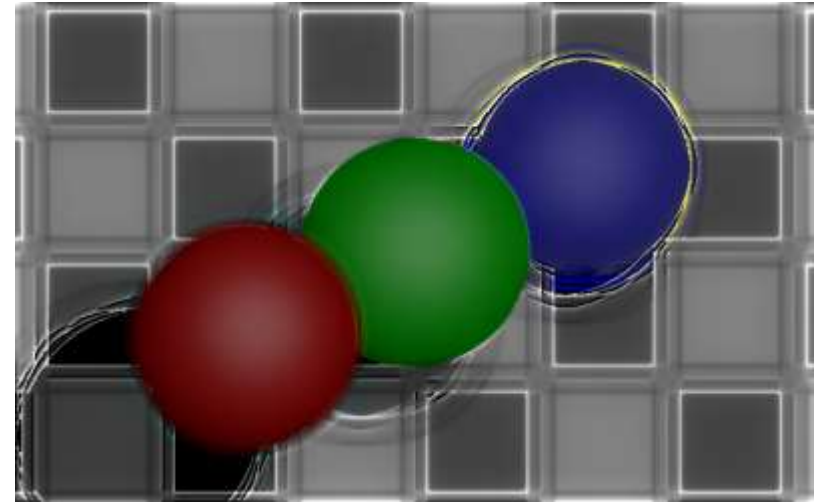


reconstruction (central view)

# Optimization: Iteration 20



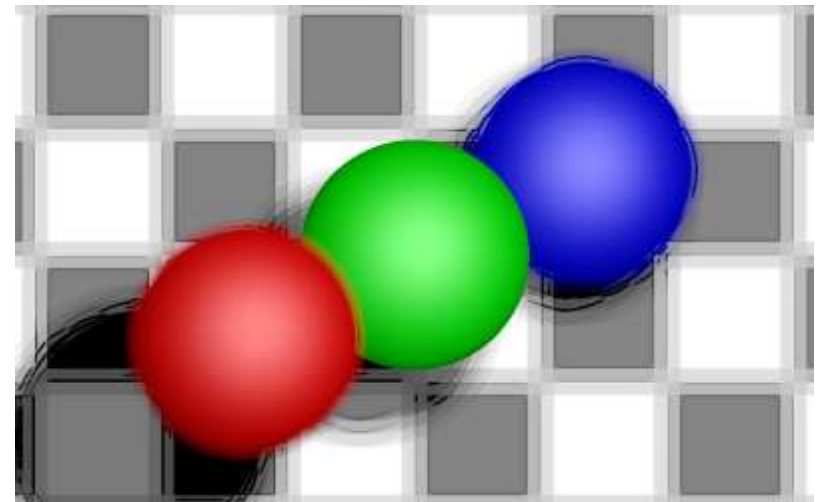
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

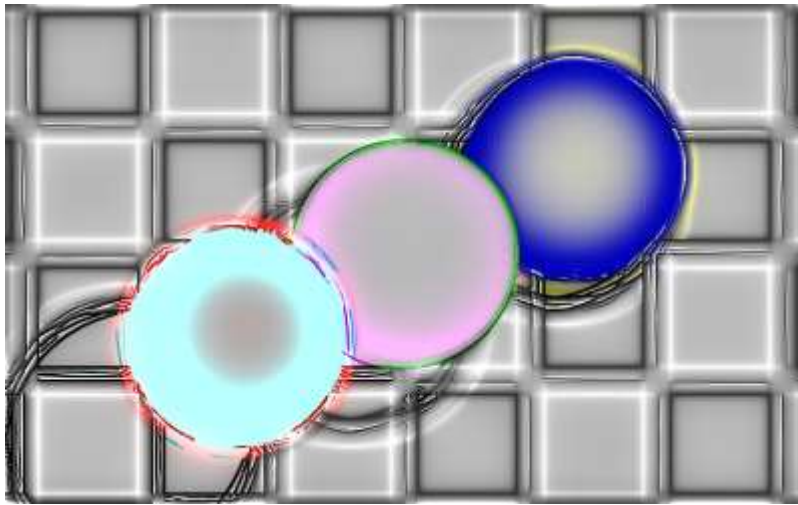
$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$

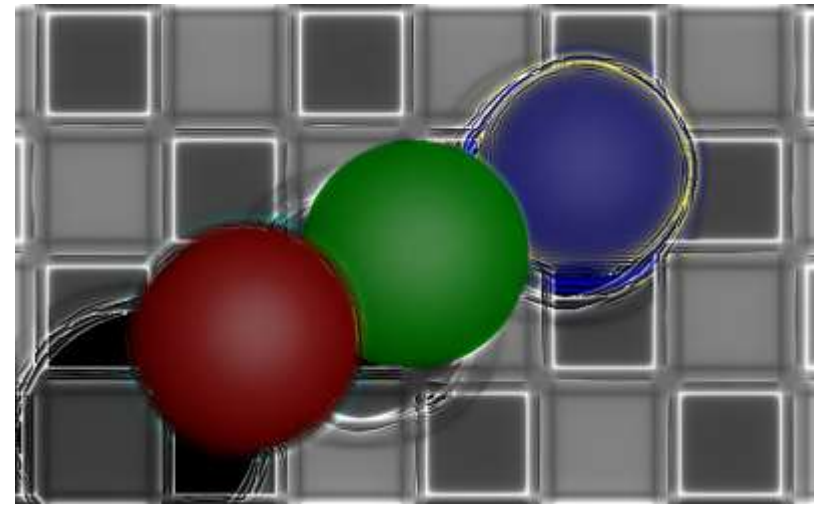


reconstruction (central view)

# Optimization: Iteration 30



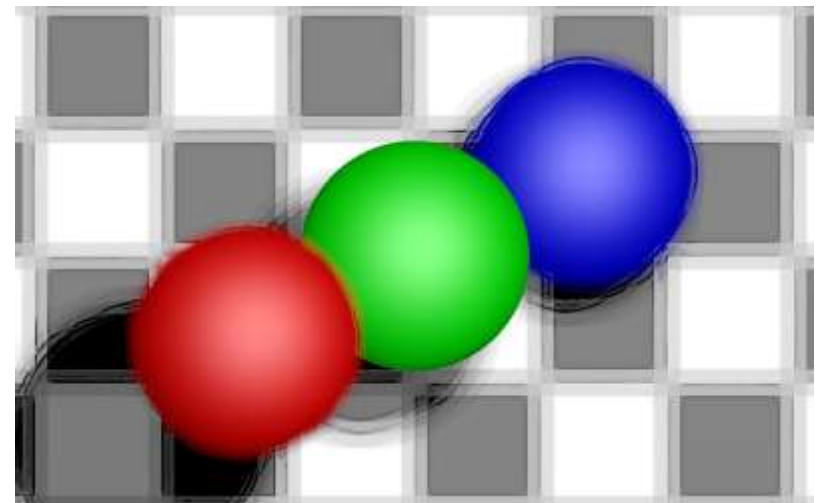
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

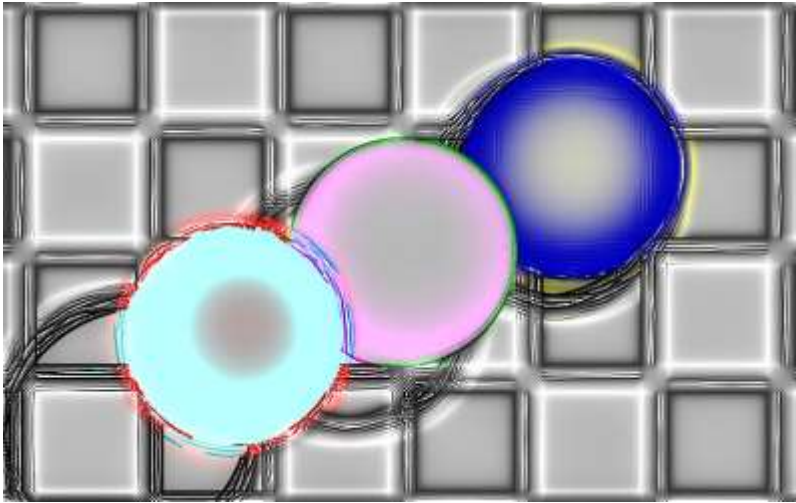
$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$

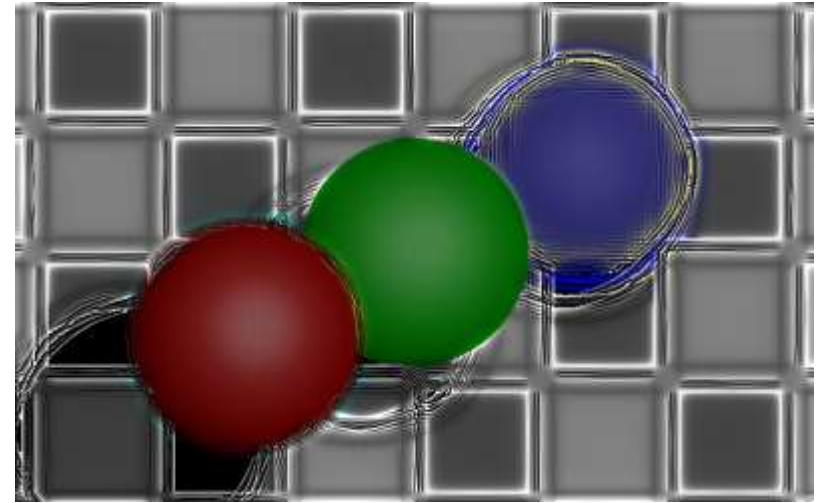


reconstruction (central view)

