

Color

Computational Photography
MIT
Feb. 14, 2006
Bill Freeman and Fredo Durand

Why does a visual system need color?



<http://www.hobbyline.com/gr/poll/p85019.jpg>

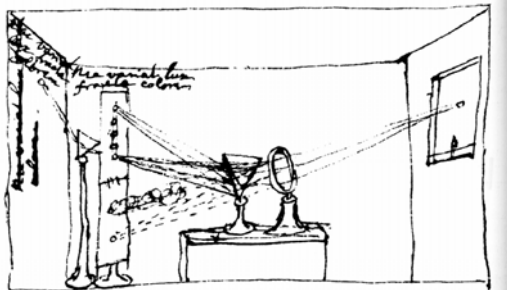
Why does a visual system need color?
(an incomplete list...)

- To tell what food is edible.
- To distinguish material changes from shading changes.
- To group parts of one object together in a scene.
- To find people's skin.
- Check whether a person's appearance looks normal/healthy.
- To compress images

Lecture outline

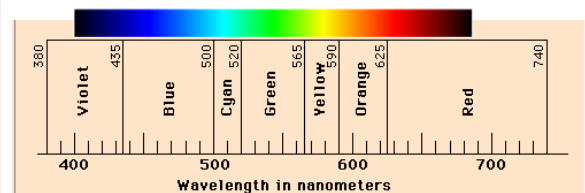
- Color physics.
- Color representation and matching.

Color

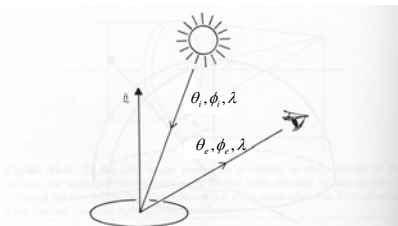


4.1 NEWTON'S SUMMARY DRAWING of his experiments with light. Using a point source of light and a prism, Newton separated sunlight into its fundamental components. By reconverging the rays, he also showed that the decomposition is reversible.
From Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Spectral colors



<http://hyperphysics.phy-astr.gsu.edu/hbase/vision/specol.html#c2>



Radiometry for color


Horn, 1986
Figure 10-7. The bidirectional reflectance distribution function is the ratio of the radiance of the surface patch as viewed from the direction (θ_e, ϕ_e) to the irradiance resulting from illumination from the direction (θ_i, ϕ_i) .

Spectral radiance: power in a specified direction, per unit area, per unit solid angle, per unit wavelength

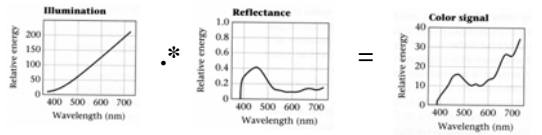
$$BRDF = f(\theta_i, \phi_i, \theta_e, \phi_e, \lambda) = \frac{L(\theta_e, \phi_e, \lambda)}{E(\theta_i, \phi_i, \lambda)}$$

Spectral irradiance: incident power per unit area, per unit wavelength

Simplified rendering models: reflectance


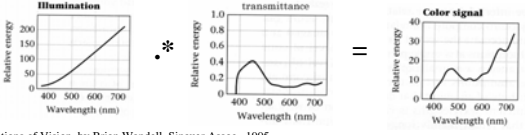


Often are more interested in relative spectral composition than in overall intensity, so the spectral BRDF computation simplifies a wavelength-by-wavelength multiplication of relative energies.



Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

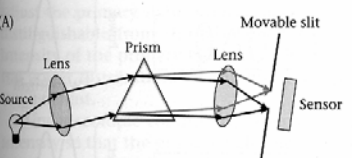
Simplified rendering models: transmittance

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

How measure those spectra: Spectrophotometer

(just like Newton's diagram...)

