

BuildIt: A Type-Based Multi-stage Programming Framework for Code Generation in C++

Ajay Brahmakshatriya CSAIL, MIT Cambridge, USA ajaybr@mit.edu Saman Amarasinghe CSAIL, MIT Cambridge, USA saman@csail.mit.edu

Abstract—The simplest implementation of a domain-specific language is to embed it in an existing language using operator overloading. This way, the DSL can inherit parsing, syntax and type checking, error handling, and the toolchain of debuggers and IDEs from the host language. A natural host language choice for most high-performance DSLs is the de-facto highperformance language, C++. However, DSL designers quickly run into the problem of not being able to extract control flows due to a lack of introspection in C++ and have to resort to special functions with lambdas to represent loops and conditionals. This approach introduces unnecessary syntax and does not capture the side effects of updates inside the lambdas in a safe way. We present BuildIt, a type-based multi-stage execution framework that solves this problem by extracting all control flow operators like if-then-else conditionals and for and while loops using a pure library approach. BuildIt achieves this by repeated execution of the program to explore all control flow paths and construct the AST piece by piece. We show that BuildIt can do this without exponential blow-up in terms of output size and execution time.

We apply BuildIt's staging capabilities to the state-of-the-art tensor compiler TACO to generate low-level IR for custom-level formats. Thus, BuildIt offers a way to get both generalization and programmability for the user while generating specialized and efficient code. We also demonstrate that BuildIt can generate rich control-flow from relatively simple code by using it to stage an interpreter for an esoteric language.

BuildIt changes the way we think about multi-staging as a problem by reducing the PL complexity of a supposedly harder problem requiring features like introspection or specialized compiler support to a set of common features found in most languages.

Index Terms—multi-stage programming, domain-specific languages, code generation, meta-programming

I. INTRODUCTION

Multi-stage programming or generative programming has many applications, ranging from efficient execution for deep neural network models and serving dynamic websites to generating efficient code for applications in specific scientific domains. Multi-stage programming provides a way of getting generality and simplicity of programming while maintaining high performance and specialization [1]–[4]. Domain-specific languages like TACO [5], Tensorflow [6], Halide [7] and GraphIt [8], [9] are simply two-stage programming frameworks in which the first stage is the high-level DSL specification, and

BuildIt is available open-source under the MIT license at https://github.com/ BuildIt-lang/buildit. the second stage is the generated low-level efficient C++/CUDA code targeting CPU/GPUs. TensorFlow [6] extracts static and dynamic execution graphs from the input program to automatically calculate gradients for the neural network layers and to efficiently execute the networks when the inputs are available. In the most general sense, multi-stage programming has several stages in which the output of a particular stage is the code for the next stage. Figure 2 shows a comparison between traditional single-stage programming and multi-stage programming. Each stage can use a different programming language and different libraries and has its own set of inputs. For example, in dynamic websites, server-side languages like PHP and NodeJS produce HTML, JavaScript and CSS for second stage execution in the user's browser. One can think of traditional single-stage programming as a special case of multi-stage programming with one stage.

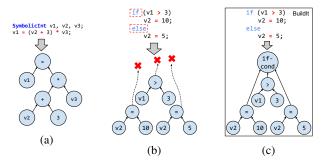


Fig. 1: a) Operators =, + and * (in red) overloaded for the new SymbolicIntType type (in blue) to create an AST for the expression. b) Shows similar ASTs created for the subexpressions, but there is no way to combine the three into an if-then-else because C++ does not support overloading control flow and lacks introspection. c) BuildIt is able to construct the full AST

Generating code for different stages can take multiple approaches. The user explicitly outputs as strings the code for the next stage (PHP outputting HTML) or uses a language like MetaOCaml [10] that has built-in support for multiple stages using a specialized compiler. We will discuss the pros and cons of each of these approaches in detail in Section II. One popular approach taken by many multi-stage programming frameworks, such as Tensorflow [6] or Halide [7], is to introduce a new type and use operator overloading and symbolic execution to extract the program representation for the next stage. Figure 1 a) shows how in an imperative and statically typed language like C++,

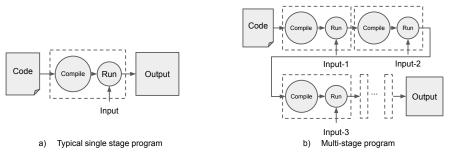


Fig. 2: Comparison between a) traditional single-stage programming and b) multi-stage/generative programming. Notice each stage in b) has its own compilation and execution step with its own set of inputs.

the addition, multiplication, and assignment operators can be overloaded to create the abstract syntax tree (AST) for the next stage. This approach quickly runs into a major problem that data-dependent control flow cannot be extracted because C++ does not support overloading conditions and loops, as shown in the second example of Figure 1 b). With the lack of introspection in C++, it is practically impossible to get a similar effect without relying on compiler changes. Since C++ is used in code generation and lowering phases of many high-performance language backends, looking for alternatives to introspection is important. In addition, using compiler modification approaches generally compromises portability and increases the complexity of codebases.

We present BuildIt, a type-based multi-stage programming framework for C++ that solves this exact problem. BuildIt uses a purely library-based approach that doesn't require any compiler changes and is capable of extracting ASTs for the next stage from the input code with all the rich data-dependent structured control flow elements, like if-then-else conditions, while and for loops and recursion. BuildIt makes a key observation that the input program can be executed several times to explore different control flow paths in the program. This is combined with traditional operator overloading and symbolic execution to get the entire AST for the next stages program. BuildIt further makes the extraction process tractable and efficient by applying novel static tags and known techniques, like memoization.

Unlike introspective solutions, BuildIt does not have a full view of the program. Instead, it examines the program through the narrow window of the calls to the overloaded operators. This is analogous to a person trying to navigate a maze. They see only one small part of the maze at a time, but by carefully recording observations and leaving markers on paths explored, the person can successfully navigate the maze. BuildIt also uses memoization and early merging of control flow paths to reduce the extraction complexity from exponential to polynomial in the number of branches.

A. Type-Based Multi-stage Programming

Different multi-stage programming frameworks further vary by the way the binding times of subexpressions and variables are decided. The binding time means the stage in which a particular subexpression is evaluated with concrete values instead of just producing the code for the next stage. For frameworks that use different languages for each stage, the binding times are decided by the language in which the expression is written. BuildIt is a type-based multi-stage programming framework, meaning the types of the variables and subexpressions decide in which stage they will be bound. Since C++ is a statically typed language, the declared types decide the binding times. BuildIt provides different types for each stage, and these will be explained in detail in Section III.

