# Model-based Autonomy in the New Millenium

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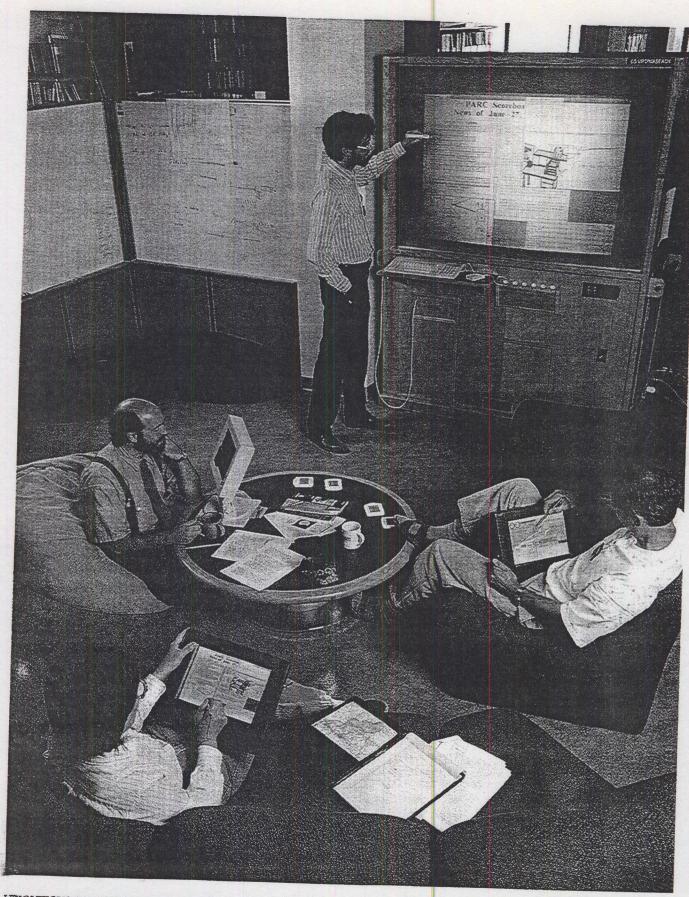
joint with P. Pandurang Nayak

#### **AI** Assertions

- Monmonotonic reasoning is essential to acting in the world.
- Deduction should be eliminated from the reactive loop.
- Qualitative modeling is too ambiguous.
- An LTMS is slow, an ATMS is fast.

## **Internet Agents**

- Testbeds easily available
- Can explore fundamental issues
  - mobility
  - realtime interaction
  - information gathering
- Its hip
- financially lucrative



UBIQUITOUS COMPUTING begins to emerge in the form of live boards that replace chalkboards as well as in other devices at the Xerox Palo Alto Research Center. Computer scientists gather around a live board for discussion. Building boards

and integrating them with other tools has helped researchers understand better the eventual shape of ubiquitous computing. In conjunction with active badges, live boards can customize the information they display.

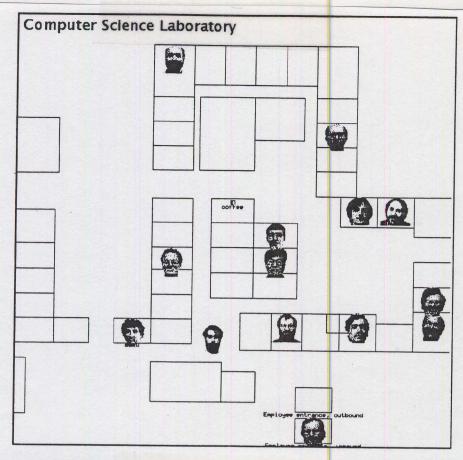
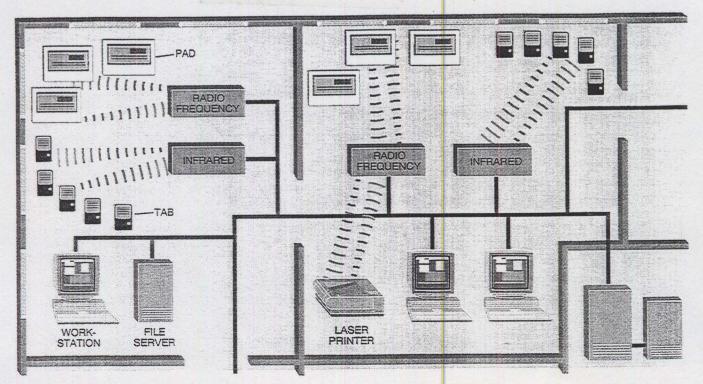


