

# Programmable Microfluidics

Bill Thies

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Massachusetts Institute of Technology

Stanford University – October 3, 2007

# Acknowledgements



**Prof. Saman  
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**Nada Amin**

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**J.P. Urbanski**  
**David Craig**



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**Natalie Andrew**

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**Prof. Mark Johnson**  
**David Potter**



*Colorado Center for  
Reproductive Medicine*

# Microfluidic Chips

- **Idea: a whole biology lab on a single chip**

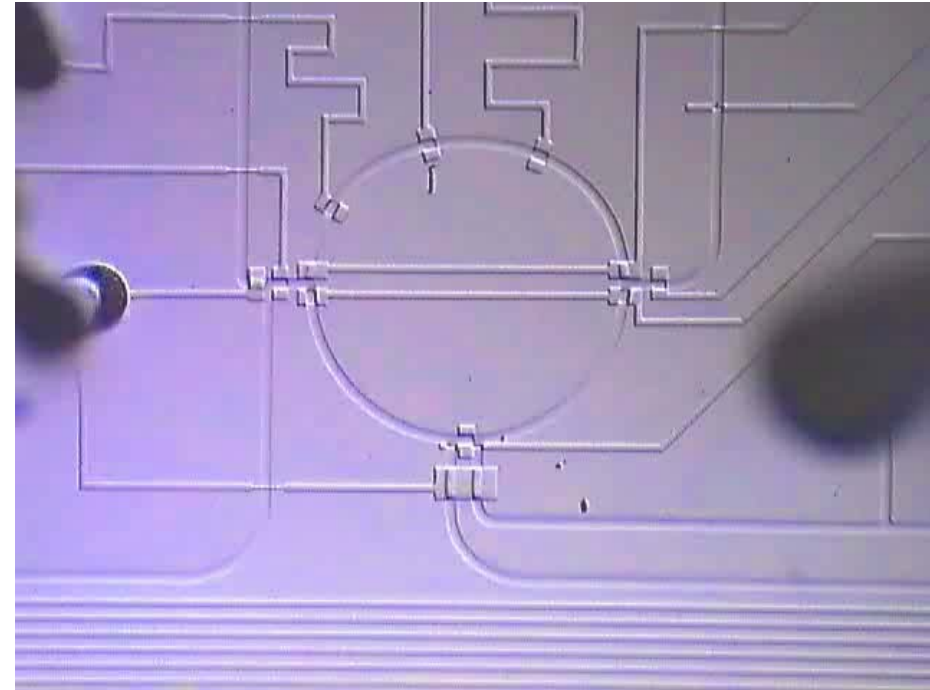
- Input/output
- **Sensors:** pH, glucose, temperature, etc.
- **Actuators:** mixing, PCR, electrophoresis, cell lysis, etc.