B. Rethinking Meta-programming

Multi-stage programming has been studied extensively in the literature, with an understanding that multi-stage programming requires specialized language constructs to be implemented in the language with a compiler([4], [11]) or the existence of features like introspection in the host language([6], [12]–[14]).

BuildIt has both theoretical and practical implications in this field. The ideas presented in this paper have foundational implications for our understanding of PL complexity. Most features in languages can be simplified to a composition of control flow (like loops and conditionals) and basic binary and unary operations. However, to-date staging requires additional PL complexity, such as access to program AST or specialized constructs and compiler support. BuildIt shows that we can reduce the complexity of a supposedly harder problem to a simpler problem. With this, we try to change the way we think about staging as a class of problems. By implementing our framework in C++, we show that staging is in fact a subclass of a class of problems that require only basic operations to implement. In addition, this has several practical implications. Because we rely on only standard C++ constructs, our implementation is portable across platforms and compilers. C++ is also one of the most commonly used languages for highperformance applications, and domain experts already have familiarity with the language and the optimizations it requires. This is important because staging was either not possible or very difficult to use with C++. Although our implementation is specific to C++, the ideas presented can also be applied to other languages since BuildIt relies only on the common features found in most programming languages.

This paper makes the following contributions:

• BuildIt combines operator overloading and symbolic execution with repeated executions to explore all control flow paths and is the first framework that can extract

the AST with all loops and conditionals for multi-stage execution in C++.

- BuildIt does not require a separate syntax or specialized constructs for control flow like if-then-else and for and while loops. This makes it extremely easy to change the binding times of subexpressions without a lot of code rewriting.
- BuildIt is the first framework for imperative languages to allow side-effects on unstaged variables inside conditions on staged variables. This allows rich patterns to be extracted and generated. BuildIt is implemented as a library by overloading basic binary and unary operators and does not require any compiler changes, making BuildIt quite portable and lightweight.
- We also show how generative multi-stage programming can be applied to code generation for DSLs, thus offering generalizability and programmability while providing specialization and efficient code generation.
- Finally, BuildIt changes the way we think about multistaging as a problem by reducing the complexity of a supposedly harder problem to a set of basic PL features.

The rest of the paper is structured as described below:

- Section II discusses different approaches to extracting the AST of programs.
- Section III introduces the BuildIt programming model and describes the static<T> and dyn<T> types.
- Section IV describes in detail the AST extraction process in BuildIt and how control flow is handled with repeated execution.
- Section V shows two case studies in which BuildIt can be applied and how BuildIt significantly improves the programmability while providing specialization.
- Section VI talks about different related works in generative and multi-stage programming and the difference in the approaches they take.

II. BACKGROUND

This section discusses different AST extraction methodologies and the pros and cons of each approach. We then describe the approach taken by BuildIt and how it approaches some of the relevant problems.

A. Text-Based Generative Programming

Text-based multi-staging requires the user to print the code for the next stage, making it the easiest to understand and implement. This approach is taken by server-side languages in webservers like PHP and NodeJS. Figure 3 shows a loop written in PHP that produces a list of items in the generated HTML. Notice how PHP treats the code for the HTML stage as just a string and echoes it to the standard output.

This approach does not require any special compiler or library support as long as the language natively supports strings. The output of the program is simply fed into the compiler for the next stage. The main limitation of the text-based approach is that it doesn't allow for any optimizations or type-checking of the generated code because the generated code is merely

<pre>1 <?php echo '';</pre>	1
<pre>2 for (\$i = 0; \$i < 3; \$i++)</pre>	2 Item 1
<pre>3 echo 'Item'.\$i.'';</pre>	3 >Item 2
4 echo '';	4 Item 3
5 ?>	5

Fig. 3: The PHP code on the left executes on the webserver to produce the HTML code on the right to be executed in the user's browser. Notice how the PHP code treats the HTML as strings.

1
<pre>2 for (x=0; x<20; x++)</pre>
<pre>3 arr[x] = val;</pre>
4
5 for (x=0; x<10; x++)
<pre>6 arr[x] = val;</pre>
7

Fig. 4: The C++ template code on the left defines a function where the M value is a template argument. On the right, the different versions of the same function are generated for different template arguments.

a string. The code would need to be parsed and analyzed before any meaningful transformations or optimizations could be applied. In addition, IDE/debugger support is lacking until the generated code is compiled/run.

B. Compiler-Based with New Language Syntax

This approach adds a specialized syntax for the code of each stage and supports its execution in different stages with a help of a specialized compiler/interpreter. A common example of such a technique is the C++ template language, in which the templates use a different syntax from the rest of the C++ code and are handled specifically by the compiler. Figure 4 shows how templated functions (or classes) can be instantiated with different arguments to produce different code to be compiled.

With a compiler-based technique, many rich features like optimizations, type checking, and debugger support can be integrated into the compiler for all stages. However, the main disadvantage is that a specialized compiler needs to be implemented and maintained instead of maintaining just a library. In addition, the user must learn and adapt to a new syntax for each stage.

Both of the techniques above, text-based and specialized syntax-based, suffer from another common drawback. Because the code for each of the stages looks very different, it is very difficult to move code between different stages. Generally, moving code between stages requires rewriting the entire program, which greatly hampers the productivity of the user.

C. Operator Overloading and Special Functions for Control-Flow

One of the most promising approaches for seamless multistage programming is to use operator overloading with symbolic execution, as mentioned in Section I. To handle control flow, the framework can add through a library specialized operators that take in lambdas and subexpressions. This approach is used in the first version of TensorFlow to construct dynamic graphs, as shown in Figure 5.

This approach solves most of the limitations mentioned above, but it still uses a specialized syntax for control flow elements. For this reason, it is difficult to move code between

1 import tensorflow as tf	$1z = a \star b$
$_2 z = a \star b$	2 if (x < y):
3 result = tf.cond(x < y)	3 result = $x + z$
<pre>4 lambda: x + z,</pre>	4 else
5 lambda: v ** 2) 5 result = y ** 2

Fig. 5: A sample if-then-else condition written in TensorFlow. Notice that the condition to be checked and the body of the then and else branches are supplied as lambdas. In addition, the operators like <and + are overloaded for the type tf.Tensor. The figure on the right shows what the constructed condition would look like.