Figure 3. Display of CSL activity from personal locators.



WIRED AND WIRELESS NETWORKS link computers and allow their users to share programs and data. The computers pictured here include conventional terminals and file serv-

known as pads. Future networks must be capable of supporting hundreds of devices in a single room and must also cope with devices—ranging from tabs to laser printers or large-

## Outline

- Immobile Robots
- Model-based Autonomous Systems
- The Cassini Challenge
- Model-based Programming
- Model-based Execution
- A search engine for reactive control
- Hybrid Modeling
- Formalization and Reduction
- Deep Space One

#### **Immobile Robots**

- 1. Physically Embedded
- 2. Immobile
- 3. Self-Absorbed
  - Tight couplings
  - high reconfigurability
- 4. (Massively) Distributed
- 5. Heterogenous
- 6. Hybrid Discrete Continuous

## Model-based Autonomous Systems

- 1. Model-based Programming
  - compositional modeling
  - qualitative modeling
- 2. Model-based Execution
  - Self Configuration
  - Self Modeling
  - Deduction in the reactive loop
- 3. Model-based hybrid systems
  - concurrent systems ⇒ Livingstone (AAAI96)
  - adaptive systems ⇒ Moriarty (QR96), AA (AAAI94

## Model-based Programming

#### **Control Code Tasks:**

- monitoring
- tracking planner goal activations
- confirming hardware modes
- reconfiguring hardware
- detecting anomalies
- isolating faults
- diagnosis
- fault recovery
- standby
- safing
- fault avoidance
- parameter estimation
- adaptive control
- control policy coordination
  - ⇒ perform using a single model

## Model-based Autonomy

#### Requirements:

- 1. supports above functions
- 2. correct response to novel situations
- 3. 100msec reaction time
- 4. 4 month development time
- 5. 80 components, 280 modes
- 6. Hybrid models

## A Kernel for Model-based Execution

Requirements (3-5): 100 msecs, 80 components, 280 modes, 4 months

Heritage: Conflict-based Diagnosis (Sherlock)

- Diagnoses thousand component combinatorial circuits in 1-2 minutes
- Probabilistic, best first search
- Conflicts eliminate infeasible subspaces
- Prediction uses local propagation

 $\Rightarrow$  arg min f(X) st M(X)

#### A Kernel for Model-based Execution

To achieve reactivity: (100 msecs, 10,000 clauses)

- Precompile model
- Reduce model to propositional formula
- Exploit unit propagation
- ATMS → LTMS
- Best first enumeration exploits monotonic decrease of probability wrt superset

## Hybrid Modeling (6)

#### Heritage:

- Concurrent, reactive system specification (Manna & Pnueli 91)
- qualitative algebra (Williams 88, Struss88)

Components: concurrent transition systems

Software I/O: constraints over finite domain

Hardware I/O: algebra on sign and relative values

⇒ Reduce incrementally to propositional logic

## Failure Transition System: $\langle \Pi, \Sigma, \mathcal{T} \rangle$

• state variables  $\Pi$ , feasible states  $\Sigma$ , transitions  $\mathcal{T}$ .

• 
$$\tau \in \mathcal{T} : \Sigma \to 2^{\Sigma}$$

- Σ is finite
- $\tau_n \in \mathcal{T}$  denotes nominal transition all others denote failure.

