RELIABLE BROADCAST IN NETWORKS WITH 
NONPROGRAMMABLE SERVERS

Hector Garcia-Molina, Boris Kogan
Department of Computer Science
Princeton University
Princeton, NJ 08544

Nancy Lynch
Laboratory for Computer Science
Massachusetts Institute of Technology
Cambridge, MA 02139

Abstract
The problem of implementing reliable broadcast in ARPA-like computer networks is studied. The environment is characterized by the absence of any multicast facility on the communications subnetwork level. Thus, broadcast has to be implemented directly on hosts. A reliable broadcast protocol is presented and evaluated by several important performance criteria.

1. Introduction.
Reliable broadcast of messages in point-to-point computer networks is an important distributed application that has received considerable attention. A simple and obvious way to broadcast a message is to send a separately addressed copy of it to every host in the network and repeat this process until an acknowledgment is received. This solution, however, leaves room for possible improvement in several directions. First of all, it is clearly inefficient since it can generate much more network traffic than necessary.

Efficiency could be improved if the network servers were programmed to handle broadcast messages intelligently. This approach is taken in [AwEv84], [DaMe78], [Peac80], [Rose80], and [SeAw83]. Unfortunately, it is not always applicable. For instance, Arpanet users cannot program that network’s servers (IMPs), nor are the servers preprogrammed to implement broadcast efficiently. However, even when servers are nonprogrammable, one can still achieve better efficiency than with the simple solution. In particular, expensive communication links can be identified and avoided whenever possible.

While the simple solution has reliability provisions in the form of acknowledgments this is not always adequate. Consider, for example, a situation when the broadcasting host gets disconnected from the network after delivering the message only to a portion of all hosts. The rest of the hosts will never (or until the source is reconnected) receive the message. Therefore, we would like to have a broadcast algorithm in which all hosts share the responsibility for reliable message delivery so that in the described scenario the hosts that successfully received the message from the source could then propagate it to others.

Finally, improvement can also come from taking advantage of the fact that broadcast applications usually operate on streams of many messages rather than on a few isolated messages. By ordering messages at the source and keeping track of the messages received so far at every host the algorithm we propose will be able to dynamically make decisions on how to propagate newly generated messages. The benefits gained in terms of...
reliability and low delay will outweigh the extra communication cost involved when the broadcast stream is sufficiently long (consists of many messages).

It is important to note that reliability is treated here as a relative measure rather than an all-or-nothing property. That is, instead of classifying protocols as reliable or unreliable, we try to estimate to what degree they are reliable (or unreliable). No statement can be made about the reliability of any broadcast protocol without first making some assumptions concerning the reliability of the network itself. For example, if the network stays in a partitioned state for an indefinite period of time, no protocol, no matter how clever, can guarantee reliable delivery of broadcast messages to all destinations. On the other hand, if the partition is repaired for a brief period of time, only to reappear and persist, some protocols might be able to take advantage of this brief opening to complete a broadcast while others might not. Thus it seems more justified to speak of relative reliability of a protocol, referring to the degree to which it is capable of utilizing communication opportunities presented by the dynamically changing network. This issue is discussed in greater detail in subsequent sections.

Interestingly enough, not all applications that make use of broadcast require that it be reliable. For example, in adaptive routing it may be necessary to distribute the information regarding queueing delays in different parts of the network. Broadcast could be used for this purpose. However, if a broadcast message is late in coming, due to communication failures, it might just as well not arrive at all because it will soon be outdated by a more recent one anyway.

So it seems useful to keep in mind some specific applications which require reliable broadcast. The main motivating application that has been driving the present work is management of highly available replicated databases. There are several known techniques for solving the problem of high data availability in replicated databases in the face of network partitions, all of which require reliable broadcast of updates. But while the goal of reliable broadcast is to eventually deliver all messages to all destinations, there are some particulars associated with certain approaches. For example, in the type of approaches that forego serializability of transaction execution in order to achieve maximum data availability (e.g., Data-Patch [Garc83], log transformation [BIIK85], [Sari85]), it is not absolutely essential that updates be installed in remote copies of the database always in the correct order, i.e., in the order they were generated. Consequently, it is not essential that broadcast messages be always delivered in the order they were dispatched.

In designing a reliable broadcast we take into account this consideration. As a result, the stress is put on delivering messages as promptly as possible, but not necessarily in the same order as they are sent. Note that this relaxation of requirements on a reliable broadcast gives potentially more flexibility to the protocol and may improve its average delay characteristic.