- **Benefits:**

- Small sample volumes
- High throughput
- Geometrical manipulation

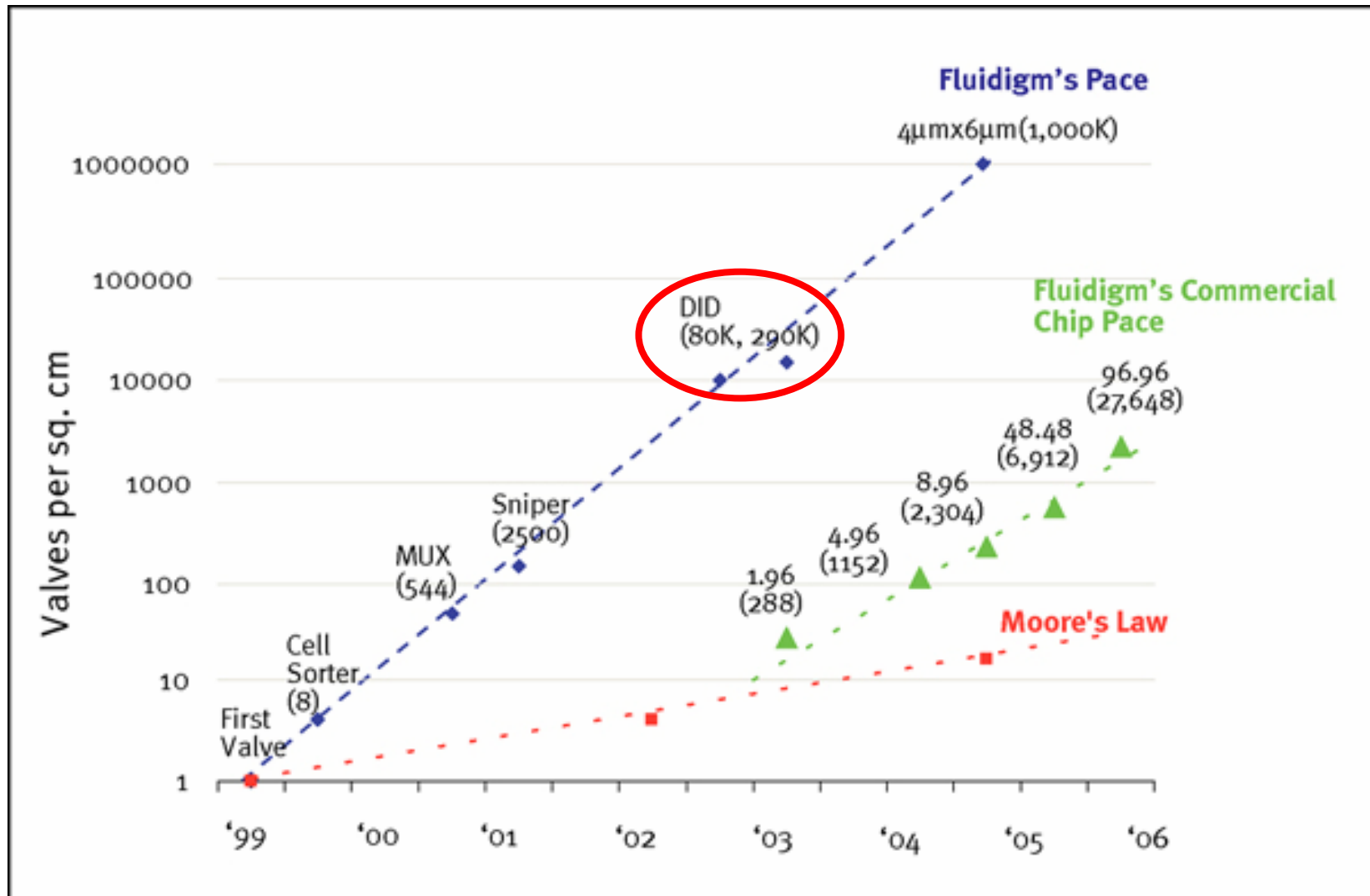
- **Applications:**

- Biochemistry
- Cell biology
- Biological computing



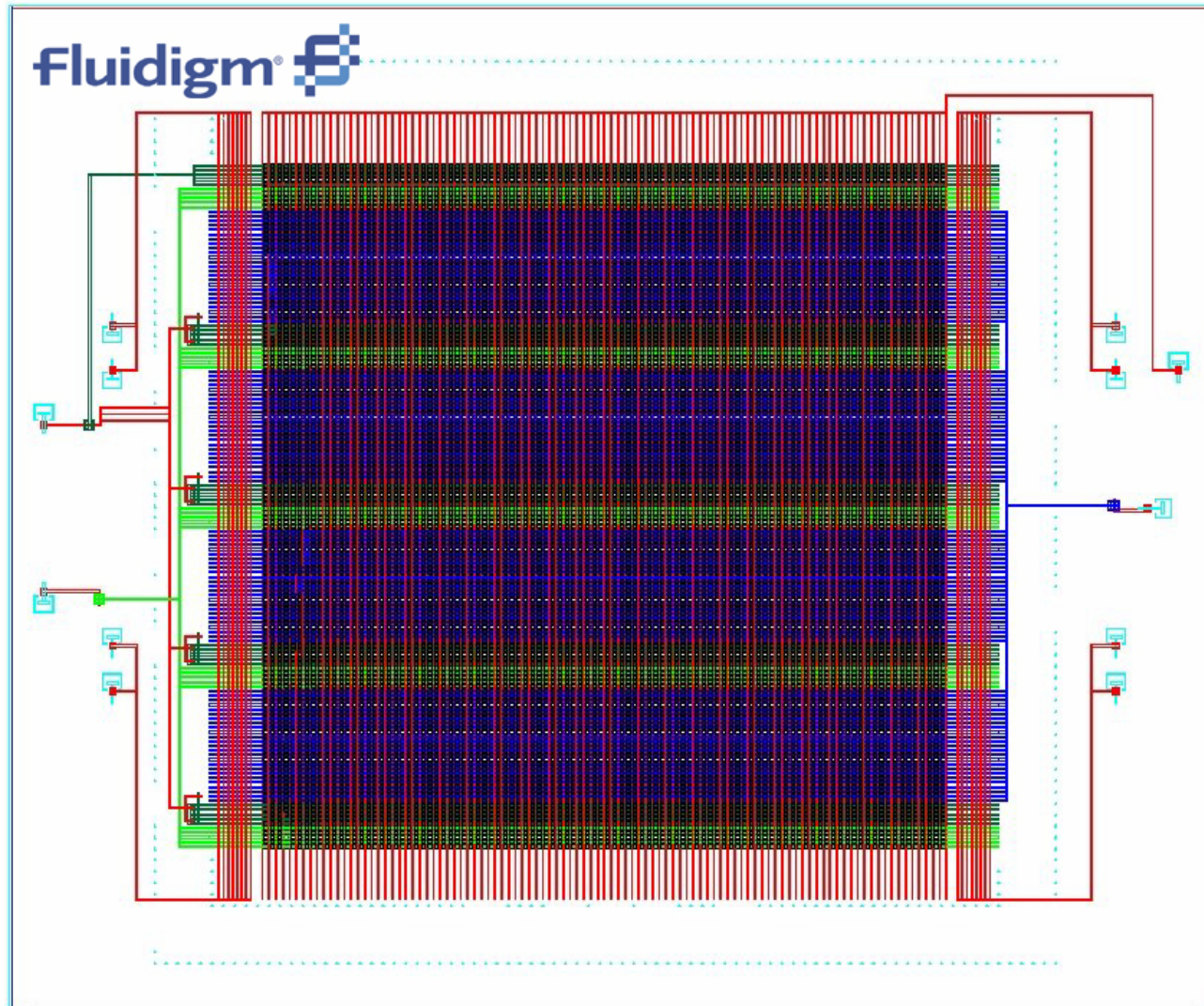
1 mm 10x real-time

# Moore's Law of Microfluidics: Valve Density Doubles Every 4 Months



Source: Fluidigm Corporation ([http://www.fluidigm.com/images/mlaw\\_lg.jpg](http://www.fluidigm.com/images/mlaw_lg.jpg))