# Optimization: Iteration 40



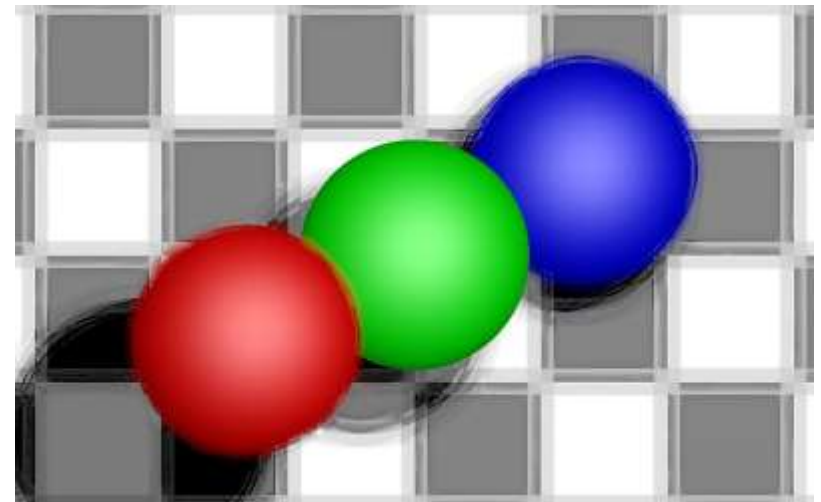
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

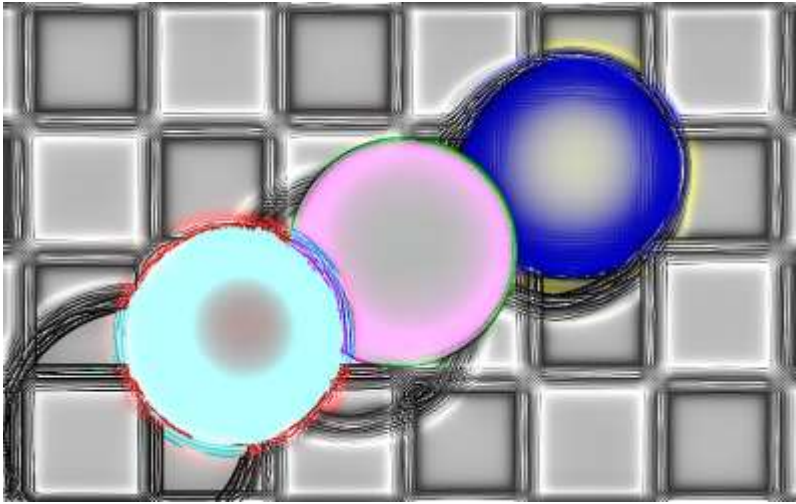
$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$



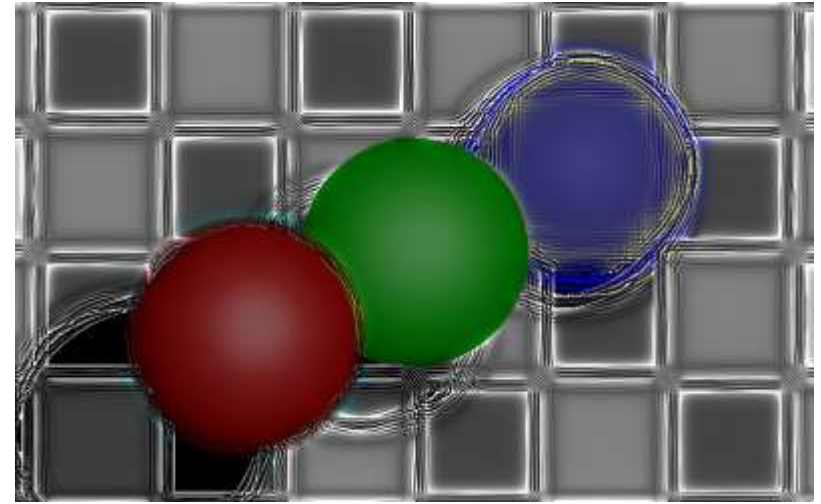
reconstruction (central view)



# Optimization: Iteration 50



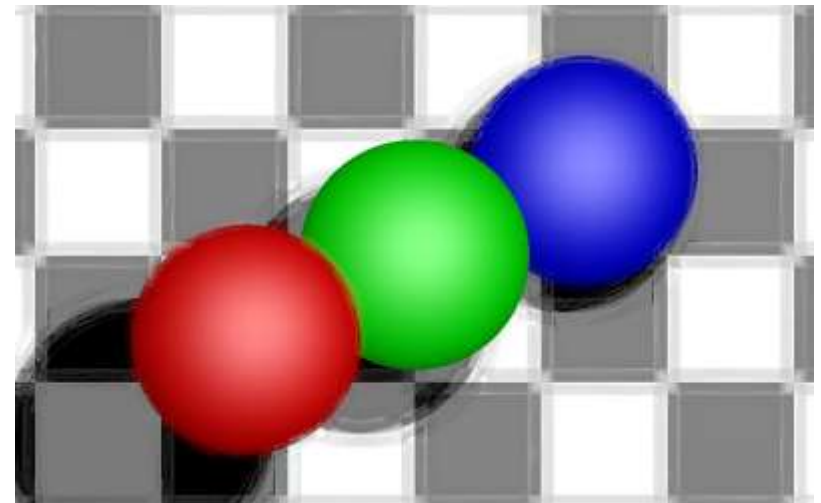
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

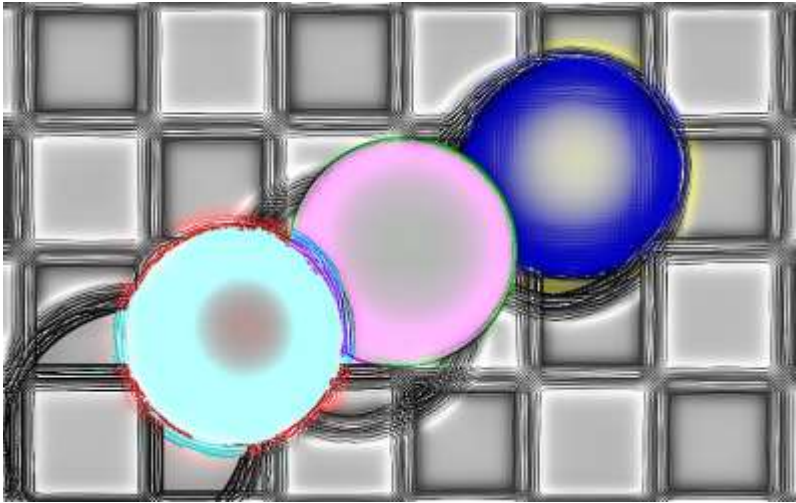
$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$

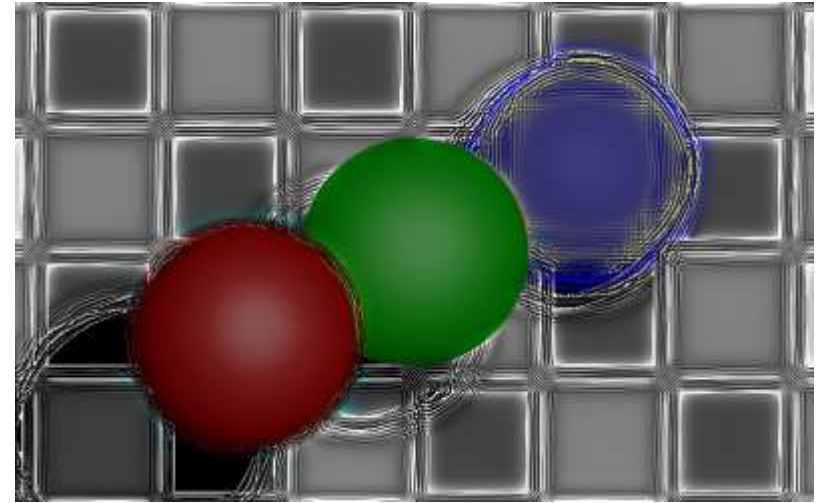


reconstruction (central view)

# Optimization: Iteration 60



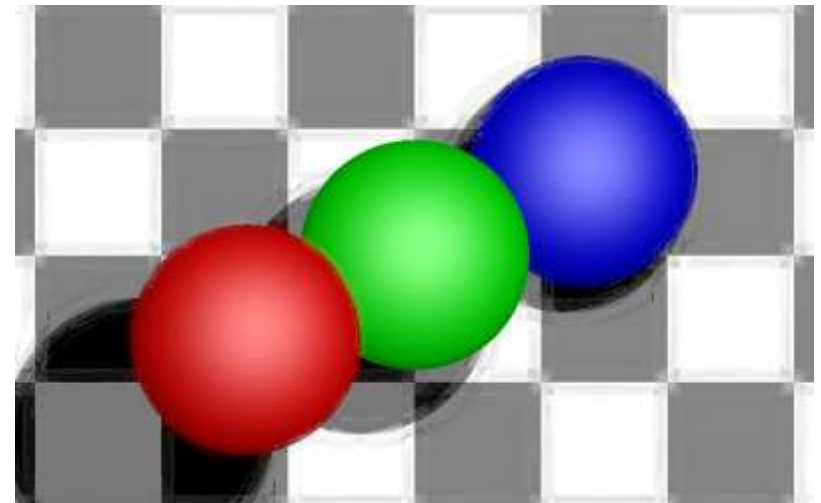
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

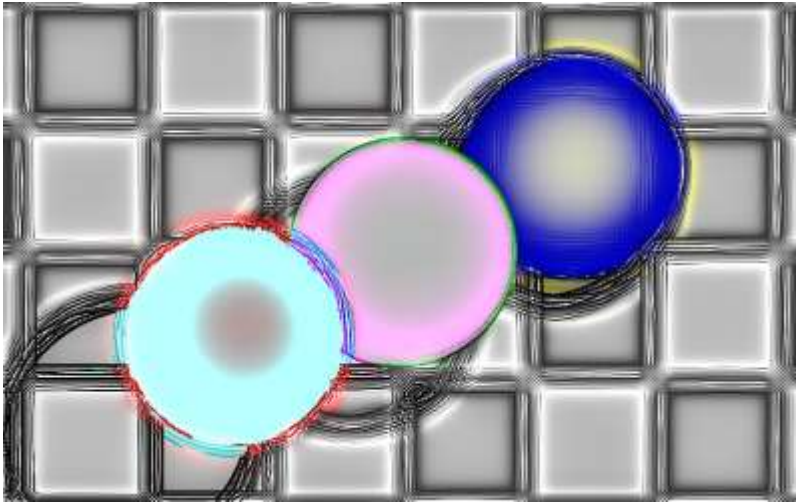
$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$