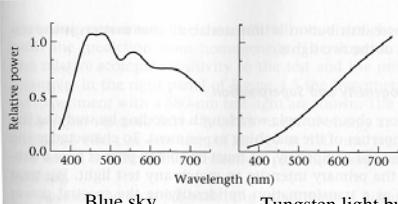


(B) Wavelength (nm)	Color (viewed in isolation)
700	Red
610	Orange
580	Yellow
540	Green
480	Blue
400	Violet

4.2 A SPECTRORADIOMETER is used to measure the spectral power distribution of light. (A) A schematic design of a spectroradiometer includes a means for separating the input light into its different wavelengths and a detector for measuring the energy at each of the separate wavelengths. (B) The color names associated with the appearance of lights at a variety of wavelengths are shown. After Wyszecki and Stiles, 1982.

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

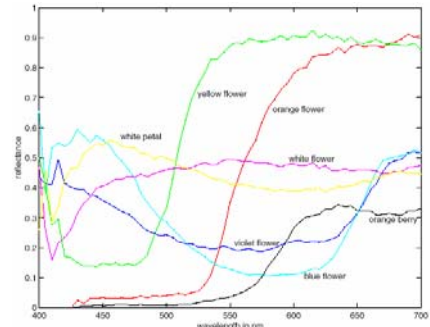
Two illumination spectra



4.4 THE SPECTRAL POWER DISTRIBUTION of two important light sources are shown: (left) blue skylight and (right) a tungsten bulb.

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Some reflectance spectra

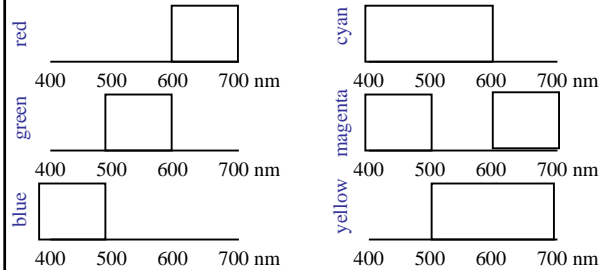
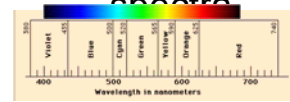


Spectral albedoes for several different leaves, with color names attached. Notice that different colours typically have different spectral albedo, but that different spectral albedoes may result in the same perceived color (compare the two whites). Spectral albedoes are typically quite smooth functions. Measurements by E. Koivisto.

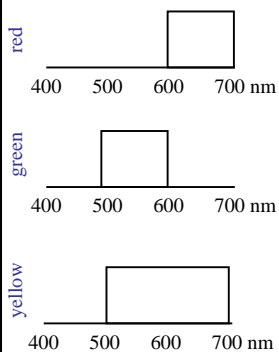
Forryth, 2002

Questions?

Color names for cartoon spectra



Additive color mixing

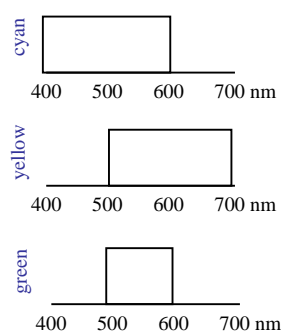


When colors combine by *adding* the color spectra. Example color displays that follow this mixing rule: CRT phosphors, multiple projectors aimed at a screen, Polachrome slide film.

Red and green make...

Yellow!

Subtractive color mixing



When colors combine by *multiplying* the color spectra. Examples that follow this mixing rule: most photographic films, paint, cascaded optical filters, crayons.

Cyan and yellow (in crayons, called "blue" and yellow) make...

Green!

Overhead projector demo

- Subtractive color mixing

Crayons

Questions?

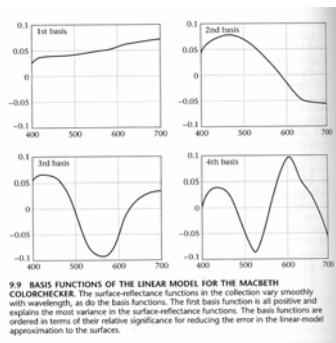
Low-dimensional models for color spectra

$$\begin{pmatrix} \vdots \\ e(\lambda) \\ \vdots \end{pmatrix} = \begin{pmatrix} \vdots & \vdots & \vdots \\ E_1(\lambda) & E_2(\lambda) & E_3(\lambda) \\ \vdots & \vdots & \vdots \end{pmatrix} \begin{pmatrix} \omega_1 \\ \omega_2 \\ \omega_3 \end{pmatrix}$$