2. Basic Assumptions.

In this section, the chosen network environment is described in more detail, and some motivations for considering this environment are introduced.

The network consists of a set of hosts, communication servers, and communication links. Hosts are computers that participate in the broadcast application. Servers are nodes interconnected among themselves by point-to-point bidirectional links into a communication subnetwork. (This study can be extended to the case when some of the links are of the broadcast type, however we choose not to consider this extension here.) Each host is attached to a server. Some servers, however, may have no corresponding hosts, and, therefore, act only as switches.

In reality, a server is either a separate dedicated communication processor (e.g., Arpanet) or a process residing at the same physical computer with the corresponding host (e.g., Bitnet). If the latter is true, a clean interface between the host and the corresponding server is assumed. For our purposes it is both convenient and sufficient to assume that servers are separate nodes.

There is no multicast facility provided by the network, and servers cannot handle messages with multiple addresses. The only kind of instruction a host can give to a server is request it to deliver a message to a single destination. Thus if the same message is to be sent to several destinations, the above procedure has to be repeated several times. Servers are assumed to be nonprogrammable as far as the broadcast application is concerned, i.e., the code that is run on the servers cannot be changed to expedite reliable broadcast. That leaves the
The only remaining alternative: implementing broadcast on the hosts.

The kind of scenario described in the previous paragraph is quite realistic. It may arise in a network of the type of Arpanet (which still does not provide a multicast facility) when (some of) the hosts connected to the network wish to enact efficient and reliable broadcast for a common application.

The host that issues broadcast messages (which will also be called data messages) is referred to as the source. Here, we study only a single-source broadcast problem. However, a multiple-source broadcast can be performed reliably by running several identical single-source protocols suggested in the present paper. From the point of view of efficiency this option also appears to be a reasonable one.

The hosts are reliable and never fail. The servers and links, however, can fail. In view of this latter assumption, the assumption concerning the reliability of hosts is no longer overly restrictive, for a host crash can now be "simulated" by a server or link failure, provided of course that hosts are equipped with non-volatile data storage. Namely, if a host crashes, the effect on the broadcast application is the same as if the link connecting the host to its server went down: in either case there is no message traffic to or from the host.

We make no assumptions about communication failures in the network other than the impossibility of malicious messages being generated. Links can fail and recover at any time. Messages can arrive out of order, have arbitrary delays, be lost at any point (even when the link over which the lost message was sent is perceived to be operational), or be spontaneously duplicated. Moreover, the fact that a message is lost is not automatically detected by the communication subsystem and, therefore, cannot be reported to the application. Similarly, failures of links and their recoveries are not detected either. Thus, the application can never be certain whether a given link is operational at any given moment.

The reason for making as few assumptions as possible about the way the communication network behaves, particularly the way in which it may fail, is to design a protocol that does not depend for reliability on the data link layer of the network [Tan81]. There is a growing feeling among the researchers in the field against such dependency. Moreover, even though most of the existing networks have reliability mechanisms — such as message acknowledgments — implemented at the data link layer, it is likely that future designs will favor pushing these mechanisms up to the application layer. A strong efficiency argument can be made in favor of such arrangement.

The next assumption will be referred to as the communication transitivity assumption. It postulates that if during the (sufficiently long) time interval $(t, t')$ host $x$ can communicate with host $y$, and $y$ can communicate with host $z$, then, during $(t, t')$, $x$ should also be able to communicate with $z$. The significance of communication transitivity will become apparent when we discuss the particulars of the proposed protocol. The assumption seems quite reasonable for networks with adaptive routing since in a situation described there exists at least one communication path between hosts $x$ and $z$ — the one that goes through (the server of) host $y$. Given sufficient time, the routing algorithm will discover it.

Hosts possess no knowledge of the network topology or any other static information concerning the network. They do, however, know the identities of other participating hosts. (When this latter assumption is not valid, i.e., some hosts do not know the identities of all other hosts, the problem becomes very different. See [Deme87] for a possible solution.)

We assume that there is a division of all links into two categories, according to their bandwidth. High bandwidth links are called cheap; low bandwidth links are called expensive. For obvious reasons, it is not specified what high and low mean precisely, but we assume that expensive links are much more expensive than cheap ones. This assumption is motivated by the existence of long haul networks (with low bandwidth links) with local networks (with high bandwidth links) integrated into them. In a global network of this kind some hosts are connected via cheap links while others are connected via expensive links only.