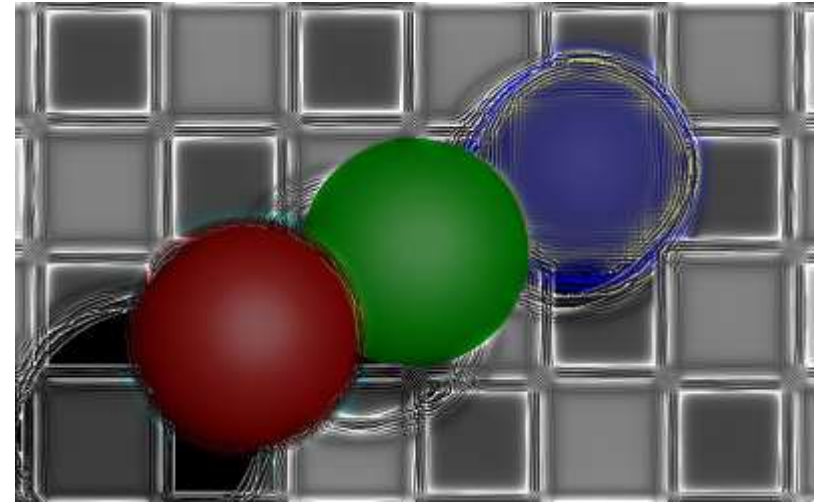
reconstruction (central view)



# Optimization: Iteration 70



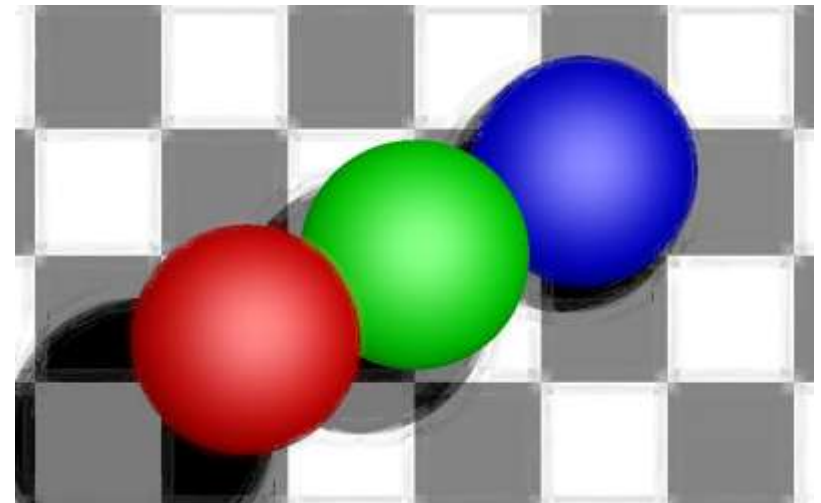
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

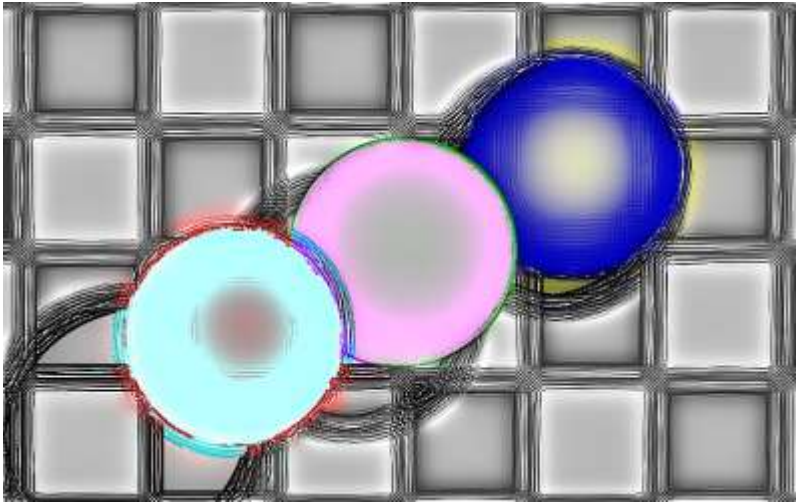
$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$

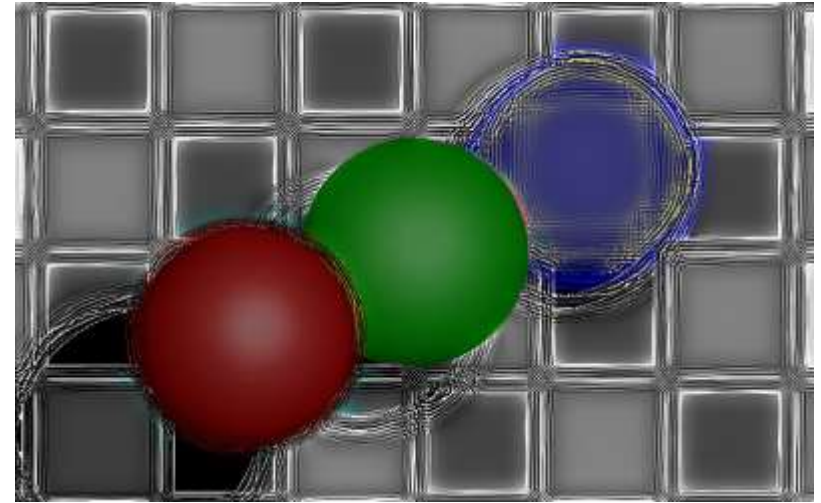


reconstruction (central view)

# Optimization: Iteration 80



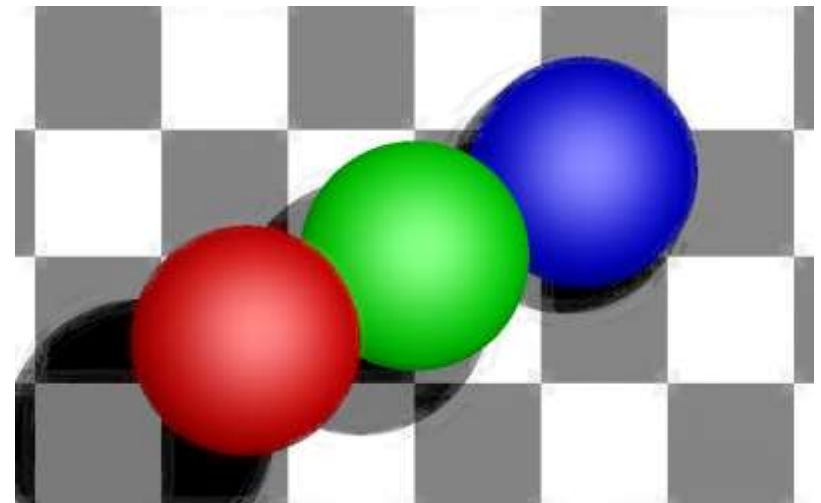
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

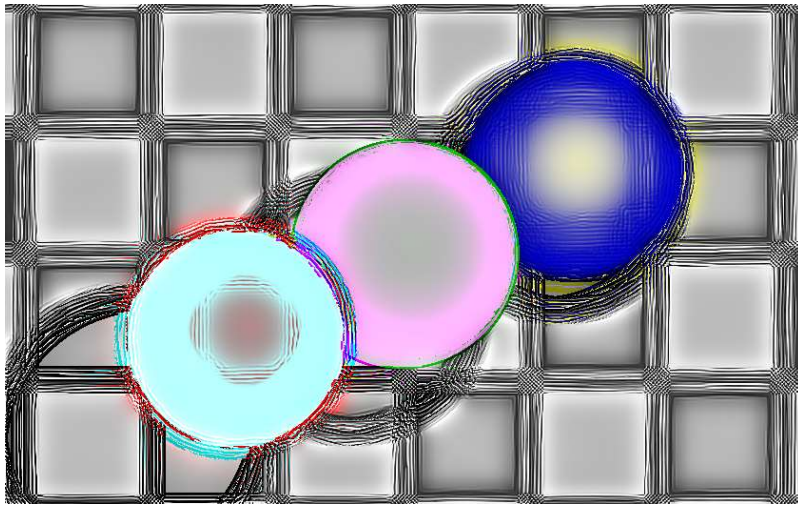
$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$

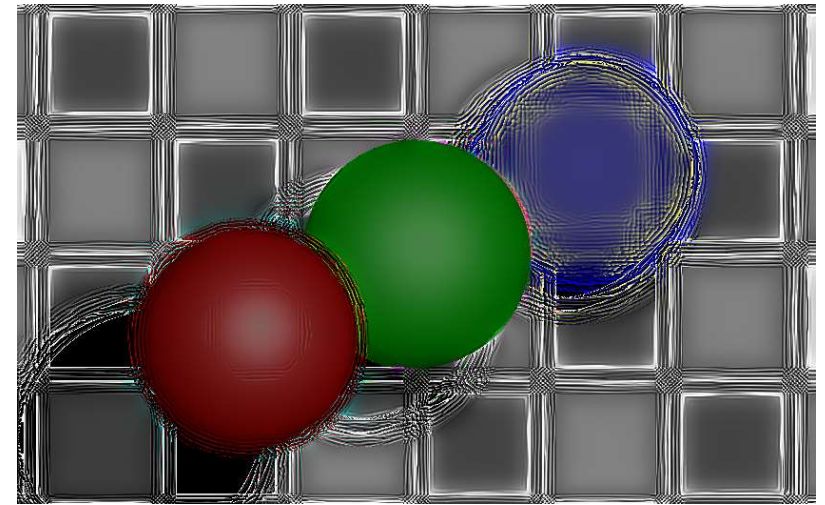


reconstruction (central view)