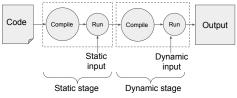


Fig. 6: To explain the programming model, we first describe a simple, two-stage execution case and then generalize it to arbitrarily many stages in Section IV.

two stages. This approach also doesn't allow side effects on non-staged variables inside control flow based on staged variables. We will see how this is relevant in Section V and what limitations it presents.

BuildIt solves all of the above mentioned problems by using the same general C++ syntax for handling control flow using only a library. Additionally, BuildIt allows seamless updates to stage n variables inside conditionals and loops on stage n+1. As mentioned before, BuildIt executes the program repeatedly to extract all control flow paths. Thus, the updates to the unstaged variables are limited to only the cases in which the branch is taken during the next stage execution.

III. PROGRAMMING MODEL

In this section, we describe in detail the programming model for BuildIt programs. This includes the two new types static<T> and dyn<T> and the constraints which all BuildIt programs must satisfy.

A. A Library-Based Approach

As mentioned before in Section I, BuildIt takes a purely library approach. This means users can start using BuildIt by including the BuildIt headers that define the new types and the overloaded operators and linking against the runtime library that has the AST extraction and code generation implementation.

B. Multi-stage to Two Stage Relaxation

We will introduce the programming model by first describing a two-stage BuildIt program. We do this to make it easy to understand the terminology and how the extraction process works. We then generalize the programming model to arbitrary many stages in Section IV. As shown in Figure 6, we call the two stages the static stage and the dynamic stage. We call the inputs taken by these stages static inputs and dynamic inputs.

C. Type-Based Programming Model

As mentioned before, BuildIt is a type-based programming framework. This means that BuildIt uses declared types of the variables and subexpressions to decide binding times. We explain below the two new types BuildIt introduces, static<T> and dyn<T>:

```
int power(int base, int exponent) {
    int res = 1, x = base;
    while (exponent > 0) {
        if (exponent % 2 == 1)
            res = res * x;
            x = x * x;
            exponent = exponent / 2;
        }
        return res;
    }
}
```

10 }

Fig. 7: A typical implementation of the power function that calculates baseexponent using repeated squaring

L	dyn < int > x = 0;	1	<pre>int var1 = 0;</pre>
2	dyn <long> y = 0;</long>	2	<pre>long var2 = 0;</pre>
3	<pre>static<int> z = 10;</int></pre>	3	/*No trace of z*/
1	if $(x > z)$	4	if (var1 > 10)
5	x = x + y;	5	<pre>var1 = var1 + var2;</pre>
5	else	6	else
7	$x = x \star y;$	7	<pre>var1 = var1 * var2;</pre>

Fig. 8: The BuildIt code shown in the left executes in the static stage to produce the code shown on the right, to be executed in the dynamic stage. Notice how dyn < int> produces variables and expressions of type int in the generated code. The conditions on expressions of type dyn < T> produce the same conditions in the generated program.

1) Static Type: static<T>: A user can declare variables of type static<T> (where T is any C++ primitive type) to indicate variables and expressions that should be evaluated in the static stage. static<T> variables have concrete values of type T during the static stage. Control flow dependent only on expressions of type static<T>, is resolved during the static stage and does not produce any conditionals or loops in the generated code. static<T> currently supports wrapping only primitive C++ types that have a comparison operator defined.

2) Dynamic Type: dyn<T>: The user can declare variables of type dyn<T> (where T is any type) to indicate variables and expressions that should be executed in the dynamic stage. An expression written using variables of type dyn<T> does not have concrete values during the static stage. Instead, it produces the exact same expression with type T, to be evaluated during the dynamic stage. For example, the BuildIt code shown in the left of Figure 8 produces code shown in the right of Figure 8 for dynamic stage evaluation. Notice how declarations of type dyn<int> produce declarations of type int. We can also see in the figure that the expressions of type static<int> are completely evaluated in the static stage and have their values appear as int constants in the generated code. Moreover, dyn<T> variables can be used inside the boolean expressions for conditions and loops to produce control-flow elements in the generated code for the dynamic stage.

3) BuildIt Programs: BuildIt programs look like any other C++ program except that it uses two extra types to decide the binding times of all expressions. BuildIt does not use any new syntax or special function calls for control flow elements like if-then-else conditions, for loops, or while loops. This makes migrating existing code to different variations of multi-stage code easy. For example, Figure 7 shows a single-stage implementation of the power function. This function takes two inputs, base and exponent of type int and returns base^{exponent} using repeated squaring.

```
idyn<int> power(dyn<int> int power_15(int base) {
    base, static<int> exp) { 2 int res = 1;
2
   dyn<int> x=base, res=1;
                               3
                                  int x = base;
   while (exp > 0) {
                                  res = res * x;
                               4
4
    if (exp % 2 == 1)
                               5
                                  x = x * x;
5
      res = res * x;
                                  res = res * x;
6
                               6
    x = x \star x;
                                  x = x * x;
                               7
     exp = exp / 2;
                                  res = res * x;
9
   }
                               9
                                  . . .
10
   return res;
                                  return res;
                               10
11 }
                               11 }
```

Fig. 9: The power function where the exponent is bound in the static stage and the base is bound during the dynamic stage. On the right is the generated code when the static input (exponent) is supplied 15.

```
i dyn<int> power(static<int>
                                int power_5(int exp) {
     base, dyn<int> exp) {
                                2 int res = 1;
2
   dyn<int> res=1, x=base;
                                    int x = 5;
3
                                3
   while (exp > 0) {
                                 4
                                    while (exp > 0) {
     if (exp % 2 == 1)
                                     if (exp % 2 == 1)
                                 5
      res = res * x;
                                      res = res * x;
6
                                 6
                                     x = x * x;
     x = x \star x;
                                 7
     exp = exp / 2;
                                     exp = exp / 2;
8
                                 8
                                    }
9
   }
                                 9
10
   return res;
                                10
                                    return res;
11 }
                                11 }
```

Fig. 10: The power function where the base is bound in the static stage and the exponent is bound during the dynamic stage. On the right is the generated code when the static input (base) is set as 5.

Figure 9 shows how the program can be specialized for a particular exponent in BuildIt by declaring the exponent as static<int> and the base as dyn<int>. The code on the right shows the generated code for exponent specialized as 15. Since all of the loops and conditions are based on static<T> expressions, they are evaluated away to produce straight-line code. Figure 10 shows the same function specialized for a particular base by declaring the base as static<int> and the exponent as dyn<int>. The figure on the right shows the code generated for the base specialized as 5. Since the loop is now based on a dyn<T> expression, it is present in the output code.