How to find a linear model for color spectra:

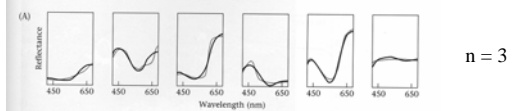
- form a matrix, D, of measured spectra, 1 spectrum per column.
- [u, s, v] = svd(D) satisfies $D = u * s * v'$
- the first n columns of u give the best (least-squares optimal) n-dimensional linear bases for the data, D:
 $D \approx u(:, 1:n) * s(1:n, 1:n) * v(1:n, :)'$

Basis functions for Macbeth color checker



Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

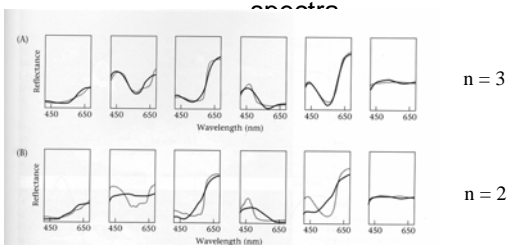
n-dimensional linear models for color spectra



9.8 A LINEAR MODEL TO APPROXIMATE THE SURFACE REFLECTANCES IN THE MACBETH COLORCHECKER. The panels in each row of this figure show the surface-reflectance functions of six colored surfaces (shaded lines) and the approximation to these functions using a linear model (solid lines). The approximations using linear models with (A) three, (B) two, and (C) one dimension are shown.

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

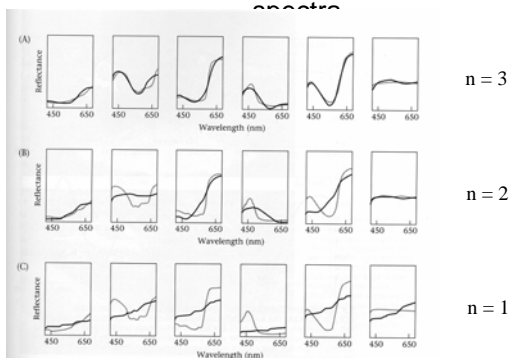
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Outline

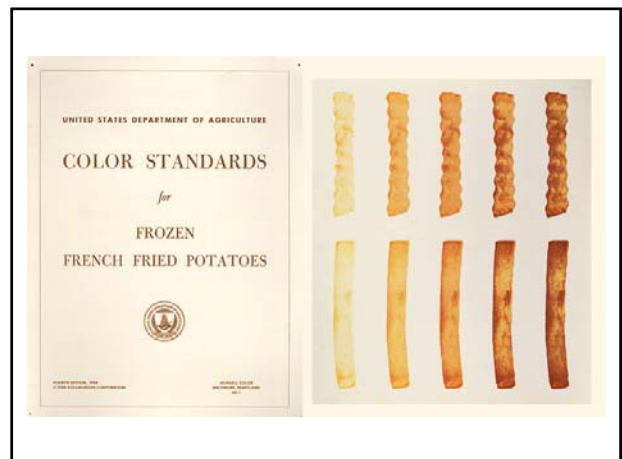
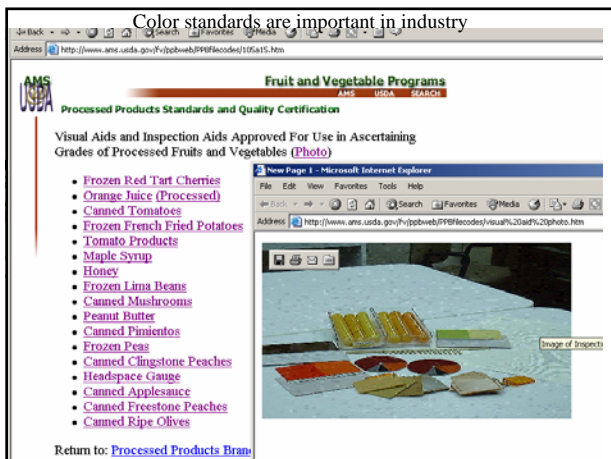
- Color physics.
- Color representation and matching.