# Optimization: Iteration 90



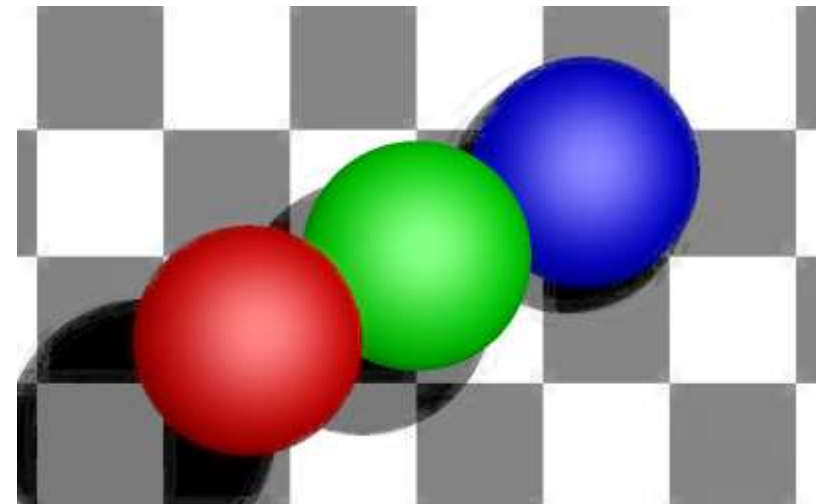
rear mask:  $f_1[i,j]$



front mask:  $g_1[k,l]$

$$F \leftarrow F \circ \frac{[(W \circ L)G^t]}{[(W \circ (FG))G^t]}$$

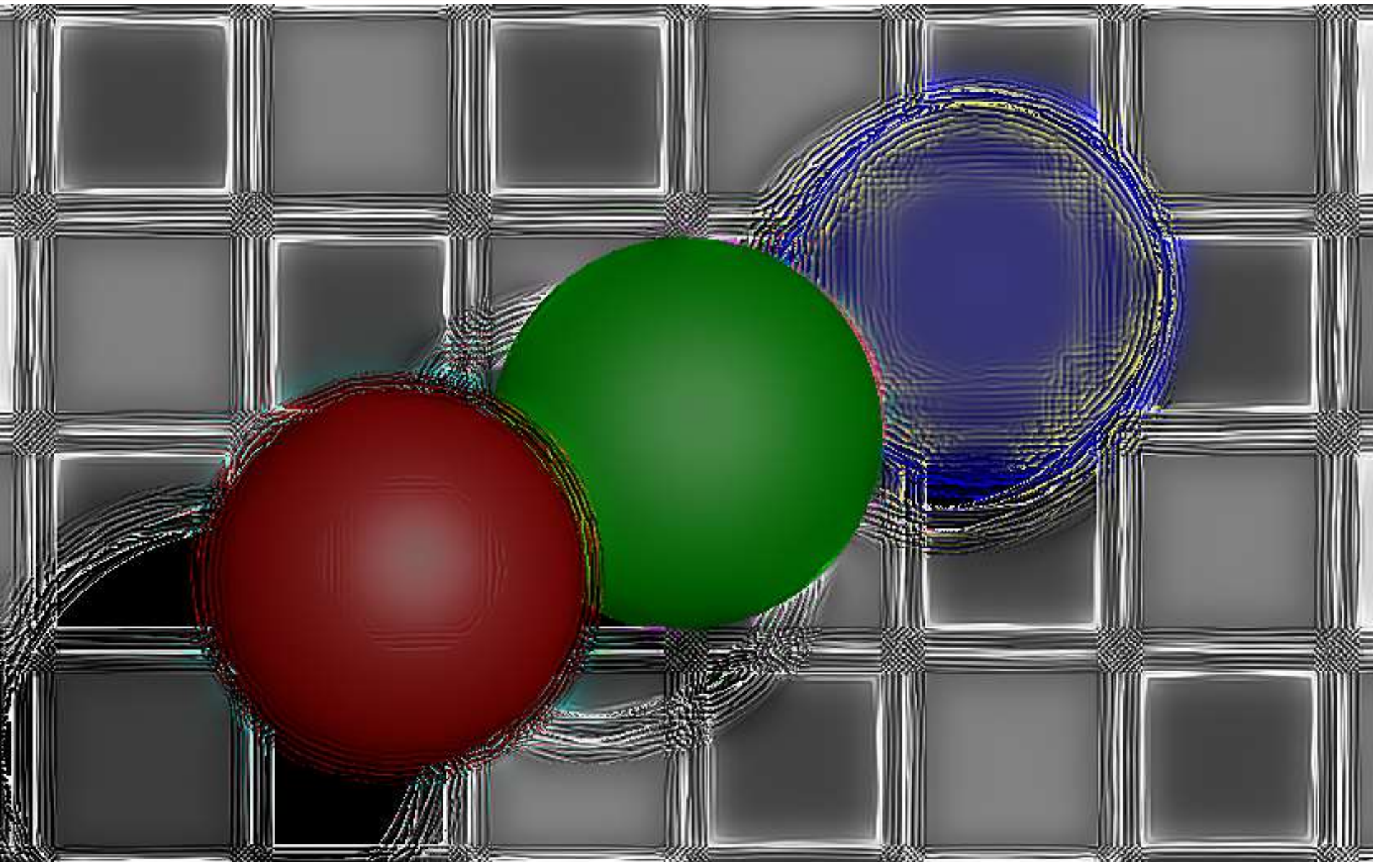
$$G \leftarrow G \circ \frac{[F^t(W \circ L)]}{[F^t(W \circ (FG))]}$$



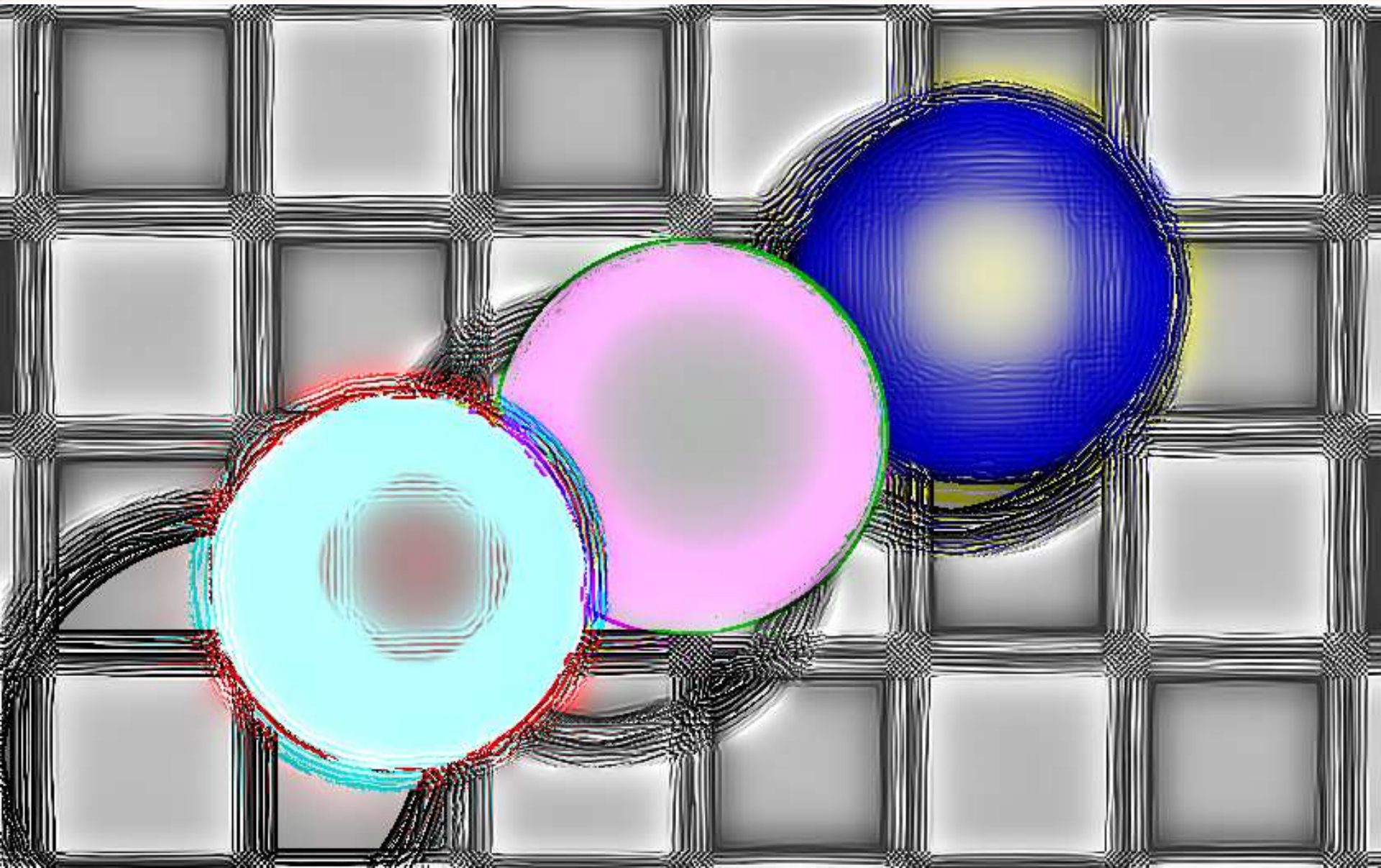
reconstruction (central view)