**Trajectory:**  $\sigma: s_0, s_1, \dots$  for feasible  $s_i \in \Sigma$ 

- nondeterministically selects  $\tau_n$  or failure  $\tau$ .
- $s_{i+1} \in \tau(s_i)$  for some  $\tau \in \mathcal{T}$

## $\langle \Pi, \Sigma, \mathcal{T} \rangle$ Specified Propositionally

- propositional state formulae
  - propositions are  $y_k = e_k$ , such that  $y_k \in \Pi$  and  $e_k \in \operatorname{domain}(y_k)$
  - Given  $s_i$ ,  $y_k = e_k$  is true iff the value of  $y_k$  is  $e_k$  in  $s_i$
- next operator ()
  - Given  $s_i$ ,  $\bigcirc \Phi$  is true if  $\Phi$  is true in  $s_{i+1}$

П domain specified by:

$$\bigvee_{i} y_{k} = e_{ki}, \ \bigwedge_{i \neq j} \neg (y_{k} = e_{ki}) \wedge y_{k} = e_{kj})$$

 $\Sigma$  specified by state formula  $ho_{\mathcal{S}}$ 

$$au \in \mathcal{T}$$
 specified by  $ho_{ au} \equiv \bigwedge_i 
ho_{ au_i}$  where

•  $\rho_{\tau_i} \equiv \Phi_i \Rightarrow \bigcirc \Psi_i$  for state formulae  $\Phi_i$ ,  $\Psi_i$ .

## **Driver Example Specification**

```
\Pi = \{mode, cmdin, cmdout\}, \text{ where }
         1. mode \in \{on, off, resettable, failed\}
         2. cmdin \in \{on, off, reset, open, close, none\}
         3. cmdout \in \{open, close, none\}
PS:
mode = on \Rightarrow (cmdin = open \Rightarrow cmdout = open)
                      \land (cmdin = close \Rightarrow cmdout = close)
                      \land \neg (cmdin = open \lor cmdin = close) \Rightarrow cmdout = none
                    cmdout = none
mode = off \Rightarrow
\rho_{\tau_n}:
                                                         \Rightarrow \bigcirc mode = off
((mode = on) \lor (mode = off)) \land cmdin = off
                                                               \bigcirc mode = on
((mode = on) \lor (mode = off)) \land cmdin = on
                                                         \Rightarrow
                                                               \bigcirc mode = on
             \neg (mode = failed) \land cmdin = reset
                                                          \Rightarrow
                                                               \bigcirc mode = reset
              mode = reset \land \neg(cmdin = reset)
                                                         \Rightarrow
                                                               \bigcap mode = failed
                                     mode = failed
                                                         \Rightarrow
```

 $\rho_{\tau_f}$ :  $\bigcirc mode = failed$ .  $\rho_{\tau_r}$ :  $\bigcirc mode = reset$ .

# Concurrent Transition Systems $S = \langle \Pi, \Sigma, \Upsilon \rangle$

**Requirement:** Model used reactively ⇒ Synchronous

- ullet composed of transition systems  $\mathcal{C}\mathcal{D}$
- CD are concurrent and synchronous
  - Each  $\tau \in \mathcal{T}$  performs one  $\tau_C$  for each  $C \in \mathcal{CD}$ :

$$- \rho_{\tau} \Leftrightarrow \bigwedge_{C \in \mathcal{CD}} \rho_{\tau_C} \Leftrightarrow \bigwedge_{j} \left( \Phi_{ij} \Rightarrow \bigcirc \Psi_{ij} \right)$$

Generates trajectory  $\sigma: s_0, s_1 \dots$  defined by:

$$\rho_{st} \equiv \rho_{\Theta} \land \Box \left( \rho_{\Sigma} \land \bigvee_{i} \left( \bigwedge_{j} \left( \Phi_{ij} \Rightarrow \bigcirc \Psi_{ij} \right) \right) \right) \bigwedge_{i} \bigcirc_{i} \left( \rho_{\mathsf{obs}_{i}} \land \rho_{\mu_{i}} \right)$$