Why specify color numerically?

- Accurate color reproduction is commercially valuable
 - Many products are identified by color ("golden" arches);
- Color reproduction problems increased by prevalence of digital imaging - eg. digital libraries of art.
 - How do we ensure that everyone sees the same color?
- Few color names are widely recognized by English speakers -
 - About 10; other languages have fewer/more, but not many more.
 - It's common to disagree on appropriate color names.

Forsyth & Ponce

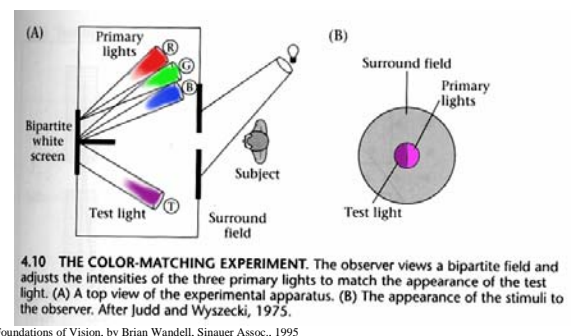
Color standards are important in industry



An assumption that sneaks in here

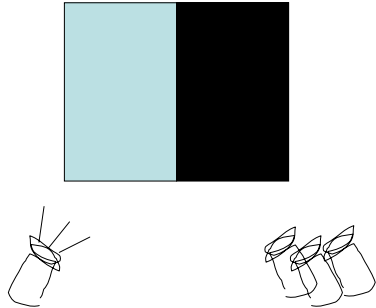
- For now we will assume that the spectrum of the light arriving at your eye completely determines the perceived color.
- But we know color appearance really depends on:
 - The illumination
 - Your eye's adaptation level
 - The colors and scene interpretation surrounding the observed color.