# Content-Adaptive Front Mask (1 of 9)

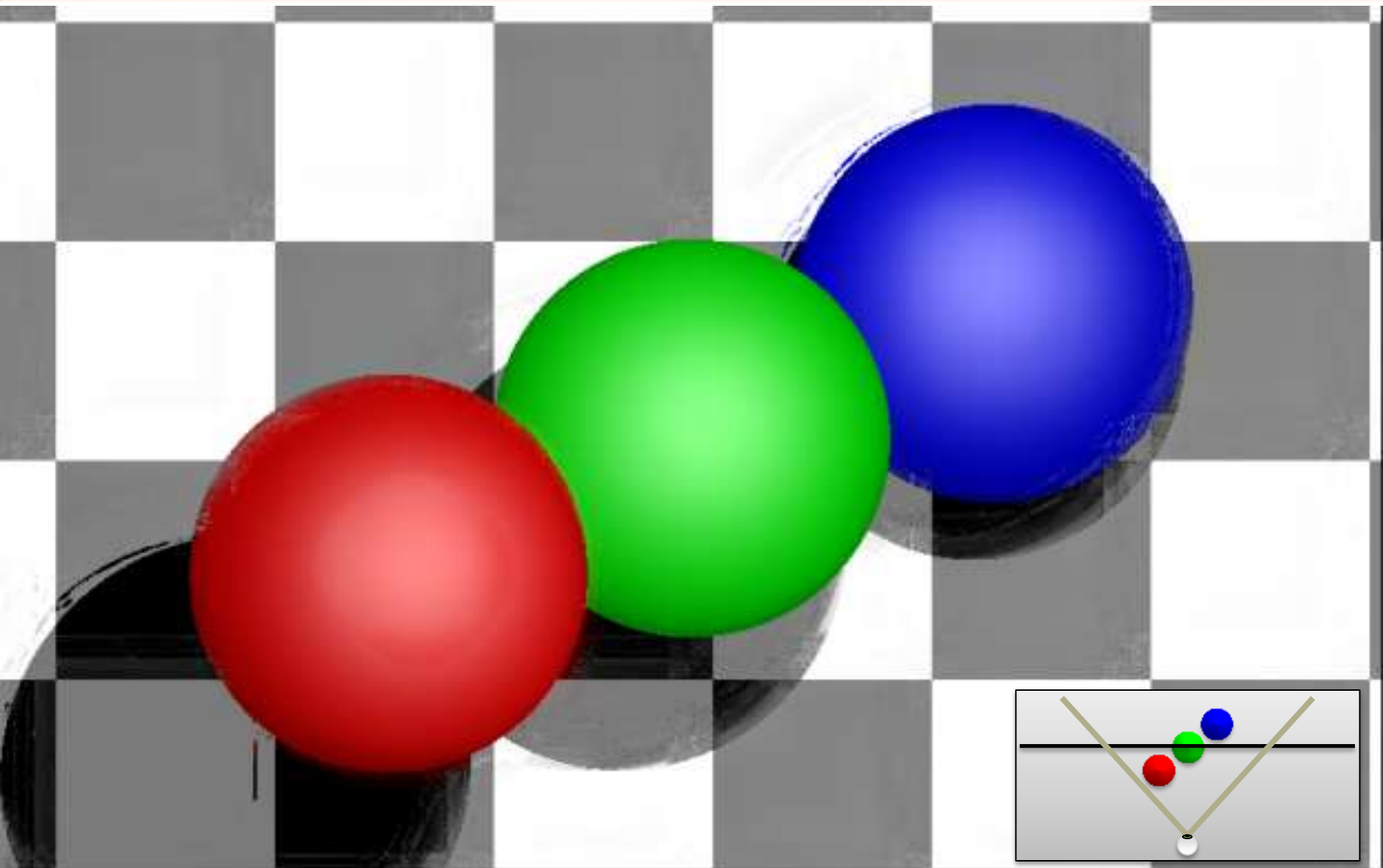


# Content-Adaptive Rear Mask (1 of 9)



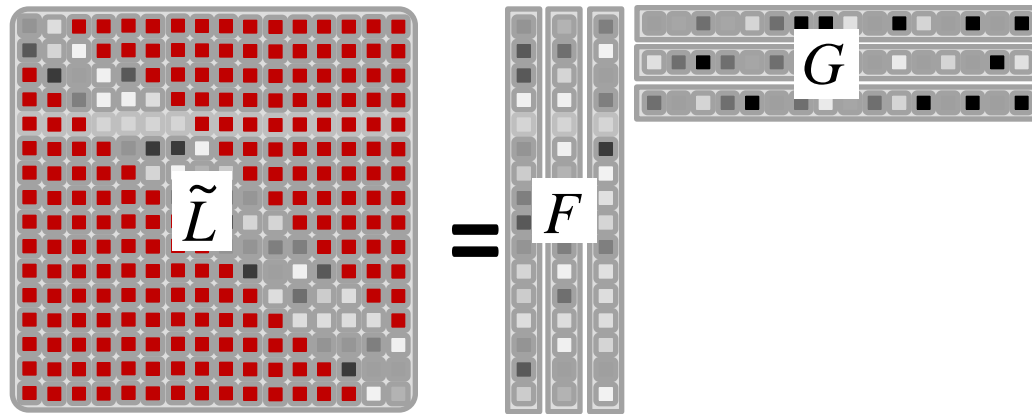


# Emitted 4D Light Field

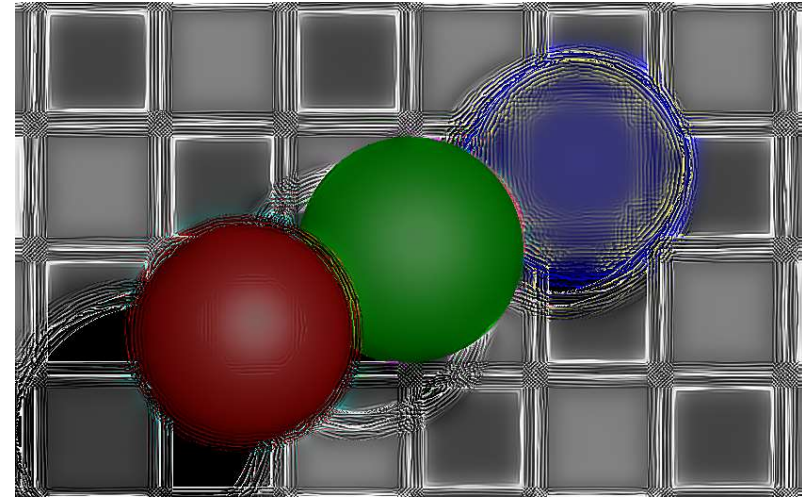




# Conclusion



$$\arg \min_{F, G} \frac{1}{2} \|L - FG\|_w^2, \text{ for } F, G \geq 0$$

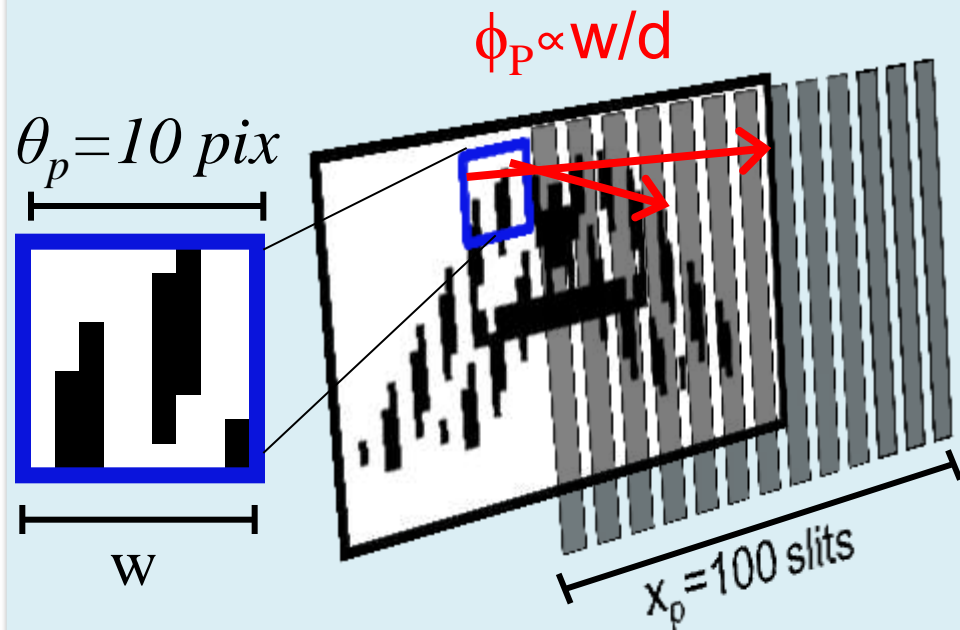


**Content-Adaptive Parallax Barriers**

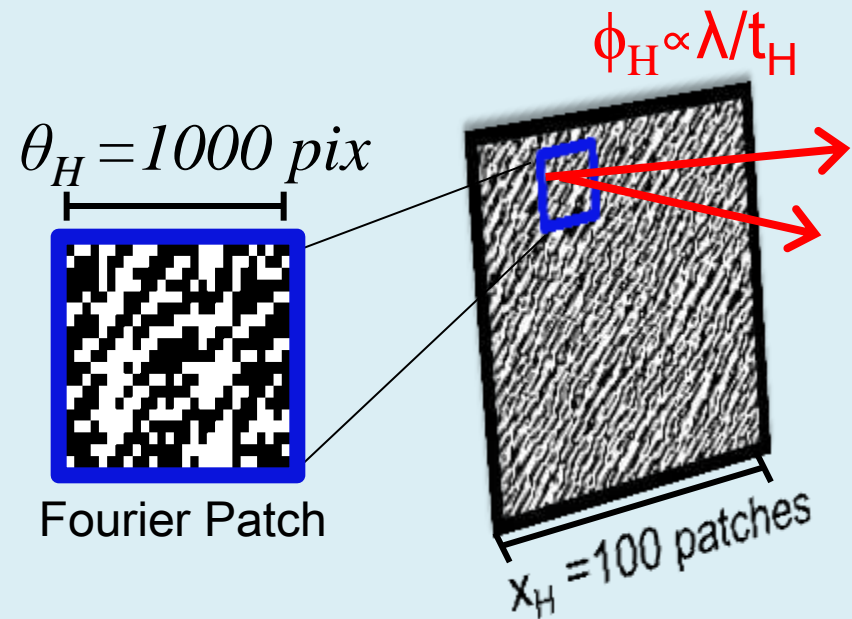
- Described a *rank constraint* for all dual-layer displays
  - With a fixed pair of masks, emitted light field is rank-1
- Achieved higher-rank approximation using temporal multiplexing
  - With  $T$  time-multiplexed masks, emitted light field is rank- $T$
  - Constructed a prototype using off-the-shelf panels
- Demonstrated light field display is a *matrix approximation problem*
- Introduced *content-adaptive parallax barriers*
  - Applied weighted NMF to optimize weighted Euclidean distance to target

