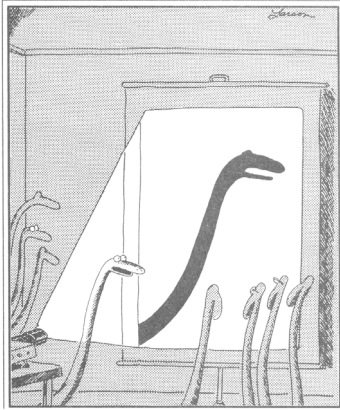


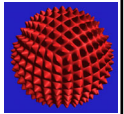
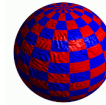
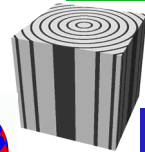
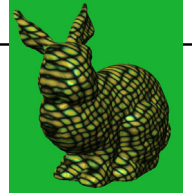
## Real-Time Shadows



"Now this is...this is...well, I guess it's another snake."

## Last Time?

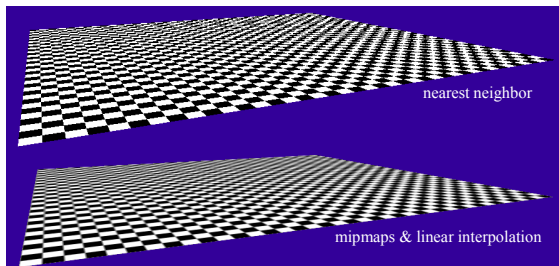
- Perspective-Correct Interpolation
- Texture Coordinates
- Procedural Solid Textures
- Other Mapping
  - Bump
  - Displacement
  - Environment
  - Lighting



MIT EECS 6.837, Durand and Cutler

## Textures can Alias

- *Aliasing* is the under-sampling of a signal, and it's especially noticeable during animation



MIT EECS 6.837, Durand and Cutler

## Schedule

- Quiz 1: Tuesday October 26<sup>th</sup>, in class (1 week from today!)
- Review Session: Monday October 25<sup>th</sup>, 7:30-9pm, 1-150
- Assignment 6: due Wednesday November 3<sup>rd</sup>

MIT EECS 6.837, Durand and Cutler

## RayTracer::traceRay confusion

**Vec3f** RayTracer::traceRay(Ray &ray, float tmin, int bounces, float weight, float indexOfRefraction, Hit &hit)

↑  
OUTPUT: radiance (color & amount of light) along direction

↑  
OUTPUT: intersection point

scene->getGroup()->intersect(ray, hit, t)  
should only be called once, from within RayTracer::traceRay

\*\* This will help you implement and debug fast raytracing (assignment 6)

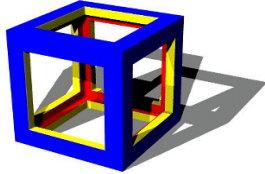
MIT EECS 6.837, Durand and Cutler

## Questions?

MIT EECS 6.837, Durand and Cutler

## Today

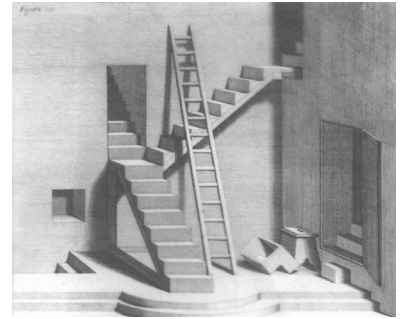
- **Why are Shadows Important?**
- Shadows & Soft Shadows in Ray Tracing
- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- Shadow Volumes



MIT EECS 6.837, Durand and Cutler

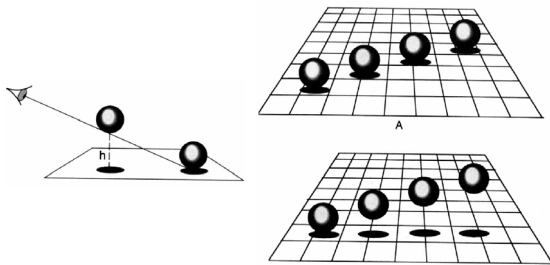
## Why are Shadows Important?