Color matching experiment

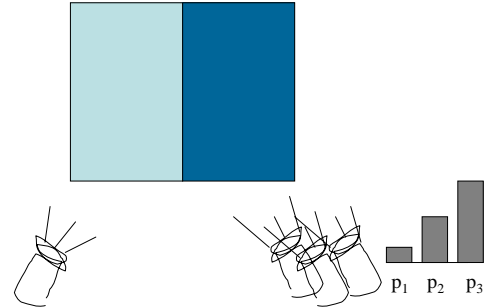


Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

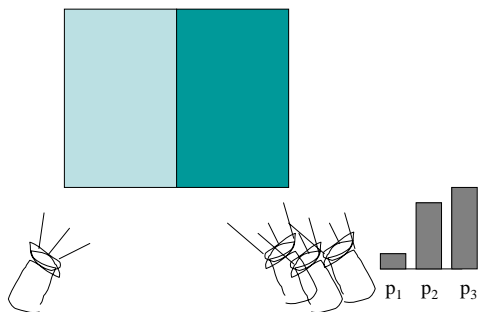
Color matching experiment 1



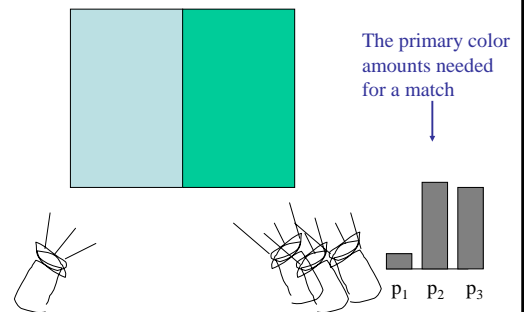
Color matching experiment 1



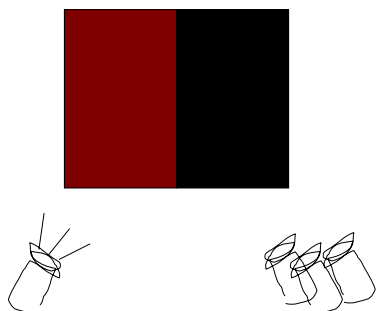
Color matching experiment 1



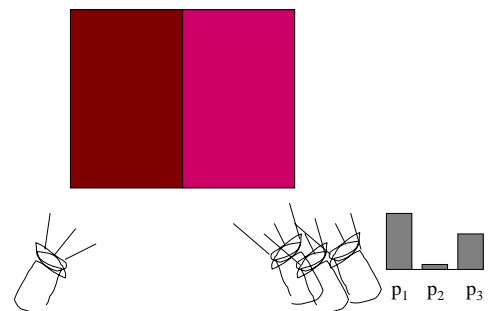
Color matching experiment 1



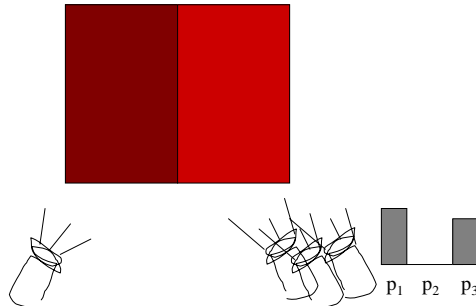
Color matching experiment 2



Color matching experiment 2



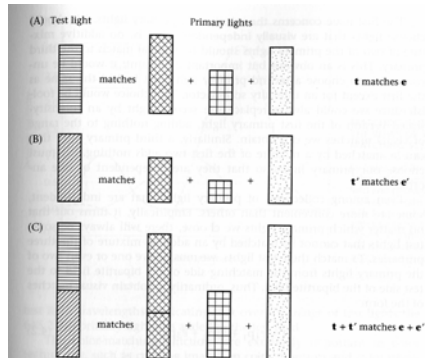
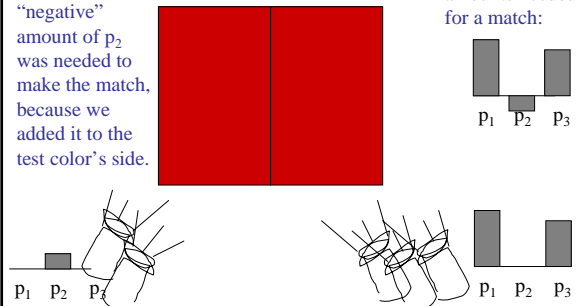
Color matching experiment 2



Color matching experiment 2

We say a “negative” amount of p_2 was needed to make the match, because we added it to the test color’s side.

The primary color amounts needed for a match:



4.12 THE COLOR-MATCHING EXPERIMENT SATISFIES THE PRINCIPLE OF SUPERPOSITION. In parts (A) and (B), test lights are matched by a mixture of three primary lights. In part (C) the sum of the test lights is matched by the additive mixture of the primaries, demonstrating superposition.

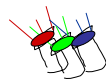
Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Grassman's Laws

- For color matches:
 - symmetry: $U=V \Leftrightarrow V=U$
 - transitivity: $U=V$ and $V=W \Rightarrow U=W$
 - proportionality: $U=V \Leftrightarrow tU=tV$
 - additivity: if any two (or more) of the statements $U=V$, $W=X$, $(U+W)=(V+X)$ are true, then so is the third
- These statements are as true as any biological law. They mean that additive color matching is linear.

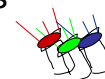
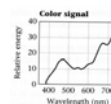
Forsyth & Ponce

Measure color by color-matching paradigm



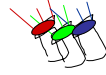
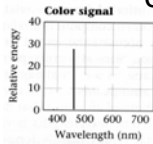
- Pick a set of 3 primary color lights.
- Find the amounts of each primary, e_1 , e_2 , e_3 , needed to match some spectral signal, t .
- Those amounts, e_1 , e_2 , e_3 , describe the color of t . If you have some other spectral signal, s , and s matches t perceptually, then e_1 , e_2 , e_3 will also match s , by Grassman's laws.
- Why this is useful—it lets us:
 - Predict the color of a new spectral signal
 - Translate to representations using other primary lights.