Since they have no static information about the network, hosts do not know which links are cheap and which are expensive. We assume, however, that there is a way for a host to tell whether the message it has just received traversed an expensive link on its way to the destination. (For instance, there could be a special bit in the message format initialized to 0 and set to 1 by a server whenever the message in question traversed
an expensive link. Even if the network did not provide this type of service, it could be implemented at the host level. One way to do this would be to timestamp each message at the time it is sent out. This would allow each host to estimate the time in transit. Since the expected times for cheaply delivered messages and for expensively delivered ones vary significantly, hosts would be able to tell them apart.) The ability to distinguish expensively delivered messages from cheaply delivered ones is the only kind of dynamic information available to hosts.

Finally, we assume that at any given time all the hosts in the network can be divided into groups such that within each group hosts can communicate among themselves cheaply, but hosts in different groups can only communicate using expensive links. Such a group of hosts is called a cluster. Clustering of hosts can change over time due to failures and repairs of communication links. Note that a host’s view of the constituency of its cluster may not always be consistent either with that of other hosts or with reality.

### 3. Basic Ideas

As was mentioned earlier, the goals of our protocol should be low cost, low average delay, and high reliability. In this section we focus on some basic ideas on how to achieve these goals, without going into details of the proposed algorithm.

We start with a fairly obvious observation, namely that optimal cost cannot be achieved for broadcast in our environment. This is illustrated by the example in Figure 3.1.

In this example we have three hosts connected by a network of four servers (hosts are denoted by squares, and servers by circles). Host $h_1$ is the source of broadcast. Clearly, the most cost efficient (as well as the delay minimizing) way for $h_1$ to broadcast a message would be as follows. Host $h_1$ hands the message to its server ($s_1$). $s_1$, then, sends it to server $s_4$. $s_4$ makes two copies of the message and sends one copy each to servers $s_2$ and $s_3$. Finally, $s_2$ and $s_3$ pass the message on to hosts $h_2$ and $h_3$, respectively. In this way, no link is traversed more than once (and, obviously, every link has to be traversed in the given example for the broadcast to succeed).

![Figure 3.1.](https://example.com/fig3.1.png)

Note, however, that, according to our assumptions, servers cannot handle multiply addressed messages, nor is there any way for host $h_1$ to explicitly instruct server $s_4$ to duplicate the message and send the copies to two separate destinations (and even if there were, that would do no good because $h_1$ knows nothing of the network topology). Hence, broadcast cannot possibly be performed as described above. So, no matter what type of protocol one comes up with for our environment, it will not, in general, have optimal performance. Therefore, the goal of our algorithm should be to minimize the cost of broadcast given the restrictions of server nonprogrammability.

Assuming that the network is not partitioned and disregarding for now the possibility of any changes in it, we could arrange clusters in a tree rooted at the cluster containing the source. Then broadcast messages could trickle down the cluster tree from parent cluster to child cluster.

Every cluster has a special (dynamically selected) host in it, called a cluster leader. A cluster leader receives broadcast messages from one of the hosts in the parent cluster, and it is responsible for delivering them to other members of its own cluster (cluster neighbors). Broadcast is initiated when the source sends a message to its cluster neighbors. The source is considered the leader of its own cluster. Figure 3.2 shows an example of a cluster tree. Nodes of this tree are represented by ellipses. Within each cluster (ellipse), hosts are represented by boxes, with boxes denoting cluster leaders shaded.

The tree arrangement helps reduce the number of transmissions required to complete broadcast of a data message. If we also want low average delay, however, it is not enough to come up with just any cluster tree. The main idea for reducing delays is, for every cluster, to try to find a parent cluster that can deliver new broadcast messages as promptly as possible. Namely suppose that, for a given cluster $C$, we have a choice of
4.1. The Host Parent Graph.

To enact broadcast, hosts attempt to configure themselves into a tree with the source as its root. In a failure-free environment, such a tree would be stable, and data messages could be sent from parent to child to make broadcast complete. However, because of the possibility of link failures, the tree can become disconnected, and the nodes should be able to reconfigure into a different tree if at all possible. The resulting structure is, therefore, dynamic and referred to as the host parent graph, to underscore the fact that connectivity is not always achieved (e.g., during network partitions).