- Depth cue
- Scene Lighting
- Realism
- Contact points



MIT EECS 6.837, Durand and Cutler

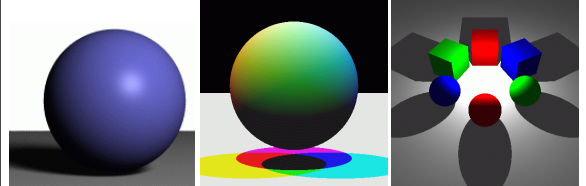
## Shadows as a Depth Cue



MIT EECS 6.837, Durand and Cutler

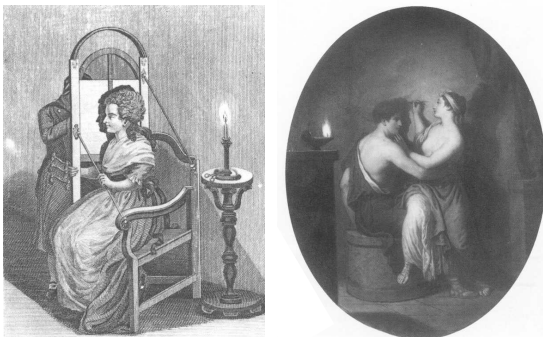
## For Intuition about Scene Lighting

- Position of the light (e.g. sundial)
- Hard shadows vs. soft shadows
- Colored lights
- Directional light vs. point light



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## Shadows as the Origin of Painting



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## Shadows and Art

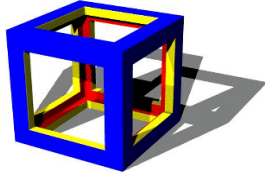
- Only in Western pictures (here Caravaggio)



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## Today

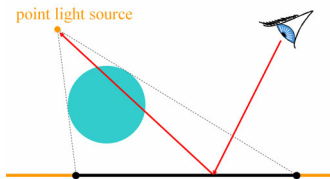
- Why are Shadows Important?
- **Shadows & Soft Shadows in Ray Tracing**
- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- Shadow Volumes



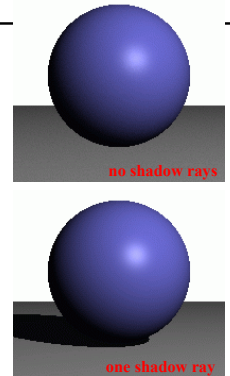
MIT EECS 6.837, Durand and Cutler

## Shadows

- One shadow ray per intersection per point light source

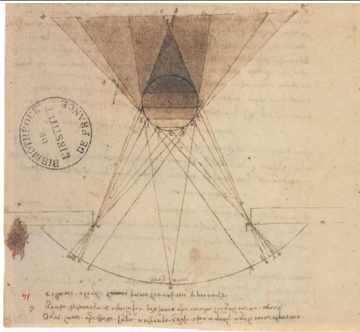


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## Soft Shadows

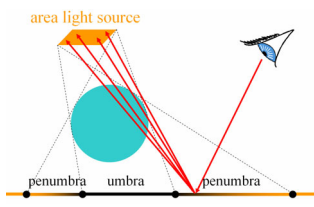
- Caused by extended light sources
- Umbra
  - source completely occluded
- Penumbra
  - Source partially occluded
- Fully lit



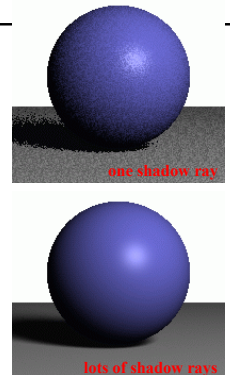
XVI. Léonard de Vinci (1452-1519). Lumière d'une fenêtre sur une sphère ondulée avec (en haut) ombre intermédiaire, primitive, dérivée et (sur la surface, en bas) pointe. Plume et encre sur papier, 24 x 38 cm, Paris, Bibliothèque de l'Institut de France (ms. 2185; B.N. 10016; 17-18 v.1).

## Soft Shadows

- Multiple shadow rays to sample area light source

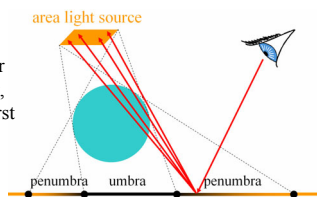


MIT EECS 6.837, Durand and Cutler



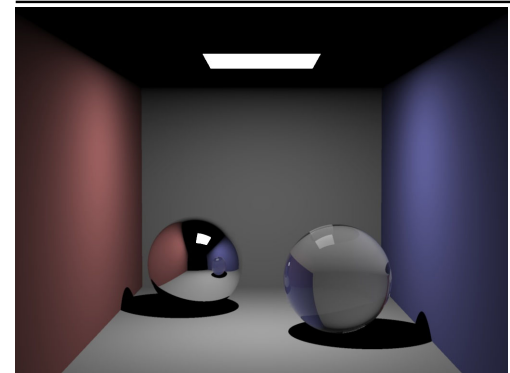
## Shadows in Ray Tracing

- Shoot ray from visible point to light source
- If blocked, discard light contribution
- Optimizations?
  - Stop after first intersection (don't worry about  $t_{min}$ )
  - Coherence: remember the previous occluder, and test that object first