Goal: compute the color match for any color signal for any set of primary colors



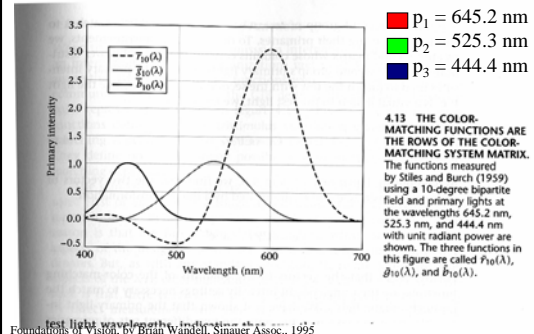
- Examples of why you'd want to do that:
 - Want to paint a carton of Kodak film with the Kodak yellow color.
 - Want to match skin color of a person in a photograph printed on an ink jet printer to their true skin color.
 - Want the colors in the world, on a monitor, and in a print format to all look the same.

How to compute the color match for any color signal for any set of primary colors



- Pick a set of primaries, $p_1(\lambda)$, $p_2(\lambda)$, $p_3(\lambda)$
- Measure the amount of each primary, $c_1(\lambda)$, $c_2(\lambda)$, $c_3(\lambda)$ needed to match a monochromatic light, $t(\lambda)$ at each spectral wavelength λ (pick some spectral step size). These are called the color matching functions.

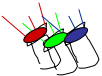
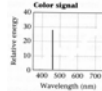
Color matching functions for a particular set of monochromatic primaries



Using the color matching functions to predict the primary match to a new spectral signal

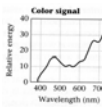
We know that a monochromatic light of λ_i wavelength will be matched by the amounts $c_1(\lambda_i)$, $c_2(\lambda_i)$, $c_3(\lambda_i)$

of each primary.



And any spectral signal can be thought of as a linear combination of very many monochromatic lights, with the linear coefficient given by the spectral power at each wavelength.

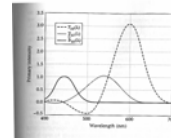
$$\vec{t} = \begin{pmatrix} t(\lambda_1) \\ \vdots \\ t(\lambda_N) \end{pmatrix}$$



Using the color matching functions to predict the primary match to a new spectral signal

Store the color matching functions in the rows of the matrix, C

$$C = \begin{pmatrix} c_1(\lambda_1) & \cdots & c_1(\lambda_N) \\ c_2(\lambda_1) & \cdots & c_2(\lambda_N) \\ c_3(\lambda_1) & \cdots & c_3(\lambda_N) \end{pmatrix}$$



Let the new spectral signal be described by the vector t .

$$\vec{t} = \begin{pmatrix} t(\lambda_1) \\ \vdots \\ t(\lambda_N) \end{pmatrix}$$

Then the amounts of each primary needed to match t are: $C\vec{t}$

Internal review

- So, for any set of primary colors, if we are given the spectral color matching functions for a set of primary lights
- We can calculate the amounts of each primary needed to give a perceptual match to any spectral signal.

Suppose you use one set of primaries and I use another?

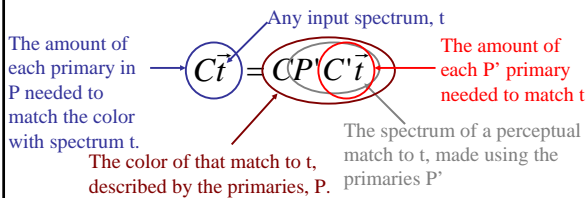
- We address this in 2 ways:
 - Learn how to translate between primaries
 - Standardize on a few sets of favored primaries.

How do you translate colors between different systems of primaries?

$$\begin{aligned} \text{Red } p_1 &= (0 \ 0 \ 0 \ 0 \ 0 \dots \ 0 \ 1 \ 0)^T & \text{Orange } p'_1 &= (0 \ 0.2 \ 0.3 \ 4.5 \ 7 \dots \ 2.1)^T \\ \text{Green } p_2 &= (0 \ 0 \dots \ 0 \ 1 \ 0 \dots \ 0 \ 0)^T & \text{Yellow } p'_2 &= (0.1 \ 0.44 \ 2.1 \dots \ 0.3 \ 0)^T \\ \text{Blue } p_3 &= (0 \ 1 \ 0 \ 0 \dots \ 0 \ 0 \ 0)^T & \text{Purple } p'_3 &= (1.2 \ 1.7 \ 1.6 \dots \ 0 \ 0)^T \end{aligned}$$

Primary spectra, P Primary spectra, P'

Color matching functions, C Color matching functions, C'



So, how to translate from the color in one set of primaries to that in another:

The values of the 3 primaries, in the unprimed system

The values of the 3 primaries, in the primed system

$$e = CP'e'$$

a 3x3 matrix

P' are the old primaries
C are the new primaries' color matching functions

And, by the way, color matching functions translate like this:

From earlier slide $Ct = CP'C't$ But this holds for any input spectrum, t , so...