All BuildIt programs must use static<T> and dyn<T> to declare variables and write expressions. In addition, BuildIt programs can use expressions that are not static<T> or dyn<T>, but they can be accessed solely in read-only mode. These variables would exhibit the same behavior as static<T> and would be completely evaluated in the static stage.

IV. AST EXTRACTION METHODOLOGY

In this section, we describe in detail the methodology BuildIt follows to extract the AST for the program to be executed in the dynamic stage.

A. Handling Static Variables

Variables of type static<T> are simply wrappers around variables of type T and mimic the behavior of the enclosed type. An implicit conversion operator is defined to expose the value of the wrapped type. Thus, we can perform all of the operations on static<T> that are valid for T, including assignment and binary and unary operators, using them in if-then-else and loops without any change.

```
1 builder_context context;
2 //non BuildIt type read only vars here
3 const int iter = atoi(argv[2]);
4 auto ast = context.extract([=] {
5 for (dyn<int> x = 0; x < iter; x++)
6 ...
7 });
8 ast->dump(std::cout, 0);
```

Fig. 11: Example showing how to wrap BuildIt code inside a lambda and pass it to a Builder Context object. The code can also be wrapped inside a function that takes arguments.

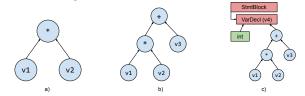


Fig. 12: Step-by-step construction of expression trees. Notice that the expressions are shown in blue, statements are show in red, and types are show in green. The VarDecl AST node has int as a type attached to it.

B. Extracting Straight-Line Code

Like other works, BuildIt uses operator overloading and symbolic execution to extract information about the operators and variable declarations for dyn<T> expressions and variables. Using operator overloading preserves the syntax for these operators while hiding the complexity of creating the expressions from the user. The programmer wraps the code to be extracted in a function or a lambda and passes it to a Builder Context object. This allows BuildIt to execute the code repeatedly to explore all control flow paths. Figure 11 shows an example of how the Builder Context object is invoked with the lambda.

BuildIt overloads all of the binary and unary operators for expressions of type dyn < T> to create appropriate AST nodes and return a reference to the created nodes. These AST references are further combined to create more AST nodes and to construct the AST for the entire expression. For example, suppose we have the expression v1 * v2 + v3 where v1, v2and v3 are of type dyn < T>. Since usual C++ precedence rules follow, the subexpression v1 * v2 is evaluated first to create an AST node for the * operator, as shown in Figure 12 a). When the + operator is evaluated next, BuildIt creates a new AST node for the + operator and nests the previously created AST as a subexpression, as show in Figure 12 b).

All of the constructors for the variables of type dyn<T> are overloaded to create variable declaration statements in the AST being constructed. For example, suppose we have a variable declaration of type dyn<int> as dyn<int> v4 = v1 * v2 + v3;. First, the AST for v1 * v2 + v3 is created, as explained as above. The copy constructor for v4 is called with the AST for v1 * v2 + v3 as the parameter. This creates a variable declaration statement AST node and adds it to the AST being constructed, as shown in Figure 12 c).

The other type of statement in straight-line code is an expression statement, and BuildIt captures this with some bookkeeping to identify the end of a statement. The Builder Context object holds an ordered list of uncommitted expressions. Whenever an AST node for an expression is created, it is

Fig. 13: Sample straight-line code to be extracted. Overloaded operators are in red, and one possible execution order for the operators is show above each of them.

1) UL: ["v2 v3"1 1) UL: ["v2 * v3", "v4 / v5"]3) UL: ["v2 * v3 + v4 / v5"]4) UL: ["v1 = v2 * v3 + v4v5"] v5", "v7 && v5", "v6 = 5) UL: ["v1 = v2 * v3 + v4 88 v8"] 6) UL: ["v1 = v2]v3 + v4 v7 && v8"1 * 7) UL: []

Fig. 14: State of the Uncommitted List (UL) after each call to overloaded operator in Figure 13.

also added to this list and is removed when it is used as a child in another expression. Thus, this list holds only those expressions that do not have a parent. Whenever the execution reaches an obvious end of a statement (for example, a variable declaration or the end of the program), all of the expressions in the uncommitted list are converted to expression statements and are added to the AST. Figure 13 and Figure 14 show an example of a straight-line code, the step-by-step execution, and the the uncommitted list after call to each overloaded operator.

C. Extracting if-then-else Conditions

In this section, we introduce our novel repeated execution strategy to explore all control flow paths in the program. This technique builds on the techniques for extracting straight-line code explained above.

Before we can extract the conditions, we must detect that we have encountered a condition. A condition on expression of type dyn<T> looks like if (expr) where expr is of dyn<T>. We overload the explicit cast operator from dyn<T> to bool, which is requested when an expression of type dyn<T> is used inside a condition. At this point, we must determine how the program would proceed in both cases if the expression returned true or false in the dynamic stage.

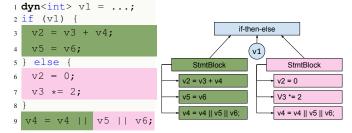


Fig. 15: The ASTs constructed for the if-then-else. The block in green is extracted by the fork that returned true. The block in red is extracted by the fork that returned false. The two ASTs are combined to create an if-then-else.

We continue by remembering this expression inside the if condition. We then logically fork the execution at this point by creating two new, identical Builder Context objects. These objects restart the execution, following the exact same path until they reach the conditional. At this point, they take separate paths by returning true and false as a result of the cast to bool operator respectively. Both of the forks then continue execution and produce two different but complete ASTs for the rest of the program. These two ASTs are the straight-line paths the program would take in the dynamic stage based on whether the expression inside the if() evaluates to true or false. To create a single program that has this same behavior, we finally merge the two ASTs by adding an if-then-else node in the AST and adding the two ASTs as the sub-tree inside the then and else branch, respectively.

Figure 15 shows a simple if condition on the expression v1. The code in green shows the code executed by the fork that returned true. The code in red shows the code executed by the fork that returned false. The last line is executed by both of the executions. Finally, Figure 15 shows the two ASTs produced by the two executions (in green and red).