## **Hybrid Transition System**

- 1. Signs:  $\langle S', \oplus, \otimes \rangle$ ,  $S' = \{+, 0, -, ?\}$  (Minima AAAI88, AIJ91)
- 2. Relative values:  $\langle R', \oplus, \otimes \rangle$ ,  $R' \equiv \{L, N, H, ?\}$  where  $[x]_r = H, N, L$  iff  $[x x_n]_s = +, 0, -$

#### Example: Latched thruster

 $\Pi = \{mode, cmdin, inflow, thrust\}, \text{ where}$ 

$$mode = open \Rightarrow [inflow]_{sr} = [thrust]_{sr}$$
 $(mode = stuck\text{-closed})$ 
 $\lor (mode = closed) \Rightarrow [inflow]_{s} = [thrust]_{s} = 0$ 

```
ho_{\mathcal{T}n}:
((mode = open) \lor (mode = closed))
\land cmdin = close \Rightarrow \bigcirc mode = closed
((mode = open) \lor (mode = closed))
\land cmdin = open \Rightarrow \bigcirc mode = open
mode = stuck\text{-}closed \Rightarrow \bigcirc mode = stuck\text{-}closed
```

 $\rho_{\tau_f}$ : Omode = stuck-closed

# Configuration System $\langle S, \Theta, \sigma \rangle$

- transition system S
- initial state  $\Theta \in \Sigma$  of S
- goal configurations  $\sigma: g_0, g_1, \ldots$   $g_i$  specified by state formulae.

Generates configuration trajectory  $\sigma: s_0, s_1 \dots$ 

- $s_0$  is  $\Theta$
- $s_{i+1}$  satisfies  $g_i$  OR
- $s_{i+1} \in \tau(s_i)$  for  $\tau \neq \tau_n$

#### Mode Identification

Functions: confirm hardware modes, track planner goal activations, detect anomalies, isolate faults and perform diagnosis.

#### Given time i:

- ullet  $S_i$  denotes possible states prior to control
- ullet  $S_{\mu_i}$  denotes states with control  $\mu_i$
- $S_i \cap S_{\mu_i}$  denotes possible states w control
- ullet  $S_{\mathcal{O}_{i+1}}$  denotes states with observations  $\mathcal{O}_{i+1}$

#### Then:

$$S_{0} = \{\Theta\}$$

$$S_{i+1} = \left(\bigcup_{j} \tau_{j}(S_{i} \cap S_{\mu_{i}})\right) \cap \Sigma \cap S_{\mathcal{O}_{i+1}}$$

$$= \bigcup_{s \in S_{i} \cap S_{\mu_{i}}} \left(\bigcap_{k} \tau_{jk}(s)\right) \cap \Sigma \cap S_{\mathcal{O}_{i+1}}$$

Weakening:

$$S_{i+1} = \bigcup_{s \in S_i \cap S\mu_i} \left( \bigcap_k \tau_{jk}(s) \right) \cap \Sigma \cap S_{\mathcal{O}_{i+1}}$$

$$\subseteq \bigcup_j \left( \bigcap_k \tau_{jk}(S_i \cap S\mu_i) \right) \cap \Sigma \cap S_{\mathcal{O}_{i+1}}$$

Recall:

$$\rho_{\tau_i} \equiv \Phi_i \Rightarrow \bigcirc \Psi_i$$

In terms of state formulae:

$$\rho_{S_{i+1}} \equiv \bigvee_{\tau_j} \left( \bigwedge_{\rho_{S_i} \land \rho_{S_{\mu_i}} \models \Phi_{jk}} \Psi_{jk} \right) \land \rho_{\Sigma} \land \rho_{\mathcal{O}_{i+1}}$$