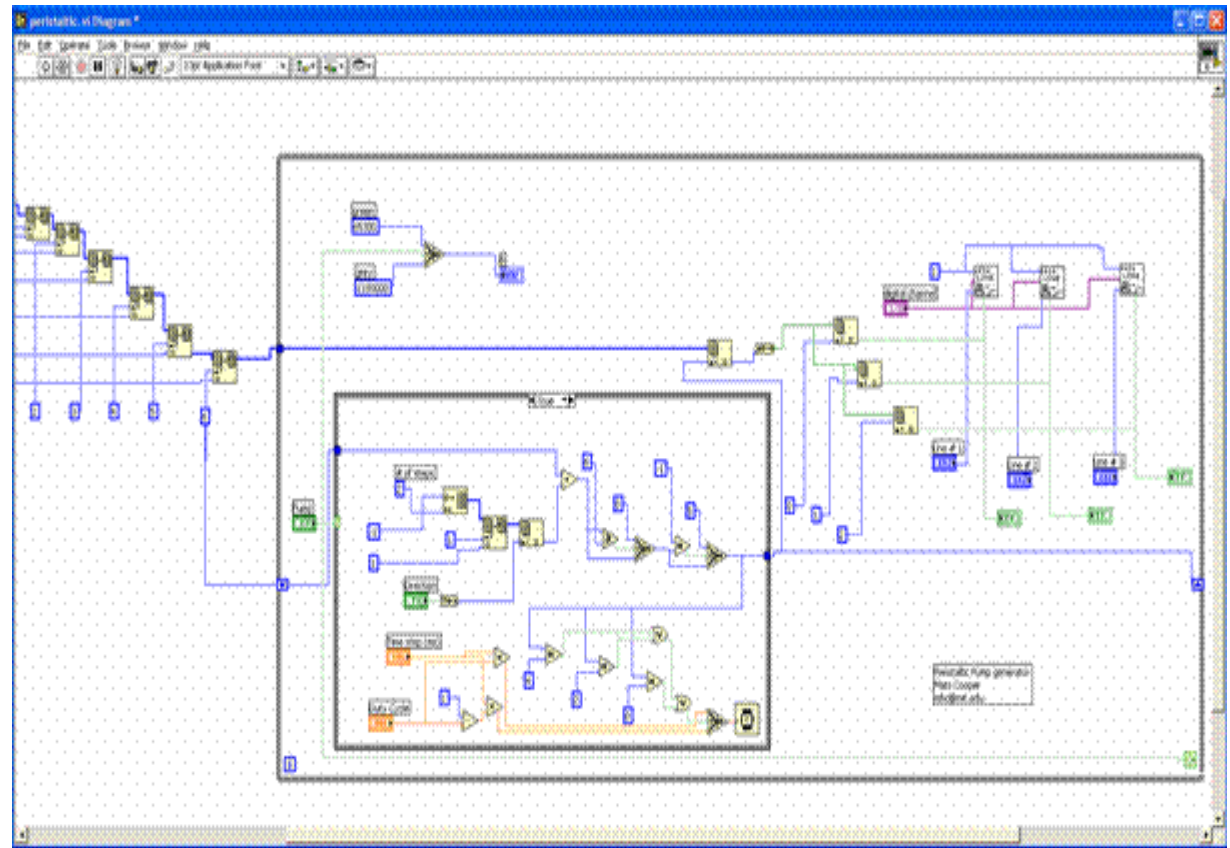
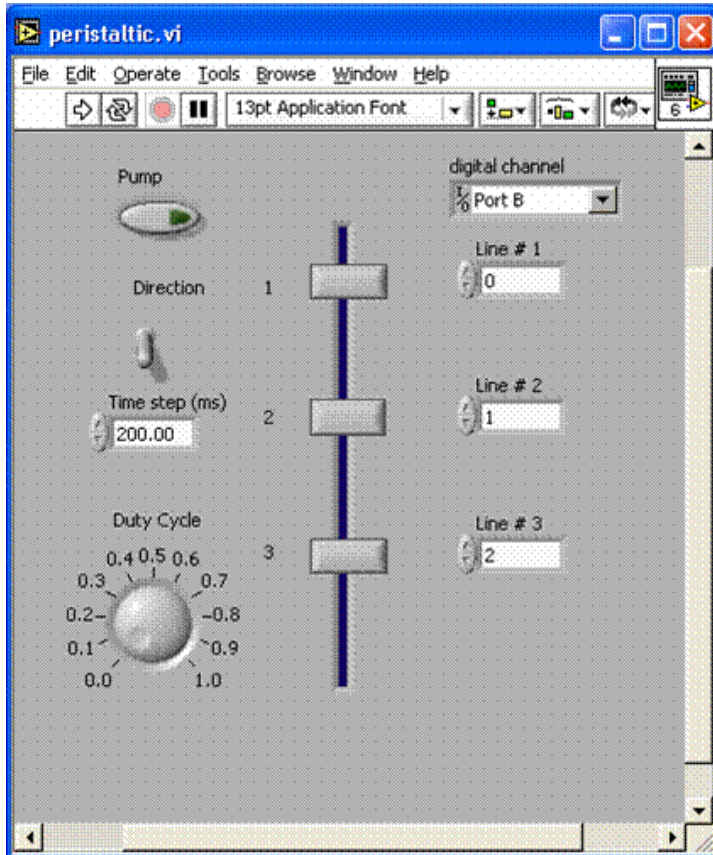
# Moore's Law of Microfluidics: Valve Density Doubles Every 4 Months



*Source: Fluidigm Corporation (<http://www.fluidigm.com/didIFC.htm>)*



# Current Practice: Expose Gate-Level Details to Users



- **Manually map experiment to the valves of the device**
  - Using Labview or custom C interface
  - Given a new device, start over and do mapping again