D. Need for Static Tags

The conditions extracted from the process described above is correct but has an obvious flaw. In Figure 15, we can see that the statements that appear after the conditions (v4 = v4 | | v5 | | v6;) are duplicated on both sides of the if-then-else. This leads to exponential blowup in the size of generated code with respect to the number of if conditions. We must uniquely identify statements in the generated ASTs across executions so that we can merge those from the then and else branches. To achieve this, we introduce static tags. The static tag comprises two parts: the stack trace (array of RIPs) at the point when the statement was created and the state of all static variables at the point the statement was created. To facilitate this, the Builder Context object maintains a reference of all currently alive static variables. When the overloaded operators on dyn<T> are called, we create a static tag from the stack trace and snapshots of the static variables and attach it to the generated expression.

We assert that if two statements have this same 2-tuple (static tag), the execution following those will be identical and will thus produce the same AST. It is obvious why this is true. Recollect from Section III that a BuildIt program can use three types of values: dyn<T>, static<T>, and other types in read-only mode. The execution of a program depends on its current state. Since the tags for the two statements are the same, the instruction pointers (and the return addresses on the stack) are all the same. Furthermore, all of the values the program can access are also the same because the static tag also includes a snapshot of all of the live static<T> variables. In addition, the variables of non-BuildIt types will be the same because they are read-only for the duration of the BuildIt program. Thus, the two programs at this point are indistinguishable and will run in the same way to produce the same AST.

We use this property to trim the common suffix of the ASTs generated in the if-then-else. We begin from the end of the two statement blocks and keep removing statements as long as they have the same static tag. Once we find the first pair of statements that do not have the same static tag, we stop. After this transformation, the AST for the above example will look like that in Figure 16

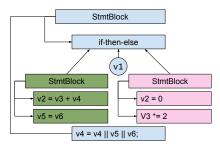


Fig. 16: The AST for the code in Figure 15 after trimming using static tags

E. Improving Extraction Complexity

The above trimming transformation reduces the output AST from exponential in size to linear in size, but the process of extraction still takes exponential time because we delay the trimming process after the entire AST has been extracted. If we can identify merge points between two executions eagerly, we can avoid traversing an exponential number of paths.

Once again, we can use static tags and apply classic memoization on the extracted AST to avoid doing redundant work. The Builder Context object maintains a map that maps static tags to the AST produced from that point onward in the program. This map is updated whenever the Builder Context object finishes the execution of the program for all the static tags seen in the program. Before creating any statement, we check if the map already has this static tag; if it does, we directly copy over the remaining AST from the map instead of constructing it again. This optimization is valid because, as we have shown before, when two statements have the same static tag, the execution from that point onward will be exactly the same and will produce the same AST.

Let us give an intuition of how this optimization ensures that the AST can be extracted in polynomial time. Since the output program size is linear in the number of sequential if-then-else conditions, the total number of unique tags and thus the total number of forks in the execution in the program are also linear. If n+1 forks occur, at least two of them will occur at the same static tag, which the memoization would avoid. With n forks, we are guaranteed to have at most 2n executions. Finally, each execution produces at most n statements (each execution is a straight line AST). Thus, a total of $O(n^2)$ statement are created. Creating a statement requires at most a linear amount of work, bringing the worstcase execution time of the extraction process to $O(n^3)$.

To demonstrate this polynomiality, we observe the program shown in Figure 17. The outer loop will completely execute iter number of times in the static stage to produce a number of conditions. We run this program with BuildIt with increasing values of iter and record the number of Builder Context objects created by the program. We record these numbers with and without the memoization optimization. Table 18 shows the results of this experiment. We can clearly see that the number of executions is linear with memoization and exponential without memoization.

```
1 // param: iter(int)
2 dvn<int> a:
3 static<int> i;
4 for(i=0; i<iter; i++) {
   if (a) {
       = a +
             i;
     а
   } else {
     a
       = a
           -
             i;
   }
9
10 }
```

Fig. 17: Code that generates iter number of if-then-else for the dynamic stage

iter	with mem-Z		with	out mem-Z
	count	time(sec)	count	time(sec)
1	3	0.01	3	0.01
5	11	0.01	63	0.01
10	21	0.01	2047	0.11
15	31	0.01	65535	2.99
18	37	0.01	524287	23.79
19	39	0.01	1048575	48.24
20	41	0.01	2097151	96.45
iter	2 * iter + 1		2 ^{iter+1} - 1	

Fig. 18: Number of Builder Context objects created with increasing value of iter for Figure 17 and the corresponding execution times

F. Extracting Loops

After straight-line code and if-then-else conditionals, all that remain are while and for loops. Both while and for loops appear with a condition on an expression of type dyn<T>. If we try to handle loops just like we handled if-then-else, by forking every time we see the condition, we will get stuck in an infinite loop in the static stage. For a simple while loop, the execution that takes the true path will always come back to the beginning of the loop and will spawn more executions.

Figure 19 shows a simple while loop with a dyn<T> expression as a condition. Figure 20 shows the code that we would extract if we naively apply the technique above. To fix this, we use the static tags again. Apart from the shared map of static tags for memoization, we also maintain a list of visited static tags private to each Builder Context object. Every time we insert a statement in the statement block, we insert the static tag in this list. Before inserting a new statement, we scan this list to check if the static tag has been visited before. If we find the static tag in the list, we insert a goto statement to the original statement and terminate the execution. We have already shown that if two statements have the same static tag, they will have the same execution after that point. Thus, it is correct to add only a goto to the previous statement instead of repeating the execution. Figure 21 shows the code we would generate with this technique.

Notice that the technique described above does not stop the execution when there is a loop on an iterator of type

<pre>1 dyn<int> iter = 0;</int></pre>	<pre>int iter = 0;</pre>
2 // Condition based on	2 if (iter < 10) {
3 // dyn <int> expression</int>	3 iter = iter + 1;
4 while (iter < 10) {	4
<pre>5 iter = iter + 1;</pre>	5
6 }	6 }
7	7 }

Fig. 19: A simple while loop with a Fig. 20: The code generated if condition based on an expression of we naively apply the fork and retype dyn<T> execute strategy

```
int iter = 0;
2 label:
3 if (iter < 10) {
4 iter = iter + 1;
5 goto label1;
6 }
7 ...
```

Fig. 21: The generated code with the static tag list technique has a if and goto

static<T>. This is because every time the execution reaches the beginning of the loop, the static tag is different. This is correct and important because we want all iterations of purely static loops to be executed in the static stage.