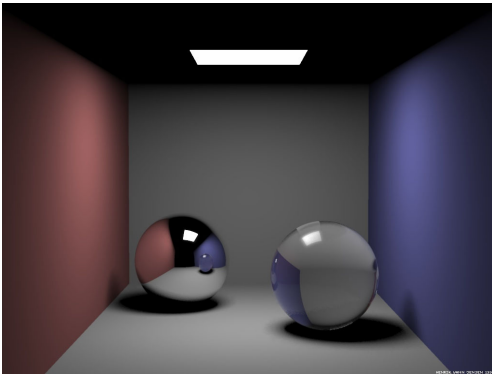


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## Traditional Ray Tracing

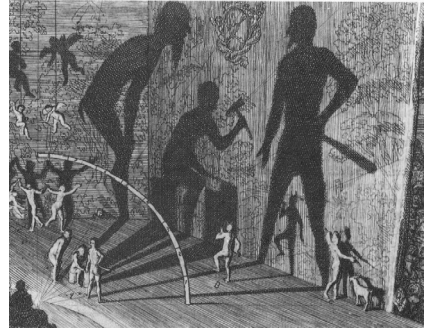


## Ray Tracing + Soft Shadows



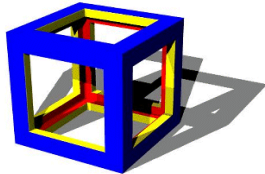
## Questions?

Plate 50 Samuel van Hoogstraten, *Shadow Theatre*. From *Inleyding tot de hooghe schooler schilder konst* 1678.



## Today

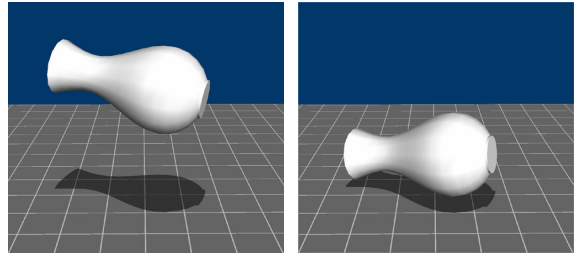
- Why are Shadows Important?
- Shadows & Soft Shadows in Ray Tracing
- Planar Shadows
- Projective Texture Shadows
  - Shadow View Duality
  - Texture Mapping
- Shadow Maps
- Shadow Volumes



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## Cast Shadows on Planar Surfaces

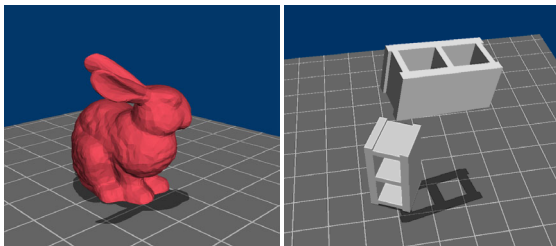
- Draw the object primitives a second time, projected to the ground plane



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## Limitations of Planar Shadows

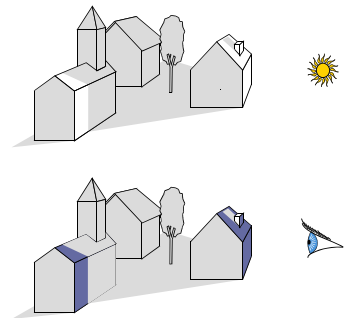
- Does not produce self-shadows, shadows cast on other objects, shadows on curved surfaces, etc.