# Our Approach:

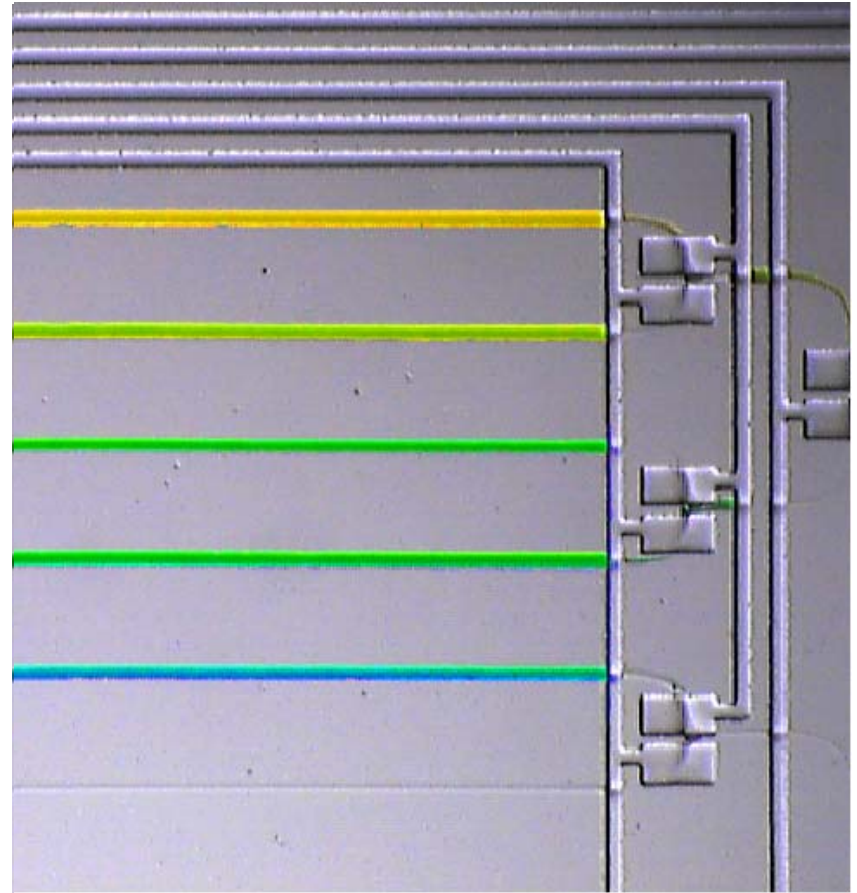
## “Write Once, Run Anywhere”

- **Example: Gradient generation**

```
Fluid yellow = input (0);  
Fluid blue = input(1);  
for (int i=0; i<=4; i++) {  
    mix(yellow, 1-i/4, blue, i/4);  
}
```

- **Hidden from programmer:**

- Location of fluids
- Details of mixing, I/O
- Logic of valve control
- Timing of chip operations



*450 Valve Operations*

# Our Approach:

## “Write Once, Run Anywhere”

- **Example: Gradient generation**

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Fluid yellow = input (0);  
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for (int i=0; i<=4; i++) {  
    mix(yellow, 1-i/4, blue, i/4);  
}
```



```
setValve(0, HIGH); setValve(1, HIGH);  
setValve(2, LOW); setValve(3, HIGH);  
setValve(4, LOW); setValve(5, LOW);  
setValve(6, HIGH); setValve(7, LOW);  
setValve(8, LOW); setValve(9, HIGH);  
setValve(10, LOW); setValve(11, HIGH);  
setValve(12, LOW); setValve(13, HIGH);  
setValve(14, LOW); setValve(15, HIGH);  
setValve(16, LOW); setValve(17, LOW);  
setValve(18, LOW); setValve(19, LOW);  
wait(2000);  
setValve(14, HIGH); setValve(2, LOW);  
wait(1000);  
setValve(4, HIGH); setValve(12, LOW);  
setValve(16, HIGH); setValve(18, HIGH);  
setValve(19, LOW);  
wait(2000);
```

- **Hidden from programmer:**

- Location of fluids
- Details of mixing, I/O
- Logic of valve control
- Timing of chip operations

*450 Valve Operations*



# Our Approach:

## “Write Once, Run Anywhere”

- **Example: Gradient generation**

```
Fluid yellow = input (0);  
Fluid blue = input(1);  
for (int i=0; i<=4; i++) {  
    mix(yellow, 1-i/4, blue, i/4);  
}
```



