Timed Model-based Programming: Executable Specifications for Robust Critical Sequences

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Motivation
Deep space exploration:
• highly uncertain environment
• require highly robust system

Mission-critical sequences:
• launch & deployment
• planetary fly-by
• orbital insertion
• entry, descent & landing

Problem Statement
• Traditional programming can lead to “brittle” sequences:
  ➢ complexity of plant interactions
  ➢ complexity of control specification
  ➢ complexity of off-nominal behavior

• Time is central to the execution of mission-critical sequences:
  ➢ plant spec: component behavior includes latency and evolution
  ➢ control spec: hard-coded delays in sequence capture state knowledge

• Robust executive must consider time in its control and behavior models, in addition to reactively managing complexity

Current “State of the Practice”
Non-Critical Mission Sequences:
➢ Time-tagged nominal command sequences

Non-Critical Mission Sequences:
➢ If absolutely necessary, conditional behavior via rule-based monitors or hard-coded state machines

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Current “State of the Practice”
Non-Critical Mission Sequences:
➢ Time-tagged nominal command sequences

Critical Mission Sequences:
➢ Standard safing mechanism is disabled

Critical Mission Sequences:
➢ Hard-coded fault protection via highly-specialized s/w modules:
  ➢ ad-hoc
  ➢ complex
  ➢ expensive to generate and test
### Related Work

- State-based Specifications
  - StateCharts (Harel, '87)
  - Timed StateCharts (Kesten & Pnueli, '92)

- Synchronous Programming
  - Estelle (Berry & Gonthier, '92)
  - Lustre (Hohwy, '93)

- Constraint Programming
  - TCC (Saraswat, Jagadeesan & Gupta, '94)

- Robotic Execution
  - RAPs (Firby, '89)
  - ESL (Gat, '96)
  - TDL (Simmons, '98)

- Timed Formal Modeling
  - GDE, Sherlock (de Kleer & Williams, '87-'89)
  - Livingstone (Williams & Nayak, '96-'97)
  - Livingstone2 (Kurien & Nayak, '00)

- Timed Model-based Execution
  - RBurton (Williams & Gupta, '99)
  - Titan (Williams, Ingham, Chung & Elliott, '03)

- Mission Data System
  - MDS (Dvorak, Rasmussen, et al., '00)

### Principal Contributions

1. Language definition
   - Textual & graphical programming languages for control spec
   - Extension of plant modeling language to capture timed effects

2. Formal execution semantics
   - Plant modeled as factored Partially Observable Semi-Markov Decision Process (POSMDP)
   - Control program expressed as timed deterministic automaton
   - Execution defined in terms of legal plant state evolutions

3. Algorithm specification & implementation
   - Execution of timed control specifications
   - Reasoning on timed plant models (for estimation and reconfiguration)

4. Architecture design & implementation
   - Modular, state-based & fault-aware
   - Demonstrated on representative mission scenario

### Objectives & Outline

- Timed Model-based Execution "in a nutshell"
- Timed Model-based Programming: a visual programming paradigm
- Illustration of Timed Model-based Execution
- Execution semantics
- Executive implementation
- Contributions and future directions
Mars Entry Sequence:
State-based Specification

engine to standby
planetary approach
switch to inertial nav & hold attitude
rotate to entry-orient
separate lander

(Loosely based on Mars Polar Lander Entry Sequence)

Descent engine to "standby":
off
heating
30-60 sec
standby

Spacecraft approach:
• 270 mins delay
• Relative position wrt Mars not observable
• Based on ground computations of cruise trajectory

Switch navigation mode:
"Inertial" = IMU only

Rotate spacecraft:
• Command ACS to entry orientation
Mars Entry Sequence:
State-based Specification

engine to standby
planetary approach
switch to inertial nav
rotate to entry-orient & hold attitude
separate lander

Rotate spacecraft:
• Once entry orientation achieved, ACS holds attitude

Separate lander from cruise stage:
• When entry orientation achieved, fire primary pyro latch

Separate lander from cruise stage:
• In case of failure of primary latch, fire backup pyro latch
Key Features of Executive

- Simple state-based control specifications
- Models are writable/inspectable by systems engineers
- Handle timed plant & control behavior
- Automated reasoning through low-level plant interactions
- Fault-aware (in-the-loop recoveries)

TMBP for Mars Science Lab

MSL Mission (2009)
courtesy NASA JPL

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Timed Model-based Program

Timed Hierarchical Constraint Automata

- Graphical specification language for control programs, in spirit of Timed StateCharts
- Writable, inspectable by systems engineers

- compact encoding: multiple locations can be simultaneously marked
Timed Hierarchical Constraint Automata

- Graphical specification language for control programs, in spirit of Timed StateCharts
- Writable, inspectable by systems engineers