(It is important not to confuse communication links of the network with edges of the host parent graph. For the latter correspond to communication paths that, in general, can consist of several links.)

We say that a host parent graph $H$ induces a cluster tree $L$ if (1) $H$ is a tree; and (2) children of every cluster leader include all other hosts that are in the same cluster. Note that if a child of a cluster leader in $H$ is not from the same cluster, it must be a cluster leader itself, otherwise condition (2) above would be violated.

The relationship between $H$ and $L$ is illustrated by the example in Figure 3.2. A node in $L$ (denoted by an ellipse) is uniquely determined by lumping together a cluster leader and all its children in $H$. For example, in Figure 3.2, $C$, $C'$, and $C''$ are all nodes in $L$, with $C$ being a child of $C''$.

Not every host parent graph, though, induces a cluster tree. Consider again the host parent graph of Figure 3.2. Suppose that a high bandwidth path has just been repaired between clusters $C''$ and $C$. That means that these two clusters have been joined into one. According to the definition, the host parent graph no longer induces a cluster tree.

Failures can also cause messages to get lost, and the reliable broadcast algorithm must compensate for this. To detect lost packets, all broadcast messages are sequence numbered so that it is easy to tell when a message has failed to be delivered to any given host. When that happens, certain actions are taken to enact a redelivery of the lost message.

4. The Algorithm.

In the previous section, some high level strategies for enacting efficient reliable broadcast were outlined. In this section, the actual broadcast algorithm is presented, in particular it is shown how to construct and dynamically maintain a cluster tree. (For a formal specification of the algorithm see [Garc87].)

---

1 This is different from a cluster tree.
situation that will be eventually corrected by the algorithm. In the remainder of this section, any host whose parent is not in the same cluster will be regarded as a cluster leader.

Broadcast messages are propagated in the host parent graph from the root all the way down. Thus, upon receipt of a broadcast message, a host sends it on to all its children. For reasons explained below, a host can accept a message sequence-numbered higher than any it has received so far, only from its parent. If such a message arrives from any other host, it is discarded. A message is also discarded if the recipient host has previously accepted it. (Repeated delivery may be caused, for example, by dynamic changes in the host parent graph.)

4.2. The Attachment Procedure.

At the heart of the algorithm is the attachment procedure, which is periodically activated at every host. The purpose of this procedure is to make sure that the host is attached to a "good" parent, and if that is not the case, find a better one.

As was mentioned earlier, broadcast messages are sequence numbered. Every host keeps track of all the messages it has received so far. For each host $i$, a set $\text{INFO}_i$ contains the sequence numbers of all messages received by $i$. Let us define a partial ordering $<$ on sets of message sequence numbers. We write $A < B$ if the largest element of $A$ is strictly less than the largest element of $B$, i.e., if $\max(q) < \max(q)$. Also, we write $A \succeq B$ if $A \subset B$. If $\max(q) = \max(q)$, these sets are used for detection of duplicates and redelivery of lost packets. They are also used for dynamically maintaining the host parent graph with the goal of maximizing reliability and minimizing delays.

Each host $i$ maintains an array of sets of message sequence numbers, $\text{MAP}_i$. $\text{MAP}_i[j]$ represents host $i$'s view of $\text{INFO}_j$ (thus, $\text{MAP}_i[i] = \text{INFO}_i$). Hosts periodically update one another on the current values of their $\text{INFO}$ sets. $\text{INFO}_s$, where $s$ is the source, gets updated every time a new broadcast message is generated at the source.

$\text{CLUSTER}_i$ is a set that contains the identities of hosts that, according to host $i$, are in the same cluster with $i$. This set can be updated when a message (of any kind, not necessarily a broadcast message) is received from another host $j$. If the cost bit in the message is 1, and $j$ was a member of $\text{CLUSTER}_i$, then $j$ is taken out of this set. Similarly, if the cost bit is 0, and $j$ was not in the set, it is added. $\text{CLUSTER}_i$ is initialized to $\{i\}$, i.e., in the beginning each host assumes that it is in a cluster by itself. Of course, if there is some information to the contrary, then $\text{CLUSTER}_i$ can be initialized differently.