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## Shadow/View Duality

- A point is lit if it is visible from the light source
- Shadow computation similar to view computation



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## Texture Mapping

- Don't have to represent everything with geometry



MIT EECS 6.837, Durand and Cutler

## Fake Shadows using Projective Textures

- Separate obstacle and receiver
- Compute b/w image of obstacle from light
- Use image as projective texture for each receiver

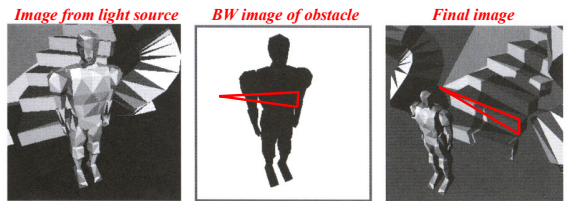


Figure from Moller & Haines "Real Time Rendering"  
MIT EECS 6.837, Durand and Cutler

## Projective Texture Shadow Limitations

- Must specify occluder & receiver
- No self-shadows
- Resolution



Figure from Moller & Haines "Real Time Rendering"  
MIT EECS 6.837, Durand and Cutler

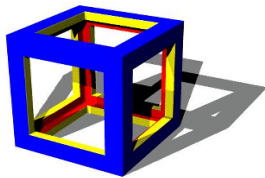
## Questions?



Plate 52 Grandville, *The Shadows (The French Cabinet)* from *La Caricature*, 1830.  
MIT EECS 6.837, Durand and Cutler

## Today

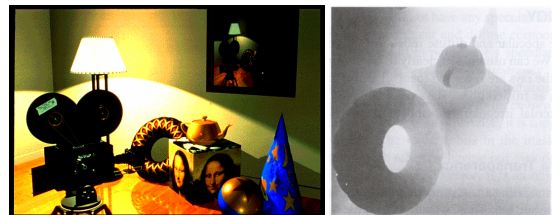
- Why are Shadows Important?
- Shadows & Soft Shadows in Ray Tracing
- Planar Shadows
- Projective Texture Shadows
- **Shadow Maps**
- Shadow Volumes



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## Shadow Maps

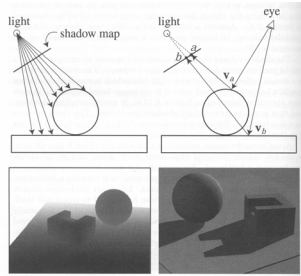
- In Renderman  
– (High-end production software)



MIT EECS 6.837, Durand and Cutler

## Shadow Mapping

- Texture mapping with depth information
- Requires 2 passes through the pipeline:
  - Compute shadow map (depth from light source)
  - Render final image, *check shadow map to see if points are in shadow*

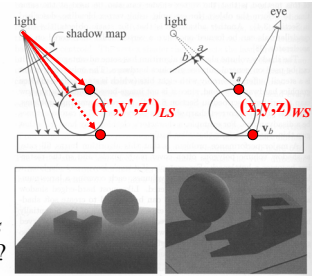


Foley et al. "Computer Graphics Principles and Practice"

MIT EECS 6.837, Durand and Cutler

## Shadow Map Look Up

- We have a 3D point  $(x, y, z)_{WS}$
- How do we look up the depth from the shadow map?
- Use the 4x4 perspective projection matrix from the light source to get  $(x', y', z')_{LS}$
- $ShadowMap(x', y') < z'$ ?

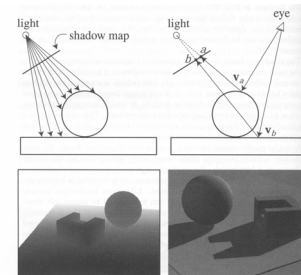


Foley et al. "Computer Graphics Principles and Practice"

MIT EECS 6.837, Durand and Cutler

## Limitations of Shadow Maps

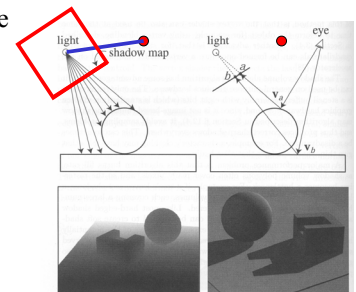
1. Field of View
2. Bias (Epsilon)
3. Aliasing



MIT EECS 6.837, Durand and Cutler

## 1. Field of View Problem

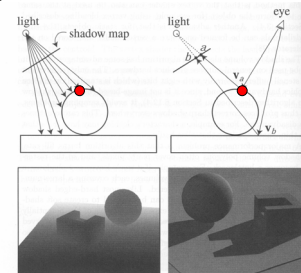
- What if point to shadow is outside field of view of shadow map?
  - Use cubical shadow map
  - Use only spot lights!