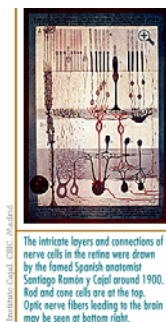
$C = CP'C'$

a 3x3 matrix that transforms from the color representation in one set of primaries to that of another.

P' are the old primaries
C are the new primaries' color matching functions

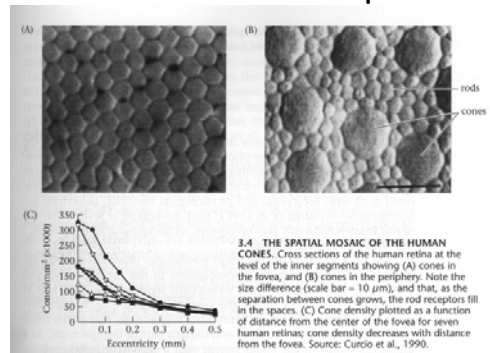
What's the machinery in the eye?

Eye Photoreceptor responses



(Where do you think the light comes in?)

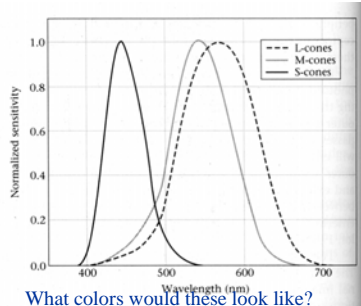
Human Photoreceptors



Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Human eye photoreceptor spectral sensitivities

3.3 SPECTRAL SENSITIVITIES OF THE L-, M-, AND S-CONES in the human eye. The measurements are based on a light source at the cornea, so that the wavelength loss due to the cornea, lens, and other inert pigments of the eye plays a role in determining the sensitivity. Source: Stockman and MacLeod, 1993.

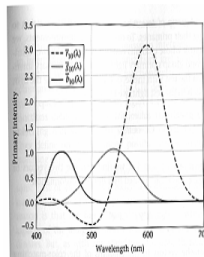


What colors would these look like?

Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

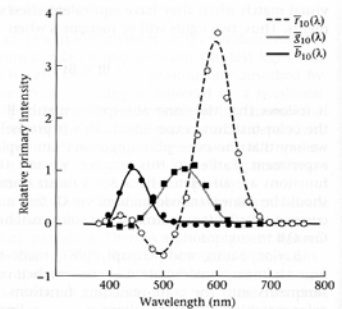
Are the color matching functions we observe obtainable from some 3x3 matrix transformation of the human photopigment response curves? (Because that's how color matching functions translate).

Color matching functions (for a particular set of spectral primaries)



Comparison of color matching functions with best 3x3 transformation of cone responses

4.20 COMPARISON OF CONE PHOTOCURRENT RESPONSES AND THE COLOR-MATCHING FUNCTIONS. The cone photocurrent spectral responsivities are within a linear transformation of the color-matching functions, after a correction has been made for the optics and inert pigments in the eye. The smooth curves show the Stiles and Burch (1959) color-matching functions. The symbols show the matches predicted from the photocurrents of the three types of macaque cones. The predictions included a correction for absorption by the lens and other inert pigments in the eye. Source: Baylor, 1987.



Foundations of Vision, by Brian Wandell, Sinauer Assoc., 1995

Internal summary

- What are colors?
 - Arise from power spectrum of light.
- How represent colors:
 - Pick primaries
 - Measure color matching functions (CMF's)
 - Matrix mult power spectrum by CMF's to find color as the 3 primary color values.
- How share color descriptions between people?
 - Translate colors between systems of primaries
 - Standardize on a few sets of primaries.