Mars Entry control program

- act on hidden state
- clocks provide timing mechanism

Timed Model-based Program

Timed Concurrent Constraint Automata

- Variant of Factored POSMDP (state not directly observable, next state depends on current state & time spent in state)
- Extend Concurrent Constraint Automata to timed behavior

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Timed Model-based Executive Architecture

Timed Model-based Program | Timed Model-based Executive
---|---
Control Sequencer | System Clock

Control Sequencer executes THCA

Mars Entry Example

Engine:

Goal: Standby

Deductive Controller provides state estimates and command sequences that achieve goals
Mars Entry Example

- **Engine to Standby**
- **Planetary Approach**
- **Switch to Inertial Nav**
- **Rotate to Entry-Orient & Hold Attitude**
- **Separate Lander**

- **T1 < 270 mins**
- **T1 ≥ 270 mins**

- **T2 < 4 mins**
- **T2 ≥ 4 mins**

- **Maintain Entry = Initiated**

- **Engine to Standby**
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Mars Entry Example

Model-based executive provides robustness in the goal-driven control loop.
Mars Entry Example

Complete EDL Scenario
- Proof-of-concept on a representative mission scenario: "Full" Entry, Descent and Landing scenario
- Control program (57 locations, 16 state vars, 6 clock vars)
- Plant model (~25 components, avg. 3-4 modes per component)

EDL Scenario Highlights
Key Capabilities
- Nominal operations:
  - Execution conditioned on state constraints
  - Execution conditioned on time constraints
  - Nominal mode tracking through commanded and timed transitions
  - Accept configuration goal and generate appropriate command sequence (single-step, multi-step reconfigurations)
- Operations in the presence of faults:
  - Fault diagnosis through commanded transitions
  - Fault diagnosis through timed transitions
  - Recovery by repair (deductive controller)
  - Recovery by leveraging physical/functional redundancy (control sequencer, deductive controller)

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TMBP Semantics

Plant Model
- Variables:
  \[ \Pi = \{ \Pi^s, \Pi^c, \Pi^o \} \]
  \( \Sigma \): full assignments \( \sigma \) over all vars in \( \Pi \)
  \( \Sigma_s \): plant states \( s \)
  \( \Sigma_c \): control actions \( \mu \)
  \( \Sigma_o \): observations \( o \)
- Factored POMDP:
  \[ PM = (\Sigma, T, P_0, P_I, P_O, R) \]
  \( T \): transitions
  \( P_0(s) \): initial state prob
  \( P_I(s' | s, \mu) \): transition prob
  \( P_O(o | s) \): obs prob
  \( R(s) \): state reward
**Timed Plant Model**

- **Variables:**
  \[ \Pi = \{ \Pi^t, \Pi^c, \Pi^o, \Pi^r \} \]
  
- **Factored POSMDP:**
  \[ TPM = (\sum_T, \mathcal{T}, P_0, P_T, P_1, R) \]
  
- Add \( \Sigma_i \) set of assignments over all plant timers in \( \Pi \)

**Mode Estimation**

- Given latest commands and observations, what is the most likely current state?
- Belief state update to estimate state for POMDPs:
  \[ p^{(i+1)}[s] = \sum_{s'} \sum_{\mu} p_{\text{obs}}(s'|s,\mu) p_{\text{trans}}(s'|s,\mu) \]

**Mode Reconfiguration**

- Given current belief state and configuration goal, what is the first control action from a policy that maximizes expected reward?
- Solve Bellman equation to compute optimal policy for POMDPs:
  \[ V^*(s) = \max_{\pi} \left[ \sum_{s'} \sum_{\mu} P(s'|s,\mu) V^*(s') \right] \]

**Timed ME & MR**

- **Problem:**
  For factored POSMDP, next state depends on current state, current control actions AND current timer values
- **Key Insight:**
  Define "system state" = plant states \( \cup \) plant timers
- Timed ME can now use same belief state update equations, where \( s \) is now the system state
- Timed MR finds optimal policy based on system state, defines "wait" actions to accommodate non-deterministic timed transitions

**Timed Control Program**

- **Control program:**
  - program locations: \( L_p \)
  - clocks: \( \Pi^c_p \)
  - deterministic automaton:
  \[ \lambda_{\text{cp}}: \Sigma \rightarrow \Sigma \]

**Executive Semantics**

- Interleaving model of execution
  cycle = discrete event + continuous phase
- Legal execution of TMBP:
  1. initial conditions are valid
  2. next state is legal
  3. next program location is legal
  4. next clock values are legal

Such that:
\[ P_0(t_0) > 0 \]
\[ t_0 = \lambda_{\text{cp}} \]
\[ \omega_0(x') = 0, \text{ for all clocks } x' \]
**Executive Semantics**