***Adaptation increases brightness and refresh rate of dual-stacked LCDs***

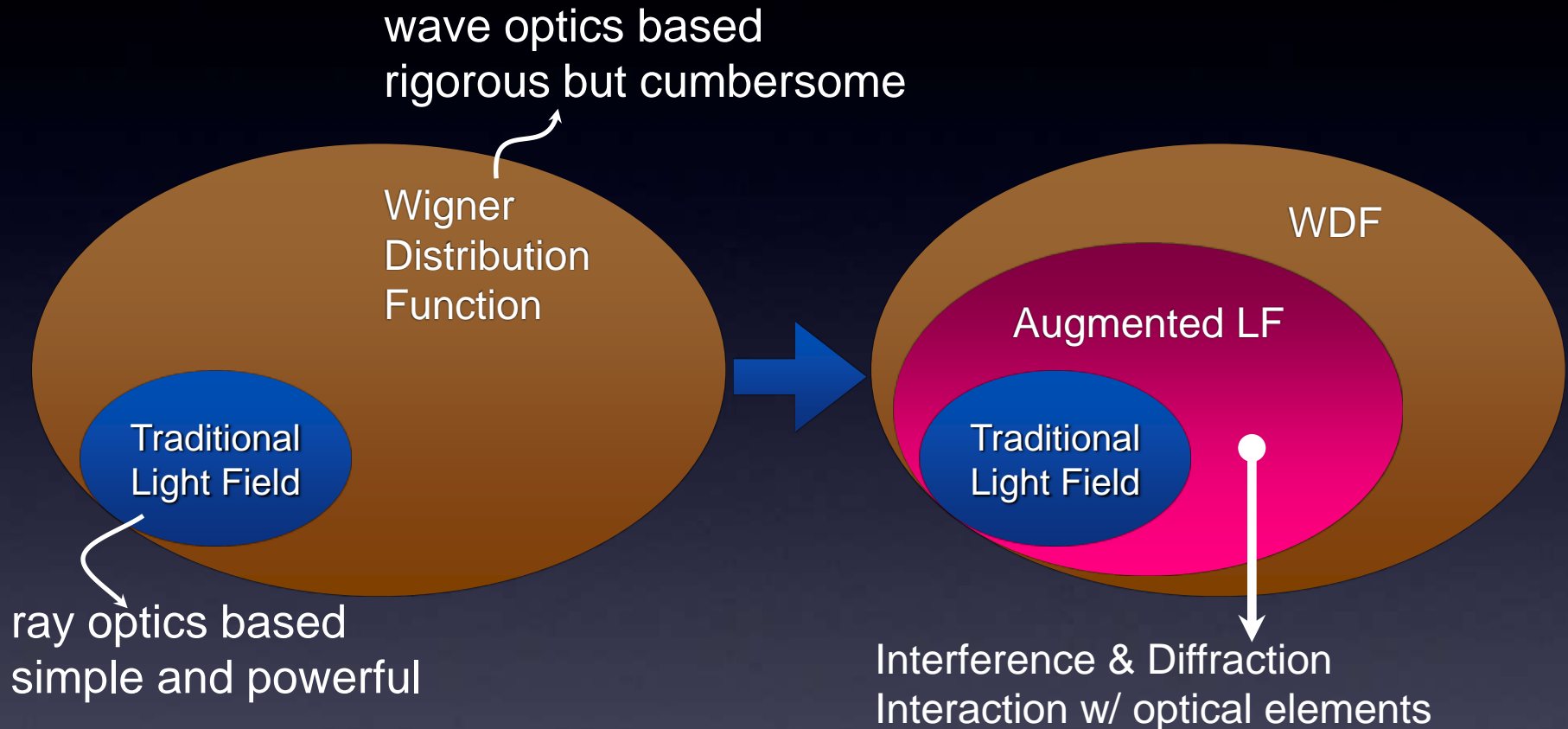
Parallax Barrier:  $N_p = 10^3$  pix.



Hologram:  $N_H = 10^5$  pix.



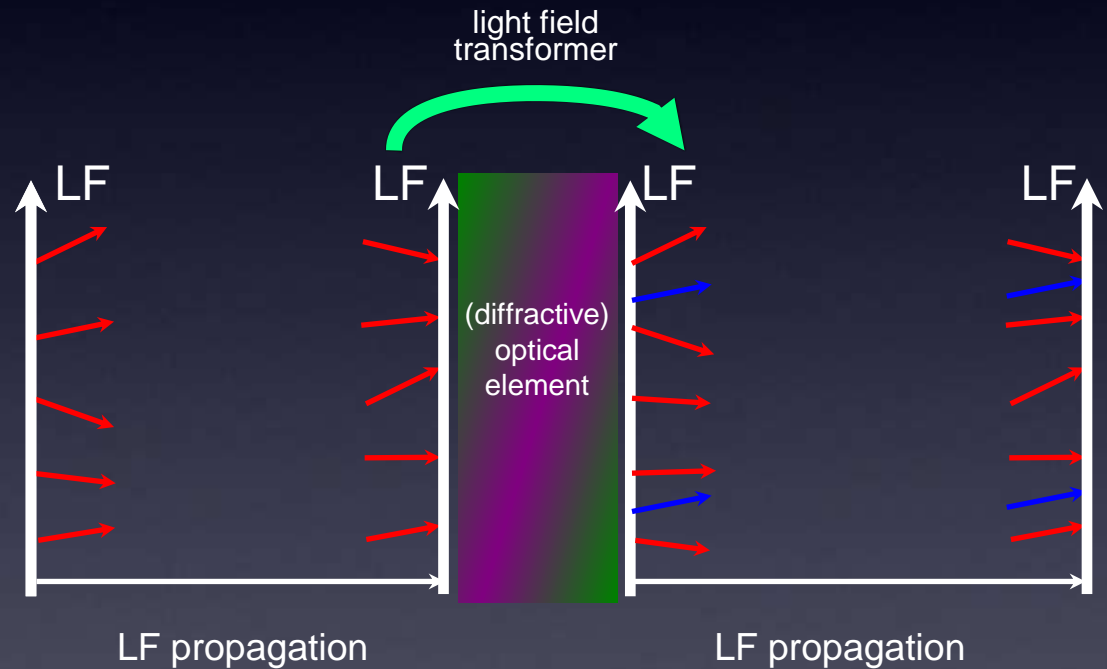
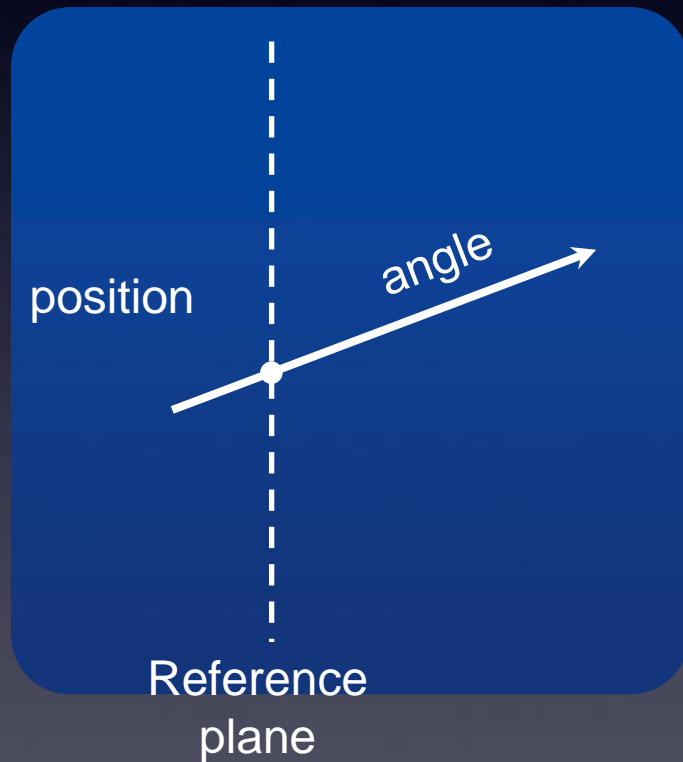
# Augmented Light Field



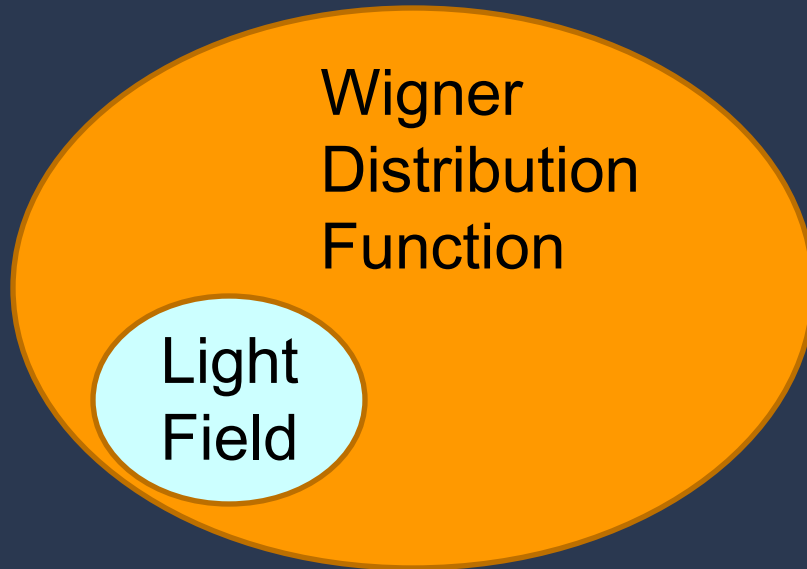
Oh, Raskar, Barbastathis 2009: Augmented Light Field

# Light Fields

Goal: Representing propagation, interaction and image formation of light using purely position and angle parameters