G. Extracting Recursive Functions

Special care must be taken while handling recursive functions that call themselves based purely on a dynamic condition. Because BuildIt explores all control flow paths, the function will end up calling itself infinitely. The condition to identify such a recursive call is similar to loop. Instead of looking for an exact match of tags, BuildIt seeks a series of stack frames in the static tags that are repeated exactly. In addition, BuildIt ensures that all the static<T> variables defined in these frames have the exact same value. When such a condition is detected, BuildIt halts the execution and inserts a recursive call to the function in the extracted AST.

H. Post Extraction Processing

In this section, we discuss some of the transformation and canonicalization passes that run on the extracted AST before code generation. BuildIt provides rich visitor patterns to easily analyze and transform AST nodes.

1) While Loop Detector: Loop detection by itself is a well-studied problem, and a variety of techniques have been proposed [15]–[18]. We apply a control flow analysis simplified from previous techniques to canonicalize all if-then-else and goto loops into equivalent while loops. The transformation pass finds all the labels in the generated AST and then identifies the last statement that jumps back to this loop. All the statements from the label to this statement become the body of the while loop. Additionally, the pass explores all paths inside the body and inserts continue or break at the end, depending on where the control flow goes. Finally, the pass attaches an appropriate condition to the created while loop by matching a pattern on the if-then-else.

2) For Loop Detector: A final pass checks all the while loops in the AST. If a loop has a variable declared just before it, that variable is checked in the while loop condition, and the same variable is updated at the end of every control flow path inside the loop that loops back, this loop is converted into a for loop with an initialization, condition, and update.

All the aforementioned passes do not change the behavior of the extracted AST and thus are correct by construction.

3) C++ Code Generation: Finally, with the BuildIt framework, we provide a C++ code generator that can be invoked by a user to generate C++ code from the extracted AST. This makes it easy for the user to compile the code for the next stage and execute it. This C++ code generator is optional, and the user can use the visitor library in BuildIt to write their own code generator for different languages, including LLVM IR and other compiler intermediate representations for optimization.

I. From Two Stages to Multiple Stages

To support true multi-staging (as opposed to only two stages) in BuildIt, we allow the dyn<T> template to wrap around BuildIt types (static<T> and dyn<T>). With this, the user can declare variables of types like dyn<dyn<int>> or dyn<static<int>> or nest these types even more than twice to add more stages. The C++ code generator in the BuildIt framework can generate type declarations for the static<T> and dyn<T> variables. Thus, the code generated from the first stage can be immediately compiled and run again in the second stage to produce code for the third stage and so on. However, such wrapping is not required for static<T> because multiple static<T> can be collapsed into a single one.

With the nested template types dyn < T > and static < T >, the code seems to get complicated and we run into the same issues found in C++ templates. The key difference here is that the complexity of all these stages and templates is confined to the variable declaration. The actual code operating on these types looks **exactly** the same regardless of what stage it executes in. Not only does this make it easy to write code in multiple stages, but it also simplifies moving code between stages. The binding time of an expression or the stage in which it is actually evaluated can be changed by simply changing its declared type. This is much easier than dealing with traditional template metaprogramming in C++.

J. Dealing with Undefined Behavior and Dead Branches

During the course of execution, programs run into unexpected cases due to programming bugs, like divide by zero errors, out-of-bound accesses, or null pointer dereference. If the input program has any kind of undefined behaviors, any program that BuildIt generates is completely valid. However, BuildIt must strive not to introduce any new, undefined behaviors. This is tricky because BuildIt explores all possible branches in the program, some of which might be dead branches.

Figure 22 shows an example of one such case, in which a divide by zero is hidden under a dead branch. We have to be extremely careful with such cases in the code extraction process and in the generated code. We will divide the undefined behaviors into two categories.

1) Undefined Behavior on dyn < T > State: These kinds of errors happen when variables and expressions of type dyn < T >invoke undefined behavior. For example, dividing a dyn < int >variable by 0. These errors are easy to handle, because BuildIt in its static stage while exploring all of the static paths never evaluates any dyn < T > expressions. If a dyn < int > is divided by 0, we simply produce the same code. If this code happens to be on a dead branch like in Figure 22, this path is never taken, and the undefined behavior is not invoked. If this undefined behavior happens to be on a path that can be taken, then the input program is malformed, and any output is valid.

```
1 dyn<int> x = ...;
2 if (x > 100) {
3 if (x < 80) { // Dead branch
4 x = x / 0; // x cannot be < 80
5 } // if x > 100
6 }
```

Fig. 22: Code snippet showing how undefined behavior on a dyn < T> expression can be hidden behind a dead branch. BuildIt can potentially run into problems because it explores all of the branches.

2) Undefined Behavior on static<T> State: : These kinds of errors, as the name suggests, are invoked by the static<T> expressions that are actually evaluated in the static stage. These are trickier to handle if they are behind a dead branch that can never be taken dynamically because BuildIt executes all branches in the static stage. When BuildIt encounters any exception during the static stage, it halts the execution of the current context and simply inserts an abort(); in the generated dynamic stage code. This abort(); is inserted only in the path that invokes the undefined behavior. Again, if this branch is a dead branch, the path is never taken, and the abort(); is not executed. If the abort(); actually gets executed in the dynamic stage, the input program is malformed, and it is a valid behavior of the program to abort.

V. CASE STUDIES

In this section, we describe how we apply BuildIt for code generation to a real-world compiler, TACO [5]. We also discuss certain other examples, in which BuildIt's code specialization abilities are useful.

A. TACO Lowering

The Tensor Algebra COmpiler (TACO) is a fast, versatile library for tensor algebra that generates high-performance C++/CUDA code from high-level expressions in tensor-index notations by the means of a specialized compiler. TACO's performance is competitive with best-in-class, hand-optimized kernels in popular libraries while supporting far more tensor operations. Another recent work [19] extends TACO to allow users to implement custom-level formats to support different formats for the tensors.

To add a new level format, the user must implement lowering functions that generate code for operations on the level format. This requires the user to build the AST of the generated code by calling constructors of the IR classes and piecing them together. Figure 23 shows one such function implemented by the user for the compressed level format that generates code for adjusting the size of an array at runtime. Notice the call to the constructor for IfThenElse, Assign and other TACO IR nodes. The user can further specialize the generated code for scenarios by writing conditions based on compile-time parameters, as shown in Line 8.