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## 2. The Bias (Epsilon) Nightmare

- For a point visible from the light source  $ShadowMap(x', y') \approx z'$
- How can we avoid erroneous self-shadowing?
  - Add bias (epsilon)

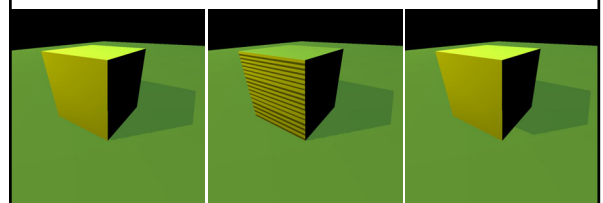


MIT EECS 6.837, Durand and Cutler

## 2. Bias (Epsilon) for Shadow Maps

$$ShadowMap(x', y') + bias < z'$$

Choosing a good bias value can be very tricky



Correct image

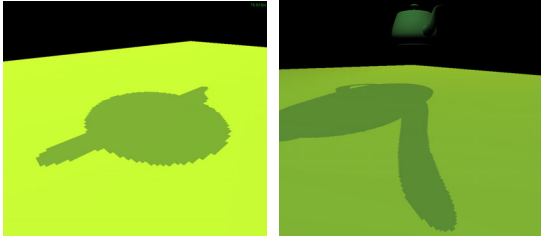
Not enough bias

Way too much bias

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### 3. Shadow Map Aliasing

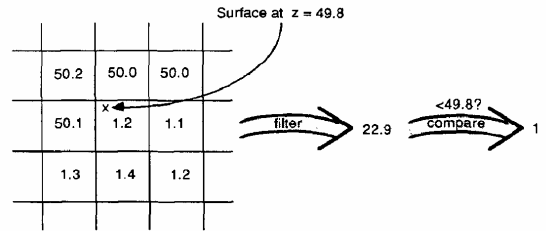
- Under-sampling of the shadow map
- Reprojection aliasing – especially bad when the camera & light are opposite each other



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### 3. Shadow Map Filtering

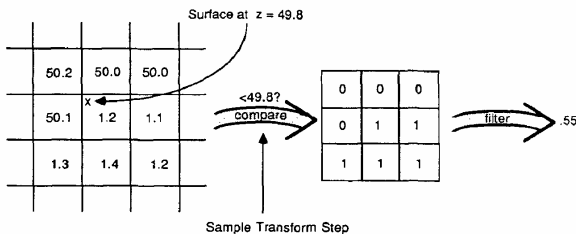
- Should we filter the depth? (weighted average of neighboring depth values)
- No... filtering depth is not meaningful



a) Ordinary texture map filtering. Does not work for depth maps.

### 3. Percentage Closer Filtering

- Instead filter the result of the test (weighted average of comparison results)
- But makes the bias issue more tricky



### 3. Percentage Closer Filtering

- 5x5 samples
- Nice antialiased shadow
- Using a bigger filter produces fake soft shadows
- Setting bias is tricky



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### Projective Texturing + Shadow Map



Light's View

Depth/Shadow Map

Eye's View

Images from Cass Everitt et al.,  
"Hardware Shadow Mapping"  
NVIDIA SDK White Paper

MIT EECS 6.837, Durand and Cutler

### Shadows in Production

- Often use shadow maps
- Ray casting as fallback in case of robustness issues



Figure 12. Frame from *Lemony Snicket's A Series of Unfortunate Events*.

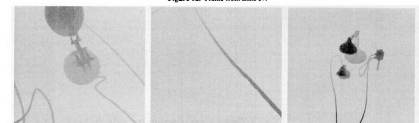
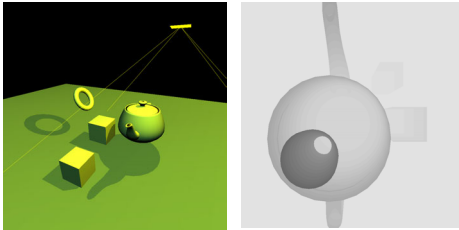


Figure 13. Shadow maps from *Lemony Snicket's A Series of Unfortunate Events*.

## Hardware Shadow Maps

- Can be done with hardware texture mapping
  - Texture coordinates  $u, v, w$  generated using  $4 \times 4$  matrix
  - Modern hardware permits tests on texture values



MIT EECS 6.837, Durand and Cutler

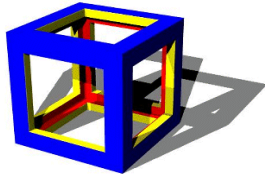
## Questions?