$\text{CHILDREN}_i$ is a set of all the children of host $i$ in the host parent graph and is maintained by host $i$ itself. Also, host $i$ has an array $\text{pi}[j]$ such that its $j$-th element is the supposed parent of host $j$. Entry $\text{pi}[i]$, of course, is the true parent of $i$, at all times. Array $\text{pi}$ is updated when cluster neighbors periodically inform $i$ of the identities of their new parents.

Finally, there is a static linear ordering imposed on all the hosts. The number assigned by the ordering to host $i$ is denoted by $\text{order}(i)$.

The attachment procedure consists of a number of options that must be tried by the host, in the order indicated, until either a suitable new parent is found or all options are exhausted without success. In the latter case, the host waits a certain period of time\(^1\) before initiating the same procedure again. If, however, a parent is found, a message is sent to it requesting inclusion in its $\text{CHILDREN}$ set. If the acknowledgment to this message times out, the procedure is repeated to find another candidate with which the given host can communicate. The old parent, if any, is also notified of the change by an appropriate message.

The options, for each host $i$, are as follows (the new parent of $i$'s denoted by $j$).

I. For a host currently without a parent:

1. Attach to a host in the same cluster that has a parent in a different cluster or no parent at all (a cluster leader), and a greater (according to relation $<$) $\text{INFO}$ set. Thus $j$ must satisfy the following conditions:

   \[
   j \in \text{CLUSTER}_i; \quad \text{pi}[j] \notin \text{CLUSTER}_i; \quad \text{MAP}_i[i] < \text{MAP}_i[j]
   \]

2. Attach to a cluster leader in the same cluster with an "equal" $\text{INFO}$ set and a greater

\(^1\)This time period is a parameter of the algorithm.
First of all, we need to show that the attachment procedure constructs a parent graph that is dynamically acyclic, i.e., has no persistent cycles, barring the case of partition. Since hosts accept broadcast messages only from their parents and no host ever attaches to a parent with a smaller INFO set, no host's INFO set can be smaller than that of any of its descendants. Therefore the only way to form a cycle is for a host to attach to one of its own descendants with an "equal" INFO set.

Let us first consider cycles that involve hosts from several clusters. Such a cycle contains at least one cluster leader, which will look for a new parent with a greater INFO set soon after the cycle is formed (case II, option (3)). If the cluster leader is successful in its search, the cycle will be broken when the leader attaches to its new parent. Otherwise, it means that the leader cannot communicate with any hosts that have greater INFO sets. By the transitivity assumption, none of the hosts on the cycle can communicate with such hosts either. Therefore the cycle will not be broken until communications are restored. Note, however, that a cycle in the host parent graph is undesirable only because no host on it can get any new broadcast messages. But in the described situation this is the case even if there were no cycle (because of an apparent network partitioning). Thus, the presence of a cycle is unimportant here (as long as it gets broken when communications are restored).

A cycle contained within a single cluster can be detected when a host i tries option (1) of case III and discovers that it is its own ancestor (i ∈ ANCI), by following parent pointers. But, unlike a cycle that spans multiple clusters, this type of cycle cannot be automatically broken by the attachment procedure. Therefore we need a special rule for breaking single-cluster cycles. The host with the highest static order number on the cycle shall detach from its parent and go through the appropriate options for finding a new one. Once again, success is guaranteed unless there is a network partition. Having considered both types of cycles, we can conclude now that unless there is a partition in the network, no cycle in the parent graph can be stable. On the other hand, if there is a partition, then the presence of a cycle is not detrimental to broadcast.

Options (1) and (2) of cases I and II work towards establishing a single cluster leader for
each cluster, by making it a priority to look for a new parent within the cluster. Only when this fails, does the host look for a parent outside its cluster (option (3) of cases I and II). Option 1 of case III (for a host with a parent within the same cluster) attempts to establish a connection with a cluster leader directly, if it is not the case already. As a result, all hosts in the same cluster tend to organize into a single cluster tree node.

Option (3) of case I is for a host that has been unable to find a parent within its own cluster and, therefore, has to look elsewhere. This host, then, becomes a cluster leader.

Option (3) of case II is for a cluster leader that tries to improve its situation in terms of the delay with which it receives broadcast messages, by switching to a parent that has received more recent messages (with greater sequence numbers). This idea for reducing delays is similar to the one proposed by Awerbuch and Even [AWEv84]. In their work, however, it was applied in a different network setting (programmable servers, more restricted failure assumptions, disallowed acceptance of out-of-order messages).