Writing such code is typically difficult for domain experts who are not familiar with compiler techniques. Even for compiler experts, mixing runtime and compile-time conditions is not very intuitive and can be error-prone. We solve these problems by using BuildIt to enable easy code generation. We provide an abstract interface that users can implement for each

```
Stmt increaseSizeIfFull(Expr a, Expr size,
    Expr needed) {
2
3
   Stmt realloc, resize;
   if (mode.useLinearRescale) {
4
     realloc = Allocate(a, Add(size, mode.growth),
      true, size);
6
     resize = Assign(size, Add(size, mode.growth));
7
   } else {
    realloc = Allocate(a, Mul(size, 2), 1, size);
9
     resize = Assign(size, Mul(size, 2));
10
11
   }
12
13
   Stmt ifBody = Block({realloc, resize});
   return IfThenElse(Lte::make(size, needed), ifBody);
14
15 }
```

Fig. 23: Implementation of the $\verb"increaseSizeIfFull"$ helper function used by the level formats

```
void increaseSizeIfFull(dyn<int*> &array,
2 dyn<int> &size, dyn<int> needed) {
3 if (size <= needed) {</pre>
     if (mode.useLinearRescale) {
4
      array = realloc(array, size * 2);
5
      size = size * 2;
     } else {
      array = realloc(array, size + mode.growth);
8
      size = size + mode.growth;
9
10
     }
   }
11
12 }
```

Fig. 24: BuildIt implementation of the $\verb"increaseSizeIfFull"$ helper function

level format. Instead of writing code to generate the AST, they implement the level format like a library with BuildIt's dyn<T> type. Furthermore, all of the specialization for compiletime conditions are implemented using static<T> variables and expressions. The same function now implemented with BuildIt can be seen in Figure 24. Instead of using specialized IfThenElse constructors, the user must simply write an if condition. Beyond this, the conditions on static<T> can be interleaved with the dynamic control flow using the same syntax as on Line 4.

BuildIt extracts an AST from the user-supplied code, which is written exactly how a library would be written. We implement a lowering pass using BuildIt's AST visitor to generate TACO's IR from the AST to complete the code-generation process. Both of these approaches generate the exact same code, and thus the performance of the generated code is unaltered. The same methodology can be used by domain experts to rapidly prototype lightweight DSLs from existing high-performance library implementations and specialize the generated code for certain scenarios.

Figure 25 and Figure 26 show another example of how BuildIt makes generating code for TACO easy. Line 8 shows an example of how a compile-time condition is implemented. Line 12 shows how increaseSizeIfFull is called after the append logic and the resulting statements are inserted into the statement block before the append statements. In Figure 26, increaseSizeIfFull is simply called conditionally and BuildIt takes care of inserting the statement in the right order. This lets the programmer write the logic in the natural execution order, as they would write in a library.

```
Stmt CompressedModeFormat::getAppendCoord(Expr p,
    Expr i, Mode mode) {
2
3
   taco_iassert(mode.getPackLocation() == 0);
  Expr idxArray =getCoordArray(mode.getModePack());
4
   Expr stride = mode.getModePack().getNumModes();
5
   Stmt storeIdx = Store::make(idxArray,
6
    Mul::make(p, stride), i);
   if (mode.getModePack().getNumModes() > 1) {
    return storeIdx;
9
10
11
   Stmt maybeResizeIdx = increaseSizeIfFull(
    idxArray, getCoordCapacity(mode), p);
12
13
   return Block::make({maybeResizeIdx, storeIdx});
14 }
```

Fig. 25: Implementation of the getAppendCoord function in TACO for the compressed-level format. Notice the expressions and statements explicitly created by calling the constructors for the AST nodes

```
void BICompressedModeFormat::getAppendCoord(
    dyn<int> p, dyn<int> i, Mode mode) {
   taco_iassert(mode.getPackLocation() == 0);
3
   dyn<int*> &idxArray = getCoordArray(
4
                mode.getModePack());
   dyn<int> &capacity = getCoordCapacity(mode);
6
   if (mode.getModePack().getNumModes() <= 1)</pre>
7
    increaseSizeIfFull(idxArray, capacity, p);
8
   static<int> stride =
0
          mode.getModePack().getNumModes();
10
11
   idxArray[p * stride] = i;
12 }
```

Fig. 26: BuildIt implementation of the getAppendCoord function for the compressed-level format

B. Interpreter to a Compiler for an Esoteric Language

We present this simple yet convincing case study that demonstrates how the staging capabilities of BuildIt can be used to automatically create compilers for simple languages. We choose a very simple esoteric language, BrainFuck (BF), derived from the parent language P" [20], [21] for the purpose of this case study. Because the BF language is small, we can show the entire implementation here. At the same time, BF also has some interesting control flow-like loops and conditionals.

In addition, BF has only eight characters in its grammar +-, .><[], which mimic operations on a hypothetical turing machine. Apart from the program input and the program counter(PC), the runtime of BF has a fixed size tape and a tape head that points to one of the locations in the fixed-size tape. The "+", "-", ".", "," instructions are for incrementing, decrementing, outputting, and inputting the character at the current tape head one position right and left. The "[", "]" provide data dependent control flow. The "[" moves the PC to the matching "]" if the value at the current tape position is 0, and the "]" moves the PC back to the matching "[" if the value at the current tape head position is non-zero. These can be used to implement conditionals and loops.

Figure 27 shows a simple interpreter written for BF with BuildIt types. The input program and the PC are static states, and the tape contents and the tape head are dynamic states (Line 14). The rest of the code below goes through the entire input program and updates the states accordingly. First, this interpreter written with BuildIt looks exactly like a single-stage interpreter for BF (except for the declarations at the top).

```
1 // Input bf_program: const char*
2 static<int> pc = 0;
3 dyn<int> ptr = 0;
4 dyn<int[256]> tape = {0};
s while (bf_program[pc] != 0) {
6 if (bf_program[pc] == '>') {
    ptr = ptr + 1;
  } else if (bf_program[pc] == '<') {</pre>
    ptr = ptr - 1;
9
   } else if (bf_program[pc] == '+') {
10
11
    tape[ptr] = (tape[ptr] + 1) % 256;
   } else if (bf_program[pc] == '-') {
12
13
    tape[ptr] = (tape[ptr] - 1) % 256;
14 } else if (bf_program[pc] == '.') {
    print_value(tape[ptr]);
15
   } else if (bf_program[pc] == ',') {
16
    tape[ptr] = get_value();
17
   } else if (bf_program[pc] == '[') {
18
19
     if (tape[ptr] == 0) {
20
      pc = find_match(pc);
21
    }
   } else if (bf_program[pc] == ']') {
22
23
    pc = find_match(pc); - 1;
24
  }
25 pc += 1;
26 }
```