MIT EECS 6.837, Durand and Cutler

## Today

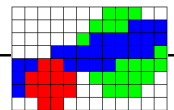
- Why are Shadows Important?
- Shadows & Soft Shadows in Ray Tracing
- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- Shadow Volumes**
  - The Stencil Buffer**



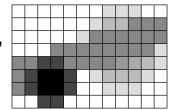
MIT EECS 6.837, Durand and Cutler

## Stencil Buffer

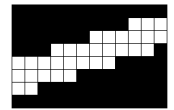
- Tag pixels in one rendering pass to control their update in subsequent rendering passes
  - "For all pixels in the frame buffer" → "For all *tagged* pixels in the frame buffer"
- Can specify different rendering operations for each case:
  - stencil test fails
  - stencil test passes & depth test fails
  - stencil test passes & depth test passes



frame buffer



depth buffer

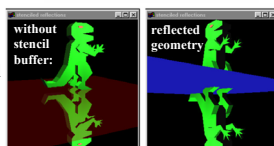


stencil buffer

MIT EECS 6.837, Durand and Cutler

## Stencil Buffer – Real-time Mirror

- Clear frame, depth & stencil buffers
- Draw all non-mirror geometry to frame & depth buffers
- Draw mirror to stencil buffer, where depth buffer passes
- Set depth to infinity, where stencil buffer passes
- Draw reflected geometry to frame & depth buffer, where stencil buffer passes

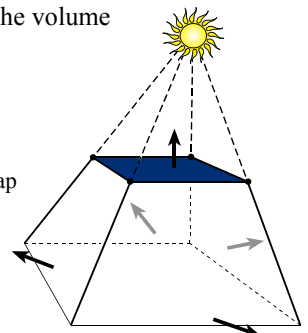


See NVIDIA's stencil buffer tutorial  
<http://developer.nvidia.com>

also discusses blending, multiple mirrors, objects behind mirror, etc...

## Shadow Volumes

- Explicitly represent the volume of space in shadow
- For each polygon
  - Pyramid with point light as apex
  - Include polygon to cap
- Shadow test similar to clipping

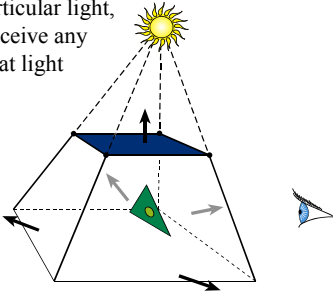


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## Shadow Volumes

- If a point is inside a shadow volume cast by a particular light, the point does not receive any illumination from that light

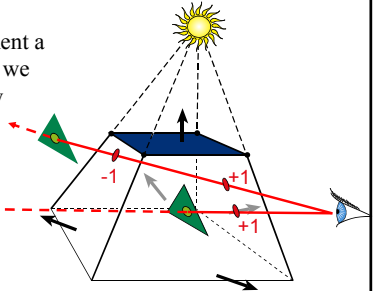
- Cost of naive implementation:  
 $\# \text{polygons} * \# \text{lights}$



MIT EECS 6.837, Durand and Cutler

## Shadow Volumes

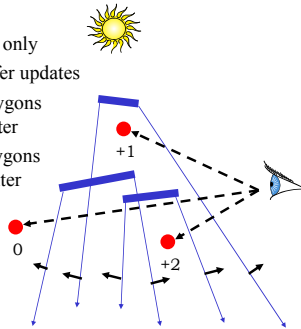
- Shoot a ray from the eye to the visible point
- Increment/decrement a counter each time we intersect a shadow volume polygon (check z buffer)
- If the counter  $\neq 0$ , the point is in shadow



MIT EECS 6.837, Durand and Cutler

## Shadow Volumes w/ the Stencil Buffer

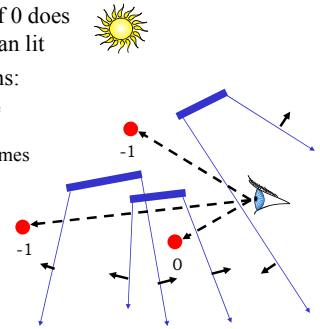
- Initialize stencil buffer to 0
- Draw scene with ambient light only
- Turn off frame buffer & z-buffer updates
- Draw front-facing shadow polygons  
If z-pass  $\rightarrow$  increment counter
- Draw back-facing shadow polygons  
If z-pass  $\rightarrow$  decrement counter
- Turn on frame buffer updates
- Turn on lighting and redraw pixels with counter = 0



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## If the Eye is in Shadow...