```
wait(2000);  
setValve(14, HIGH); setValve(2, LOW);  
wait(1000);  
setValve(4, HIGH); setValve(12, LOW);  
setValve(16, HIGH); setValve(18, HIGH);  
setValve(19, LOW);  
wait(2000);  
setValve(0, LOW); setValve(1, LOW);  
setValve(2, LOW); setValve(3, HIGH);  
setValve(4, LOW); setValve(5, HIGH);  
setValve(6, HIGH); setValve(7, LOW);  
setValve(8, LOW); setValve(9, HIGH);  
setValve(10, HIGH); setValve(11, LOW);  
setValve(12, LOW); setValve(13, LOW);  
setValve(14, LOW); setValve(15, HIGH);  
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setValve(18, HIGH); setValve(19, LOW);
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- **Hidden from programmer:**

- Location of fluids
- Details of mixing, I/O
- Logic of valve control
- Timing of chip operations

# Fluidic Abstraction Layers

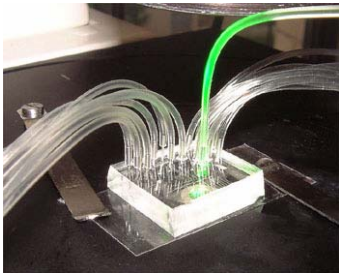
## Protocol Description Language

- readable code with high-level mixing ops

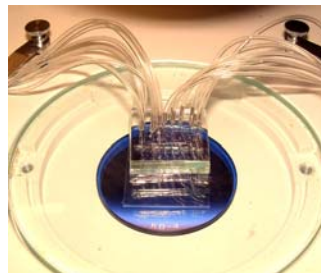


## Fluidic Instruction Set Architecture (ISA)

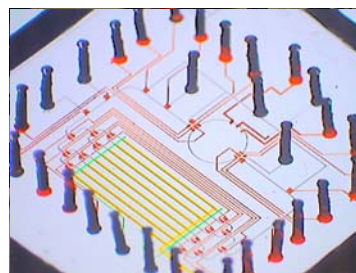
- primitives for I/O, storage, transport, mixing



chip 1



chip 2



chip 3



## Fluidic Hardware Primitives

- valves, multiplexers, mixers, latches

## Silicon Analog

C



x86



Pentium III,  
Pentium IV



transistors,  
registers, ...

# Fluidic Abstraction Layers

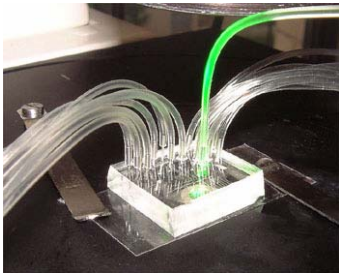
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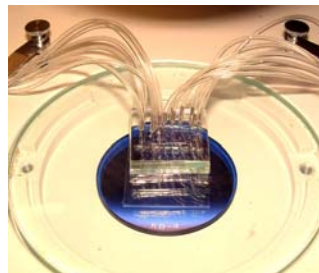


## Fluidic Instruction Set Architecture (ISA)

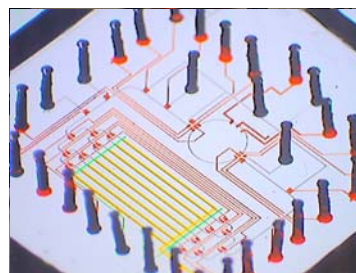
- primitives for I/O, storage, transport, mixing



chip 1



chip 2



chip 3



## Fluidic Hardware Primitives

- valves, multiplexers, mixers, latches

## • Benefits:

- Division of labor
- Portability
- Scalability
- Expressivity

# Fluidic Abstraction Layers

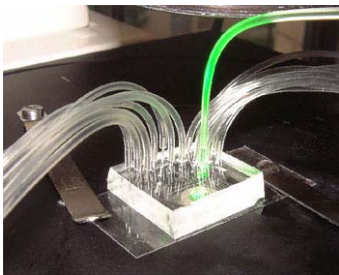
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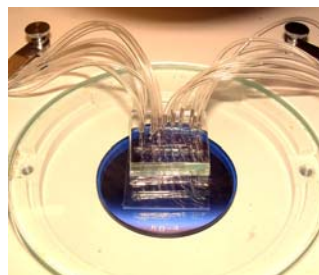