Fig. 27: Implementation of the BF interpreter written with BuildIt. This interpreter takes a BF program as input in a const char*. find_match is a helper static functions that find the position of the matching "[" or "]" for a PC

```
i int ptr = 0;
_{2} int tape[256] = {0};
3 tape[ptr] = (tape[ptr] + 1) % 256;
4 while (!(tape[ptr] == 0)) {
5 tape[ptr] = (tape[ptr] + 1) % 256;
6
   while (!(tape[ptr] == 0)) {
7
    tape[ptr] = (tape[ptr] + 1) % 256;
    while (!(tape[ptr] == 0)) {
      tape[ptr] = (tape[ptr] - 1) % 256;
9
     }
10
11
   }
12 }
```

Fig. 28: Output from Figure 27 with the input program "+[+[+[-]]]". Notice the nested while loops generated that do not exist in the original program.

Previous works [22] have shown that "a staged interpreter is a compiler. Because we are completely evaluating the BF program input in the first stage, the output of this BuildIt program would be a program that behaves just like the BF program would. Figure 28 shows the output of this program for a particular input "+[+[+[-]]]". All of the references to the input program and the PC have disappeared, and we are left with a C code that behaves exactly like the BF program. This simple example demonstrates how easily one can turn interpreters (which are easy to write) into compilers (which are generally hard to write and debug).

The reason this particular input is interesting is because it has a triply nested while loop in the generated code. Such a nested loop doesn't exist in the interpreter code but BuildIt is still able to extract it. This is mainly because BuildIt allows side effects on static<T> variables based on dyn<T> conditions, as shown in Line 19. Other techniques that use parsing the input program or lambdas for control flow (TensorFlow) would not be able to handle these rich control flow structures. Writing compilers this way has several other advantages. Besides being easy to implement and debug, interpreters are relatively easier to verify. Previous works [23] have shown that "Staged **verified** interpreters are **verified** compilers. Thus BuildIt's staging capabilities can be used to implement compilers with certain guarantees. In addition, optimizations can be incorporated into the compiler by implementing special cases (static conditions) in the interpreter to generate different code for specific scenarios. Again, reasoning about such cases is much easier with an interpreter.

C. Other BuildIt Applications

We have also applied BuildIt to generate efficient matrix multiplication CUDA code to run on GPUs, in which one of the sparse matrices is known at the time of compilation. By moving certain operations between the static and dynamic stage, we tune what fraction of the matrix is read at runtime along with what fraction of the matrix is baked as instructions into the generated program. This allows us to better utilize the instruction cache and the data caches for maximum performance. Implementing such a fine-tuning framework otherwise requires rewriting a lot of code every time we wish to move computations between stages.

VI. RELATED WORKS

[2] introduces many of the ideas used in this paper, including multi-stage programming and implementing compilers and DSLs using stage interpreters with Futamura projections [22]. This work is heavily based on the BUILDER library [24] for the SUIF [25] compiler system, which, as far as we know, is the earliest attempt at multi-stage programming using operator overloading in C++. BUILDER used operator overloading and symbolic execution for expressions but lacked support for extracting control flow and used specialized functions/constructors for loops and conditionals. In addition, C++ templates [26] and Haskell templates [27] by themselves are ways of implementing static meta-programming.

Specialized multi-stage languages like MetaML [10], MetaO-CAML [28], and Mint [29] that are a more principled approach for staging have been used for code generation and building DSLs. These take the compiler approach for extracting the program representation by the means of annotations or specialized syntax. MetaML and MetaOCAML either have a lot of code duplication [30] [31] [32] due to continuous style monadic execution or have to handle side effects through the means of a global state or delimited control operators. These can pose safety problems and invalidate guarantees of multistage programming languages. BuildIt's re-execution strategy confines the side effects to a particular branch and attempts to preserve these guarantees in an imperative language like C++ with explicit side effects. [33], [34] and Mint [29] have managed to deal with side effects without monadic execution. Terra [3], [35] is a meta-programming language that leverages a popular scripting language, Lua, to stage its execution.

Lightweight Modular Staging (LMS) [36] is the closest work to this paper and creates a staging system in Scala. It is also applied for code generation and embedding DSLs. Since the host language Scala is a functional programming language with reflection support, the challenges faced by this work are different. Notably, LMS uses reflection and introspection to extract conditionals. Their approach does model side effects through a global state, but the strategy is significantly different.

Recently, many frameworks like Tensorflow [6]. TACO [5] [19], Tiramisu [37] and Halide [38] have used operator overloading and symbolic execution to embed their DSLs in host languages like C++ and Python. Although DSLs like Cimple [39] and Tensorflow have also used specialized functions that input lambdas (or equivalent constructs in the host language) to handle control flows, supplying control structure through lambdas causes side effects on unstaged variables to spill out of the branches. Completely different from these approaches, DSLs like GraphIt [8] [9] and Simit [40] take the compiler approach for two-stage execution. A specialized compiler parses all operators and control flow structures from the input program and compiles them down to low-level C++/CUDA code. Web server languages like PHP, NGINX, NodeJS, and Asp.net use text-based, multi-stage programming for generating client code. Text-based generative programming can face the problems of code duplication and generally lack IDE and debugging support.

Applications of multi-stage programming: [41] have applied multi-stage execution in Scala using LMS [36] for achieving fast, modular whole program analysis using stage abstract interpreters. [23] have shown that verified staged interpreters are verified compilers. This extends the applications of multi-stage programming and BuildIt to program verification domains. Terra [3] generates and autotunes high-performance code for BLAS routines and stencil computations. Intel's ArBB [42] enables runtime generation of vector-style code using a combination of operator overloading and macros in C++.

VII. CONCLUSION

In this paper, we present BuildIt, which is, to the best of our knowledge, the first framework for imperative languages like C++ that can extract ASTs with control flows with a pure library approach, thus making it extremely lightweight and portable. We achieve this with repeated execution of the program to explore all control flow paths. We apply BuildIt's multi-stage programming capabilities for efficient code generation in DSLs and demonstrate that BuildIt can generate rich control flow from seemingly simple code by staging an interpreter for an esoteric language. In addition, we show how these techniques can be used for optimizations or providing guarantees in program.

BuildIt also changes the way we think about multi-staging as a problem reducing the PL complexity of a supposedly harder problem to a set of common features found in most languages.

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