## Mode Reconfiguration

**Functions:** reconfiguring hardware, standby, safing, fault avoidance

Given: goal  $g_i$ , possible states  $S_i$  and nominal model  $\tau_n$ 

Generate: control values  $\mu_i$ 

Let  $\mathcal{M}_i$  denote possible control actions at i:

$$\mathcal{M}_{i} = \{\mu_{j} | \tau_{n}(S_{i} \cap S_{\mu_{j}}) \cap \Sigma \subseteq g_{i}\}$$

$$\supseteq \{\mu_{j} | \bigcap_{k} \tau_{nk}(S_{i} \cap S_{\mu_{j}}) \cap \Sigma \subseteq g_{i}\}$$

In terms of state formulae:

$$\mathcal{M}_i\supseteq \ \{\mu_j|\ \rho_{S_i}\wedge\rho_{\mu_j} \text{ is consistent and}$$
 
$$\bigwedge_{\rho_{S_i}\wedge\rho_{\mu_j}\models\Phi_{nk}} \Psi_{nk}\wedge\rho_{\Sigma}\models\rho_{g_i}\}$$

## Livingstone

Task: Generate likely trajectories and optimal control actions

**Solve:** min f(X) st C(X) using conflict-directed BFS MI:

- •X: For  $S \in \mathcal{CD}$  introduce  $x \in X$  with domain  $\mathcal{T}_S$
- $\bullet C(X)$ : a state transitioned to using X is consistent with OBS

$$\rho_{S_{i+1}} \equiv \bigwedge_{\substack{\rho_{S_i} \land \rho_{S\mu_i} \models \Phi_{jk}}} \Psi_{jk} \land \rho_{\Sigma} \land \rho_{\mathcal{O}_{i+1}}$$

$$\bullet f(X) \colon p(\tau | \mathcal{O}_i) = \frac{p(\mathcal{O}_i | \tau) p(\tau)}{p(\mathcal{O}_i)} \propto p(\mathcal{O}_i | \tau) p(\tau)$$

• 
$$f(X)$$
:  $p(\tau|\mathcal{O}_i) = \frac{p(\mathcal{O}_i|\tau)p(\tau)}{p(\mathcal{O}_i)} \propto p(\mathcal{O}_i|\tau)p(\tau)$ 

MR:

- $\bullet X$ : control variables  $\mu$
- $\bullet C(X)$  :  $\mu_i$  satisfies:

$$\mathcal{M}_i\supseteq \{\mu_j|\ \rho_{S_i}\wedge \rho_{\mu_j} \text{is consistent and}$$
 
$$\bigwedge_{\rho_{S_i}\wedge \rho_{\mu_j}\models \Phi_{nk}} \Psi_{nk}\wedge \rho_{\Sigma}\models \rho_{g_i}\}$$

$$f(X) - p(\tau|\mathcal{O}_i) = \frac{p(\mathcal{O}_i|\tau)p(\tau)}{p(\mathcal{O}_i)} \propto p(\mathcal{O}_i|\tau)p(\tau)$$

#### Results

#### Newmaap Model Characteristics:

Number of components	80
Average modes/component	3.5
Number of propositions	3424
Number of clauses	11101

#### Recovery Scenario Performance:

Scenario	MI			MR	
	Checked	Accepted	Time	Checked	Time
EGA preaim failure	7	2	2.2	4	1.7
BPLVD failed	5	2	2.7	8	2.9
IRU failed	4	2	1.5	4	1.6
EGA burn failure	7	2	2.2	11	3.6
Acc failed	4	2	2.5	5	1.9
ME too hot	6	2	2.4	13	3.8
Acc low	16	3	5.5	20	6.1

#### Standard Combinatorial Suite:

Devices	# of components	# of clauses	Checked	Time
c17	6	18	18	0.1
.c432	160	514	58	4.7
c499	202	714	43	4.5
c880	383	1112	36	4.0
c1355	546	1610	52	12.3
c1908	880	2378	64	22.8
c2670	1193	3269	93	28.8
c3540	1669	4608	140	113.3
c5315	2307	6693	84	61.2
c7552	3512	9656	71	61.5

Applications: Cassini, ASSAP, Bioreactor ...