- Interleaving model of execution
  \( \text{cycle} = \text{discrete event} + \text{continuous phase} \)
- Legal execution of TMBP:
  \[
  \begin{array}{c|c}
  \text{Cycle start time} & t_0, t_1, \ldots \\
  \text{Plant state} & x_0, x_1, \ldots \\
  \text{Pgm location} & l_0, l_1, \ldots \\
  \text{Pgm clocks} & \omega_0, \omega_1, \ldots \\
  \end{array}
  \]

  Such that:
  1. initial conditions are valid
  2. next state is legal
  3. next program location is legal
  4. next clock values are legal

\[
\begin{align*}
\delta_t &= \delta_{t-1} + \Delta t, \\
\mu_t &= \text{MR}(PM, \delta_t) \\
\rho_t &= \text{ME}(PM, \delta_t, \mu_t, \omega_t)
\end{align*}
\]

**Implementation Approximations**

Mode Estimation:
- Full belief state update is computationally infeasible
- Assume probability of a few most-likely states dominates probability of other possible states
- Track a limited set of most-likely states, from one cycle to the next

Mode Reconfiguration:
- Assume probability of nominal behavior dominates off-nominal
- Assume reward of being in goal state dominates reward of getting to goal state
- Perform MR in 2 steps:
  - **Goal Interpretation**: find the max-reward goal state, reachable via nominal transitions, that satisfies the configuration goal
  - **Reactive Planning**: returns series of control actions that achieve the goal state

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Control Sequencer Implementation

Timed Model-based Program

Timed Model-based Executive

Plant Model

Control Sequencer

Deductive Controller

System Clock

Observations

Commands

Timers

THCA Execution Algorithm

1. update active clocks
2. check maintenance constraints
3. assert clock initializations & state goals
4. request MR to take action
5. obtain new state estimate from ME
6. await incomplete goals
7. take enabled transitions
8. mark new set of locations
9. return to step 1

Mode Estimation

- Mode Estimation tracks a limited set of most-likely states
- Explores state space in best-first order:
  - Formulate Optimal Constraint Satisfaction Problem (OCSP), to identify “k-best” extensions to current trajectories (“shortest path” from set of current possible states to next possible states)
  - Solve using OPSAT engine:

Timed Mode Estimation

- For physical plants modeled as TCCA (POSMDP):

  Bad news: state space gets much larger...

  Good news: can leverage existing OPSAT engine!

TCCA Mode Estimation Algorithm (k = 1)

Given current system state \( s^0 \), control action \( \mu^0 \), observation \( o^{(0)} \) & current time \( t^0 \):

1. Update timer values for \( s^0 \)
2. Compute probability associated with each possible next system state
3. Choose highest-probability system state
4. In this system state, reinitialize to zero any timers associated with components with changed modes
5. Return resulting system state

Perform steps 2 & 3 in best-first order, by framing as an Optimal Constraint Satisfaction Problem, then solving using OPSAT
TCCA Mode Estimation as OCSP

- Setup OCSP < x, f, C >:
  - decision vars x, such that dom[x] = reachable target modes
  - objective function f(x) = prior probability of state x, i.e.:
    \[ P_{T}(x) \prod_{i=1}^{n} \mu_{i}(t) \]
  - constraint C(x), such that x \land C_{M} \land d^{(i+1)} is consistent

- Solve using OPSAT

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Conclusions

- TMBP paradigm for visual programming of embedded systems:
  - THCA unify features of StateCharts, synchronous programming, constraint programming, timed automata and robotic execution languages
  - CCA allow constraint-based, probabilistic modeling of physical plants
  - (TCCA extend CCA to capture timed effects)

- Semantic specification for TMBP:
  - Physical plants modeled as factored POMDPs
  - ME as belief state update, MR as decision theoretic planning
  - Control programs modeled as deterministic automata
  - Control Sequencer steps control program location based on state & time
  - Execution of TMBP defined in terms of legal plant state evolutions

- Design & implementation of Timed Model-based Executive:
  - Execution architecture is modular, state-based & fault-aware
  - Control Sequencer executes THCA
  - ME performs approximate belief state update for (T)CCA
  - MR performs reactive planning for (T)CCA

Directions for Future Work

Theoretical:
- Formal verification (model checking) for timed plant models, timed control programs
- Extension to Hybrid Model-based Programming
  - Control programs can specify trajectories in terms of continuous and/or discrete states
  - Fold continuous estimators & controllers into Deductive Controller

Implementation:
- Improve Timed ME
  - Move costly M-B deduction offline, through compilation of the timed models
- Improve Timed MR
  - Consider time to reach goal to be included in cost