- ... then a counter of 0 does not necessarily mean lit
- 3 Possible Solutions:
  - Explicitly test eye point with respect to all shadow volumes
  - Clip the shadow volumes to the view frustum
  - "Z-Fail" shadow volumes

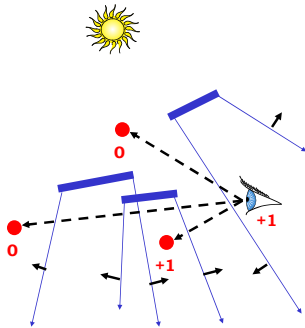


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## 1. Test Eye with Respect to Volumes

- Adjust initial counter value

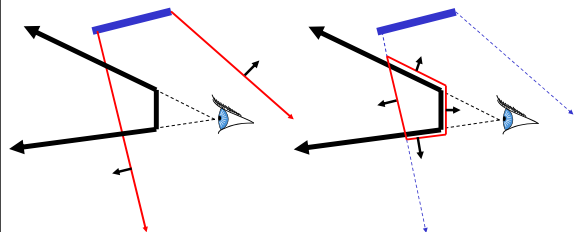
*Expensive*



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## 2. Clip the Shadow Volumes

- Clip the shadow volumes to the view frustum and include these new polygons
- Messy CSG*



MIT EECS 6.837, Durand and Cutler

### 3. "Z-Fail" Shadow Volumes

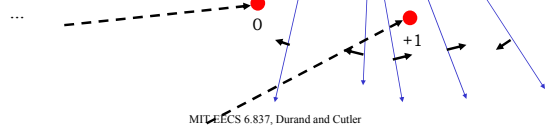
Start at infinity

Draw front-facing shadow polygons

If z-fail, decrement counter

Draw back-facing shadow polygons

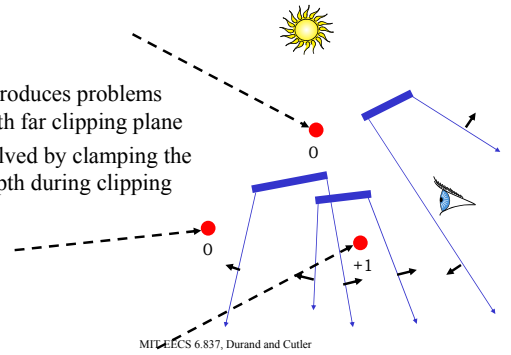
If z-fail, increment counter



MIT EECS 6.837, Durand and Cutler

### 3. "Z-Fail" Shadow Volumes

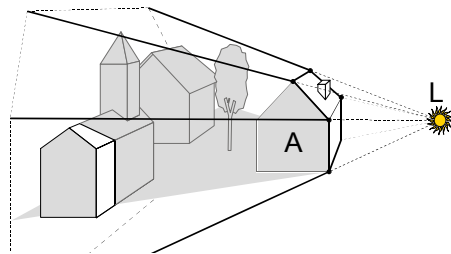
- Introduces problems with far clipping plane
- Solved by clamping the depth during clipping



MIT EECS 6.837, Durand and Cutler

### Optimizing Shadow Volumes

- Use silhouette edges only (edge where a back-facing & front-facing polygon meet)



MIT EECS 6.837, Durand and Cutler

### Limitations of Shadow Volumes

- Introduces a lot of new geometry
- Expensive to rasterize long skinny triangles
- Limited precision of stencil buffer (counters)
  - for a really complex scene/object, the counter can overflow
- Objects must be watertight to use silhouette trick
- Rasterization of polygons sharing an edge must not overlap & must not have gap

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### Questions?

- From last year's quiz: Check the boxes to indicate the features & limitations of each technique

Features / Limitations	Planar Fake Shadows	Projective Texture Shadows	Shadow Maps	Shadow Volumes	Ray Casting Shadows
Allows objects to cast shadows on themselves (self shadowing)	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
Permits shadows on arbitrary surfaces (i.e. curved)	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
Renders geometry from the viewpoint of the light	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
Generates extra geometric primitives	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
Limited resolution of intermediate representation can result in jaggie shadow artifacts	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

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### Next Time:

Global Illumination:  
Radiosity & The  
Rendering Equation

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