Besides being an instrument for reducing delays, option (3) of case II can help a host to detect when its parent has become disconnected from it. For, in that case, the old parent's INFO set, as perceived by the child, will fall behind those of other out-of-cluster hosts with which the given host can communicate. Note, however, that for hosts other than cluster leaders the attachment procedure does not provide an automatic way of detecting the failure or disconnection of the parent. Therefore, we need a separate provision to help detect this situation. One way to do this would be to time out on a parent that fails to send messages such as the ones containing its INFO set and the identity of its own parent, which are being routinely exchanged by hosts in the same cluster. When this occurs, the host sets its parent pointer to NIL and goes through options (1) to (3) of case III.


The attachment procedure presented above is a way for the hosts participating in broadcast to adjust to component failures as well as to the changing loads in different parts of the network. The part of the protocol discussed here deals with compensating for lost broadcast messages (or filling gaps in INFO sets). Note that loss of messages can result not only from unreliable behavior of the communication subnetwork, but also from the workings of the attachment procedure. In particular, after a host has attached to a new parent, it may receive a broadcast message from its old parent (if the old parent never got the message requesting detachment from its former child), but in compliance with the restriction introduced above it is forced to discard it.

One type of gap filling action takes place among host parent graph neighbors. When a host attaches to a new parent, the parent examines its new child's INFO set and forwards to the child all those messages that the child is missing and that the parent has. When a host receives a gap filling message (a broadcast message with a sequence number less than the largest it has already seen), it forwards it to all those of its parent graph neighbors (its children and its parent) that according to its MAP do not have it. In addition to the above, every host periodically tries to fill its parent graph neighbors' gaps by sending them messages that it perceives as missing from their INFO sets. This is done more frequently for the members of the same cluster and less frequently for the members of different clusters. The restriction that a host can accept broadcast messages only from its parent does not have to apply to gap filling messages because they do not alter the order among INFO sets.

Gap filling among parent graph neighbors only is not sufficient in that it fails, in some cases, to fill all the gaps or at least as many gaps as the current communication status of the network would allow. To illustrate consider the following example. Let there be three hosts in the network: s (the source), i, and j (all in different clusters). The parent graph is shown in Figure 4.1. In it, s is the root, and i and j are its children. Suppose that a network partitioning occurs that leaves s isolated from the rest of the network. But i and j can still communicate with each other. Suppose, further, that three data messages (numbered 1, 2, and 3) were issued by s before the network partitioned; message number 2 has not reached node i, and message number 1 has not reached node j. Since neither INFO<sub>s</sub> < INFO<sub>j</sub> nor INFO<sub>j</sub> < INFO<sub>i</sub>, hosts i and j will not be able to reconfigure themselves into a new parent graph until the partitioning is repaired. And thus, as i and j are not parent graph neighbors, they will not be able to fill each other's gap even though they can communicate with each other.
least $k - 1$ inter-cluster transmissions, and probably more if there is more than one host per cluster.

As far as the delay characteristics, our algorithm appears to be comparable with the basic one. Since messages are addressed individually in the basic algorithm, the network can ensure that they are delivered to each host along a shortest path (assuming that the network provides a clever routing mechanism). In our algorithm, some hosts do not get their data messages directly from the source so clever routing by the network is not taken full advantage of. However, due to the delay minimizing properties of the attachment procedure (already discussed in the previous sections), the tree that is dynamically maintained by it tends to provide the shortest paths from the source to all other hosts. Moreover, our algorithm has the advantage of not being dependent on the routing service provided by the network.

In terms of recovery provisions our algorithm is superior to the basic one. When a host misses a message (in a fully connected network), the message is redelivered either by one of its cluster neighbors or by a host from the parent cluster, which tends to be one of the "closest" clusters to the host in question. In the basic algorithm, on the other hand, the source itself would always have to enact a redelivery, which, in general, is costlier because the host that needs this message may be in a very "remote" cluster.

In a partitioned network, the source, using the basic algorithm, does not stop trying to send data messages to all the hosts that are cut off from it, which is wasteful. In our algorithm, the hosts in the same partition will tend to organize into a tree, and only the root will periodically probe the network to detect when reconnection occurs.

It is important to point out that the basic algorithm can cause congestion of the source host's server since data messages go out separately to every host. Our algorithm does not present such a problem because responsibilities for disseminating data messages are distributed among all hosts.