Mars EDL: RMPL Code Excerpt

```plaintext
MarsEDL:: ()
  do |
    EntrySequence(),
    DescentLandingSequence()
  watching (landing = success)
|
EntrySequence():
  engine = standby;
  t1 = 0;
  when (t1 >= 16200.0) donext |
    nav = inertial;
    t2 = 0;
  when (t2 >= 240.0) donext |
    do |
      always (att = entry-orient),
      when (att = entry-orient) donext (lander = separated)
    |
    watching (entry = initiated)
  |
|
```
TCCA Mode Reconfiguration
Algorithm Extensions

- Untimed MR algorithms have been extended to address:
  - timed transitions
  - irreversible actions

Desired MR behavior, given config. goal Engine = Firing...
RP should return the following control sequence:
(PDE-cmd = Turn-on, Engine-cmd = Standby, Wait until Standby mode is achieved, Valve1-cmd = Turn-on, Valve2-cmd = Turn-on, Engine-cmd = Fire, PDE-cmd = Turn-Off)

Assumptions/Limitations

1. Executive is “fast enough” to keep up with plant evolution
   - Mode of a component cannot change more than once per execution cycle, for ME algorithm to function correctly.
   - From Control Seq’s perspective, transitions assumed to occur at execution cycle start times, and plant state is assumed to hold constant through to the time of the next execution cycle.
   - Duration of execution cycle is dictated by Ded. Contr. computation time, so require this computation time to be short.
   - This assumption limits effective resolution of time constraints in control programs and plant models.

2. Observations are provided to executive in a timely manner
   - In the absence of observations to refute nominal behavior, current exec implementation assumes nominal behavior.
   - In case of timed transitions, executive will take transition at “expected” nominal transition time (mean of transition PDF).
   - Observation associated with a transition should be received within the execution cycle that the triggering command was issued.

Soundness Arguments

- Deductive controller
  - founded on proven model-based reasoning techniques
  - timed language extensions have properties similar to formal real-time specification languages, to allow for straightforward verification
  - algorithms implement a tractable approximation of factored POMDP semantics
  - despite worst-case exponential performance of on-line reasoning, practical experience has shown adequate performance for typical engineered systems
  - deductive controller enables in-the-loop robustness

Soundness Arguments (cont.)

- Control Sequencer
  - graphical language for control programs unifies:
    - representational efficiency of Timed Statecharts,
    - executable computational model for, and
    - verifiability properties of formal RT specification languages
  - execution algorithm provides the capabilities of robotic execution languages:
    - conditional execution
    - goal-driven execution
    - closed-loop execution
    - reactive preemption
  - execution algorithm is linear in # of THCA locations
  - implemented algorithm proven to conform to specified control sequencer semantic model

Soundness Arguments (cont.)

- Overall Executive
  - “traditional” model-based control architecture, familiar to spacecraft control and system engineers
  - control program provides “set points” for deductive controller
  - executive reacts to feedback from plant under control
  - modular and expandable architecture
  - can interface with existing system-level planning technologies (e.g. Kirk, ASPEN, EUROPA)

Execution Architecture
**ME in MDS**

- System State Vars
- Model-Based Mode Form
- Local State Vars
- Mode Estimators
- Qualitative Observations
- Measurements
- Sensor Adapters
- Actuator Adapters
- HW Devices

---

**Control Sequencer Semantics**

- **Input:**
  - timed control program \(TCP\)
  - sequence of plant state estimates
  - sequence of cycle start times from system clock
- **Output:**
  - sequence of config goals
- **Internally:**
  - updates clock variables according to
  - advances current TCP location according to

---

**Deductive Controller Semantics**

- **Input:**
  - plant model TPM
  - sequence of config goals
  - sequence of observations
  - sequence of observation times from system clock
- **Output:**
  - sequence of state estimates
  - sequence of control actions
- **Internally:**
  - composition of Mode Estimation and Mode Reconfiguration semantic specifications

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**“State of the Art” Solutions**

<table>
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<tr>
<th>Tool</th>
<th>SCL</th>
<th>ESL</th>
<th>TDL</th>
<th>CIRCA-II</th>
<th>Titan</th>
<th>Livingstone/L2</th>
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* For: provides framework for addressing the issue, but no explicit solution

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**Motivation**

High-risk systems

- Nuclear plant
- Chemical plant
- Space missions
- Military early-warning
- Trade schools
- Most manufacturing
- Post Office
- Universities
- R&D firms

“Standard” POSMDP vs. “TCCA” Factored POSMDP

- TCCA model is “Factored”:
  - State depends on multiple timer values, not just single “time” parameter
- Fundamental difference due to type of problem each is meant to address
  - Standard POSMDP model for systems where state changes are more frequent than “decision epochs” (opportunities to take an action)
  - TCCA model for composite system where decision epochs are more frequent than state changes