

Lecture 5 --- 6.837 Fall '00

lineDDA() Demonstration

Draw a line by clicking and dragging on the pixel grid shown with the left mouse button. An ideal line is displayed until the left button is released. Upon release a discrete approximation of the line is drawn on the display grid using the lineDDA() method described in the previous slide. An ideal line is then overlaid for comparison.

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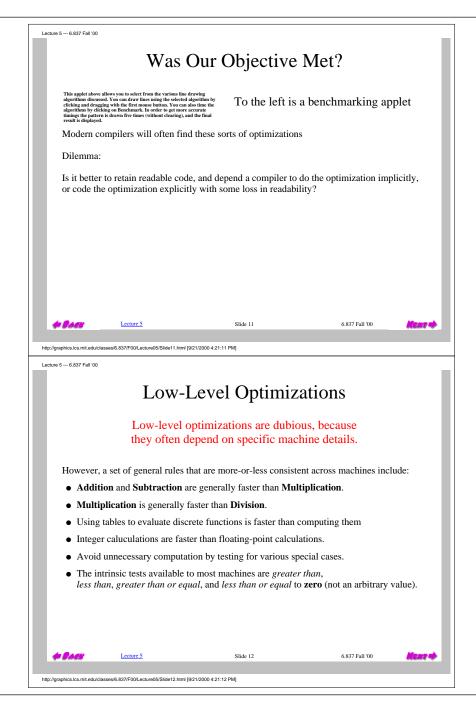
The *lineDDA()* method:

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You should not see any difference in

the lines generated by this method and the lineImproved() method mentioned previously.

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Applications of Low-level Optimizations

Notice that the slope is always rational (a ratio of two integers).

$$m = (y1 - y0) / (x1 - x0)$$

Note that the incremental part of the algorithm never generates a new y that is more than one unit away from the old one (because the slope is always less than one)

$$y_{i+1} = y_i + m$$

Thus, if we maintained the only the only fractional part of y we could still draw a line by noting when this fraction exceeded one. If we initialize fraction with 0.5, then we will also handle the rounding correctly as in our DDA routine.

fraction += m;
if (fraction >= 1) {
$$y = y + 1$$
; fraction -= 1; }



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More Low-level Optimizations

Note that y is now an integer.

Can we represent the fraction as an integer?

After we draw the first pixel (which happens outside our main loop) the correct fraction is:

fraction =
$$1/2 + dy/dx$$

If we scale the fraction by 2*dx the following expression results:

$$scaledFraction = dx + 2*dy$$

and the incremental update becomes:

scaledFraction +=
$$2*dy$$
 // $2*dx*(dy/dx)$

and our test must be modified to reflect the new scaling



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More Low-level Optimizations

This test can be made against a value of zero if the inital value of scaledFraction has 2*dx subtracted from it. Giving, outside the loop:

OffsetScaledFraction = dx + 2*dy - 2*dx = 2*dy - dx and the inner loop becomes

```
OffsetScaledFraction += 2*dy
if (OffsetScaledFraction >= 0) {
   y = y + 1;
   fraction -= 2*dx;
}
```

We might as well double the values of dy and dx (this can be accomplished with either an add or a shift outside the loop).



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The resulting method is known as Bresenham's line drawing algorithm

```
public void lineBresenham(int x0, int y0, int x1, int y1, Color color) {
     int pix = color.getRGB();
int dy = y1 - y0;
int dx = x1 - x0;
     if (dy < 0) (dy = -dy; stepy = -1;) else \{stepy = 1;\} if (dx < 0) (dx = -dx; stepx = -1;) else \{stepx = 1;\}
     raster.setPixel(pix, x0, y0);
     if (dx > dy) {
   int fraction = dy - (dx >> 1);
                                                                       // same as 2*dy - dx
          while (x0 != x1) {
                    (fraction >= 0) {
  y0 += stepy;
  fraction -= dx;
                                                                      // same as fraction -= 2*dx
                                                                       // same as fraction -= 2*dy
                raster.setPixel(pix, x0, y0);
           while (y0 != y1) {
                     x0 += stepx;
fraction -= dy;
                y0 += stepy;
                raster.setPixel(pix, x0, v0);
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```

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