Finally, it should be noted that, compared to the basic algorithm, ours may incur more additional cost in control messages, i.e., messages other than those containing broadcast data. (An example of control messages is exchange of $INFO$ sets among hosts as prescribed by the proposed algorithm. The basic algorithm also requires control messages in the form of acknowledgements.) How-

Figure 4.1.

To deal with this kind of situations we have to extend the periodic gap filling process described above so that it takes place even among hosts that are not host parent graph neighbors (e.g., between hosts $i$ and $j$ in the example of Figure 4.1). As in neighbor gap filling, a host tries to fill the gaps of other hosts when it can. However, the frequency of this type of gap filling should be relatively low since it operates across cluster boundaries, and therefore the communication cost is high.

5. Performance.

In this section, we present arguments that explain why the performance of our algorithm should be expected to be better than that of the basic algorithm mentioned in Section 1, which is the only known alternative for networks with nonprogrammable servers.

First, we compare the behavior of the two algorithms when there are no failures in the network. The cost of a broadcast algorithm is usually determined by the amount of traffic it generates, or more precisely, the number of transmissions over a single link necessary to complete the broadcast of a single data message (or $n$ messages, averaged over $n$). In our discussion, we will approximate the cost by counting only the number of inter-cluster host-to-host transmissions (as opposed to single link transmissions) since these are the most expensive ones. For example, with this metric, the cost of broadcasting a single data message in the network of Figure 4.1 would be 2 (provided there are no lost messages). This is so because $s$ has to send the message to both $i$ and $j$, and both of these paths are expensive. Note that in the original metric the cost would depend on the number of links in each path.

With the cluster tree arrangement we need only $k - 1$ inter-cluster transmissions, where $k$ is the number of clusters, to broadcast one data message. Clearly, this is optimal. In the basic algorithm, a data message from the source is sent separately to each host. That would require at least $k - 1$ inter-cluster transmissions, and probably more if there is more than one host per cluster.

$INFO_v = \{1, 2, 3\}$

$INFO_i = \{1, 3\}$

$INFO_v = \{2, 3\}$
ever, the traffic generated by control messages in our algorithm is totally independent of the number of data messages and can be adjusted as desired (see Section 6).

6. Conclusions.

We have presented a broadcast protocol for networks with nonprogrammable servers that appears to have good cost, delay, and reliability characteristics. We wish to emphasize, however, that our protocol is based on heuristics and, therefore, cannot be expected to perform optimally. The problem of efficient reliable broadcast in networks with nonprogrammable servers is a hard one, and solving it in a truly optimal way appears to be difficult.

There is one performance aspect that has not yet been discussed. It is the trade-off between reliability and cost-delay characteristics. That such should exist is no surprise. Reliability is understood to mean the ability of the algorithm to utilize as much as possible the communication opportunities presented by the network. Thus, if there is even a brief interval during which hosts \( h_1 \) and \( h_2 \) can communicate, and \( h_1 \) has a broadcast message that \( h_2 \) does not, a reliable protocol will detect this fact and have \( h_1 \) send this message (repeatedly if necessary) to \( h_2 \). But to achieve this, including the detection of the existence of the communication path between the two hosts, hosts have to exchange messages. The more frequently this is done, the more chance we will have to use the brief interval to deliver the message, and, at the same time, the more costly the algorithm will be.

In the algorithm presented here, these trade-offs are embodied in the frequency with which hosts enact INFO exchange, parent pointer exchange, and gap filling. These can be tuned according to specific cost-reliability requirements.

Throughout this paper we have assumed that hosts have access to dynamic information concerning clustering. Note that even if such information is unavailable, but instead there is a static knowledge of clusters, the latter can be used in the algorithm, albeit with less satisfying performance results. Furthermore, if no cluster information at all is available, the algorithm still can be used, with the assumption that every host is in a separate cluster by itself, at any given moment.

A number of fairly obvious optimizations can be incorporated in the actual implementation of the algorithm. For instance, some control messages that are dispatched by the same host at about the same time can be piggybacked in one packet. As another example, INFO sets can be pruned of messages with sequence numbers 1 through \( n \) when it becomes known that all hosts have safely received them.

7. Acknowledgments.

We would like to thank Barbara Blaustein, Charles Kaufman, Sunil Sarin, and Oded Shmueli for their helpful comments. Some of the ideas developed here were originally introduced in [Garc85].

8. Bibliography.