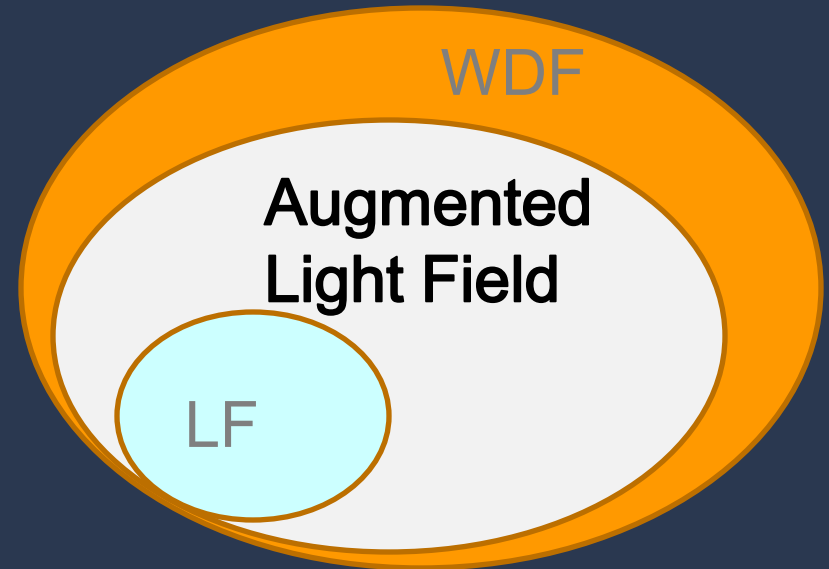
# Augmented Lightfield for Wave Optics Effects



$$LF < WDF$$

Lacks phase properties  
Ignores diffraction, interference

Radiance = Positive



$$ALF \sim WDF$$

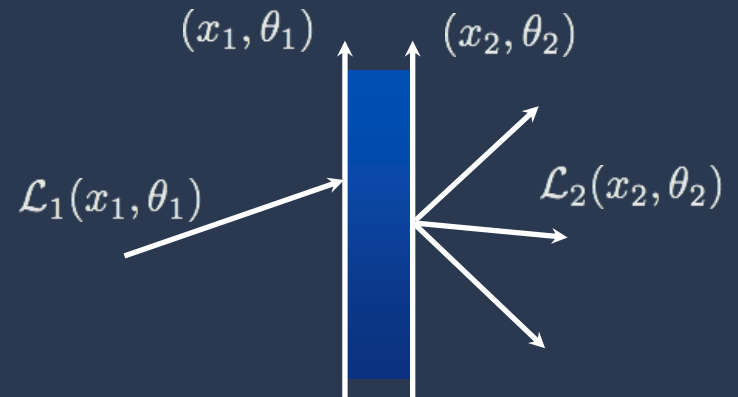
Supports coherent/incoherent

Radiance = Positive/Negative

Virtual light sources

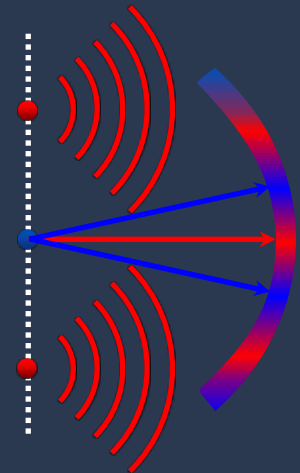
Free-space propagation

Light field transformer



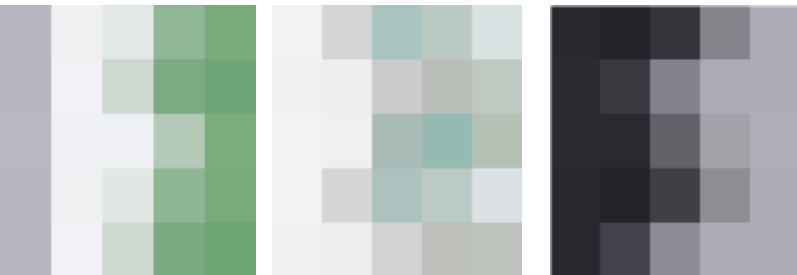
Virtual light projector

Possibly negative radiance





# Lightfield vs Hologram Displays



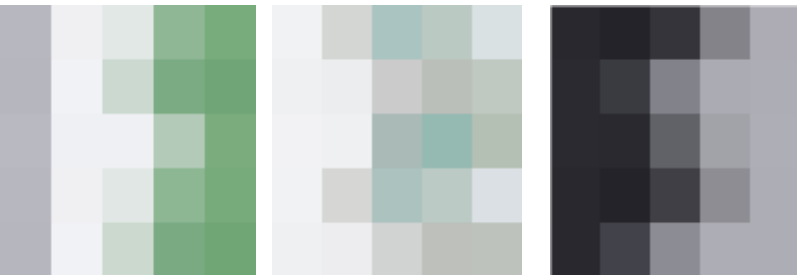
Is hologram just another ray-based light field?

Can a hologram create any intensity distribution in 3D?

Why hologram creates a 'wavefront' but PB does not?

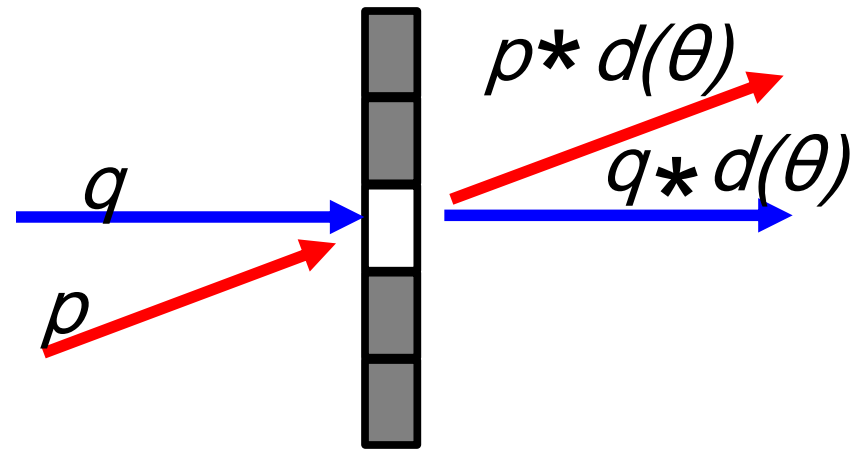
Why hologram creates automatic accommodation cues?

What is the effective resolution of HG vs PB?

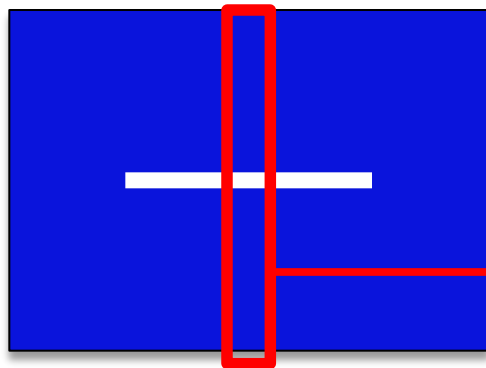


# Zooming into the Light Field

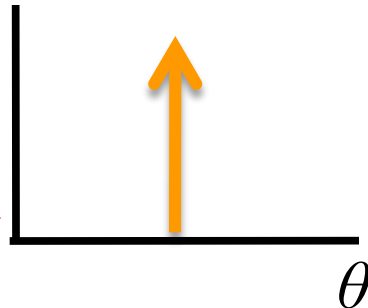
Rays: No Bending



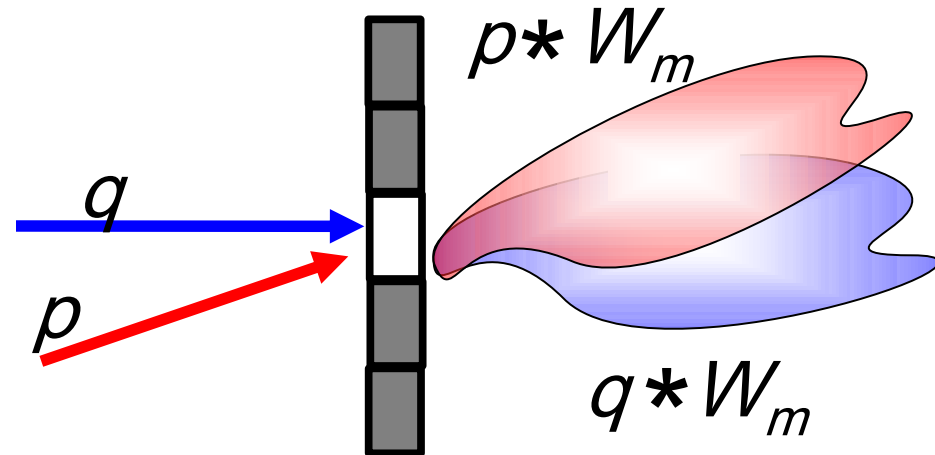
$L(x, \theta)$



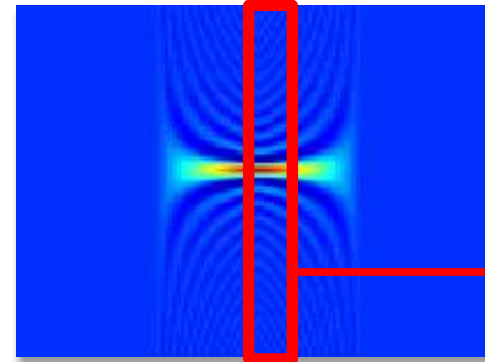
$d = \text{delta}$



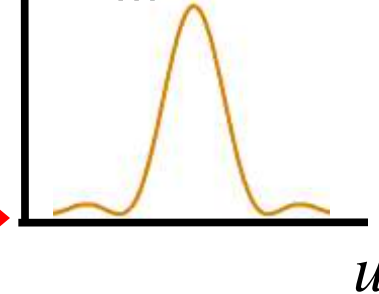
1 Fresnel HG Patch



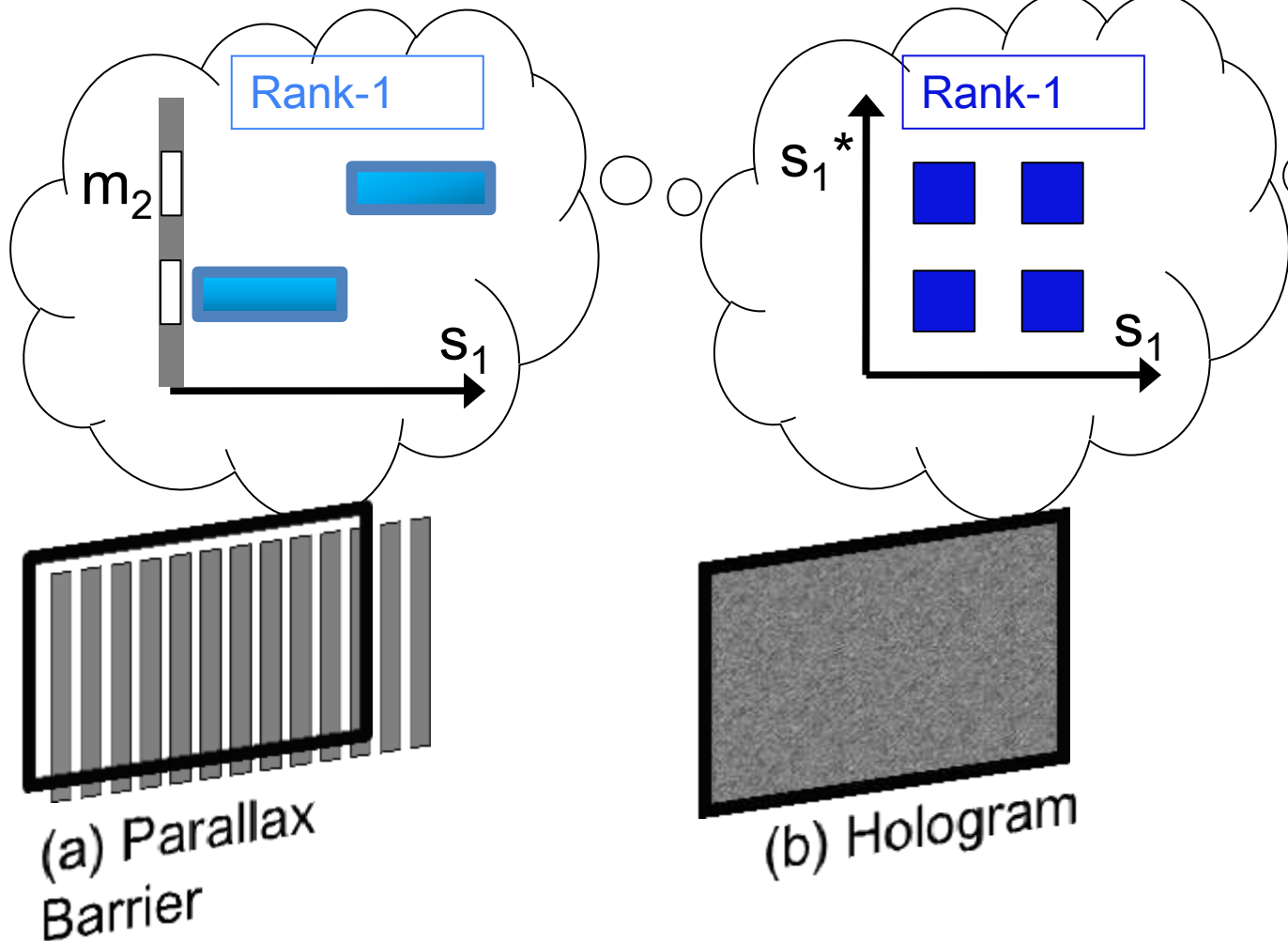
$W(x, u)$



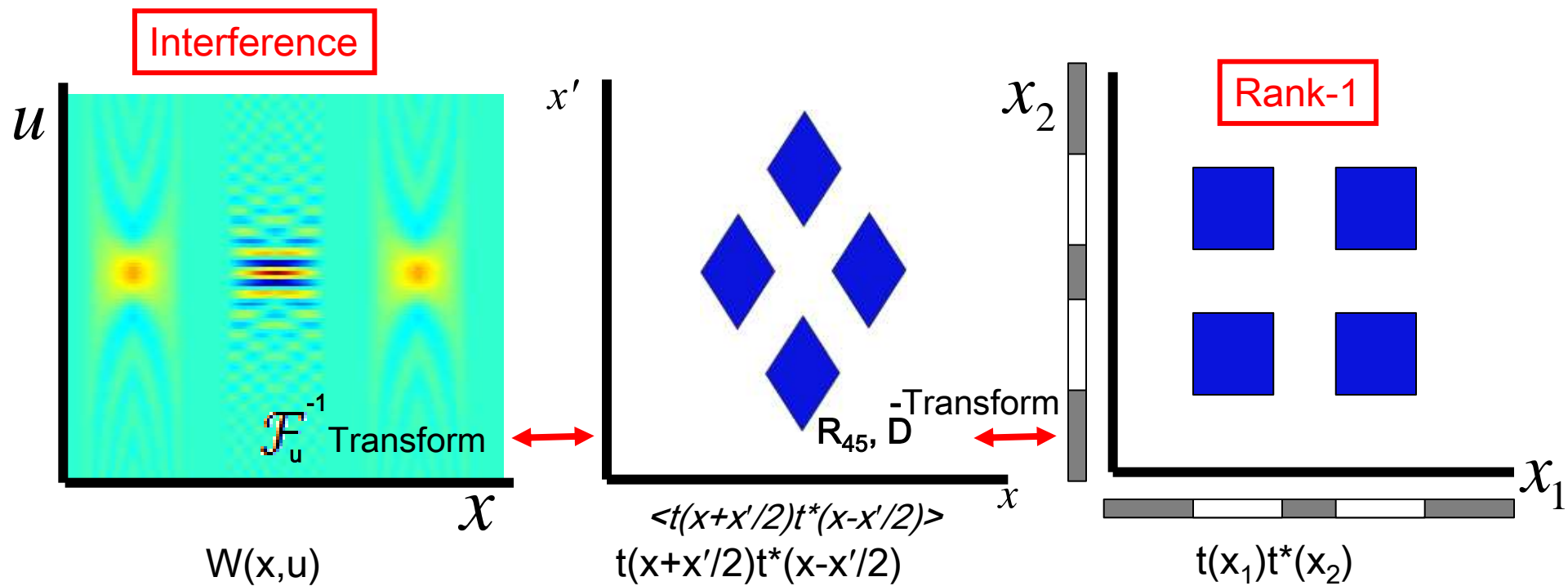
$W_m = \text{sinc}$

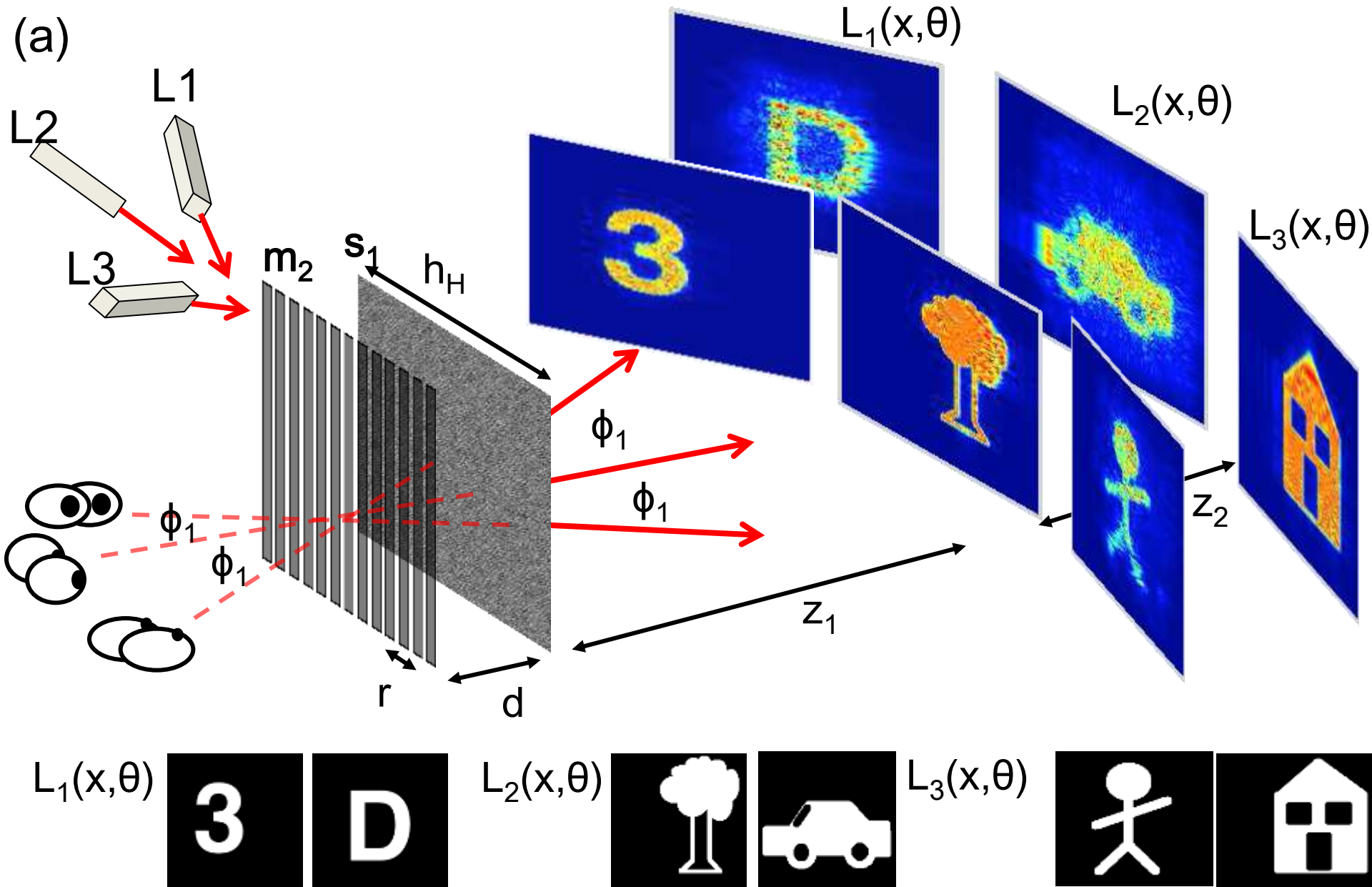


# Algebraic Rank Constraint



(a) Two Slits, Coherent







Is hologram just another ray-based light field?

Can a hologram create any intensity distribution in 3D?

Why hologram creates a 'wavefront' but PB does not?

Why hologram creates automatic accommodation cues?

What is the effective resolution of HG vs PB?



# Inverse Problems

- Co-design of Optics and Computation
  - Photons not just pixels
  - Mid-level cues
- Computational Photography
  - Coded Exposure
  - Compressive Sensing for High Speed Events
    - Limits of CS for general imaging
- Computational Light Transport
  - Looking Around Corners, trillion fps
  - Lightfields:
    - Compressive Campture
    - 3D Displays and Holograms