## Fluidic Instruction Set Architecture (ISA)

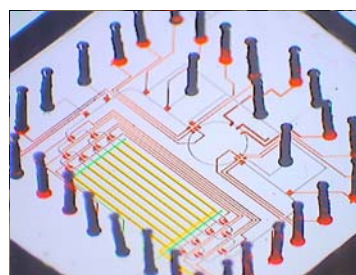
- primitives for I/O, storage, transport, mixing



chip 1



chip 2



chip 3

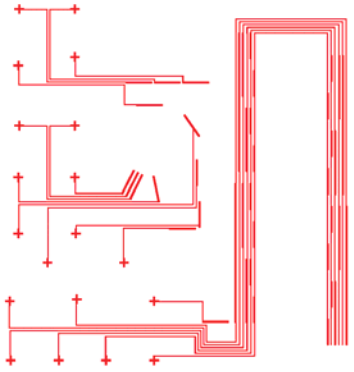
## • Benefits:

- Division of labor
- Portability
- Scalability
- Expressivity

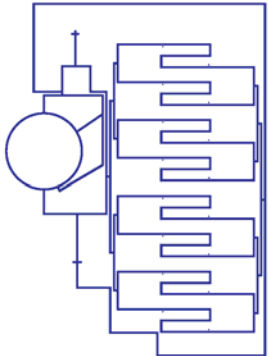
## Fluidic Hardware Primitives

- valves, multiplexers, mixers, latches

# Primitive 1: A Valve (Quake et al.)



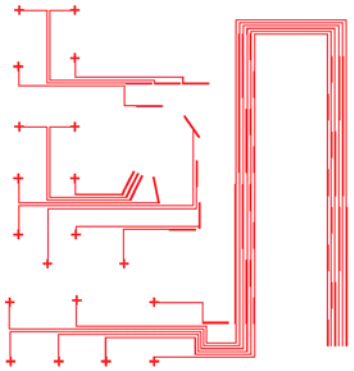
Control  
Layer



Flow  
Layer

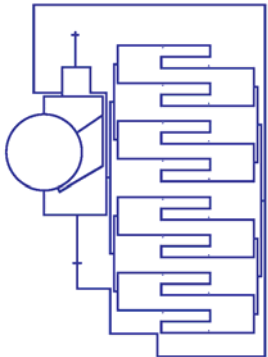


# Primitive 1: A Valve (Quake et al.)



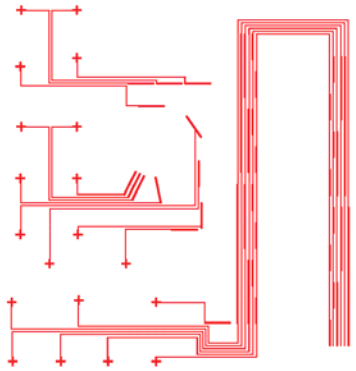
**Control  
Layer**

0. Start with mask of channels



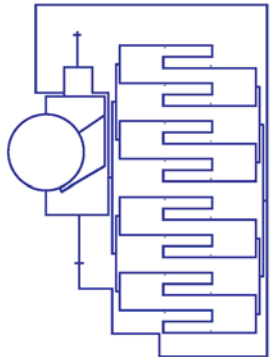
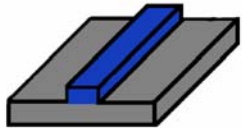
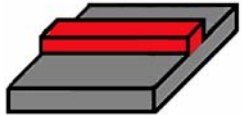
**Flow  
Layer**

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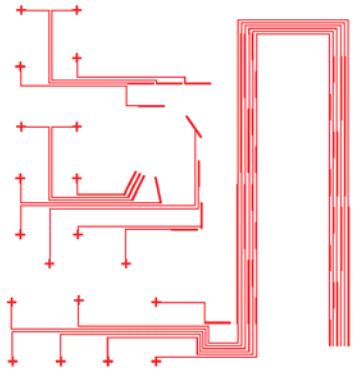
**Control  
Layer**

1. Deposit pattern on silicon wafer



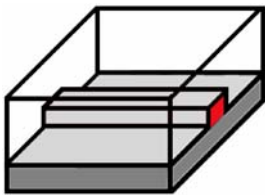
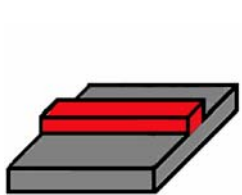
**Flow  
Layer**

# Primitive 1: A Valve (Quake et al.)

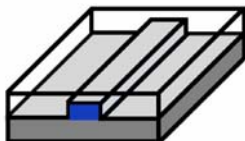
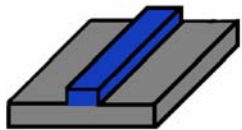


**Control  
Layer**

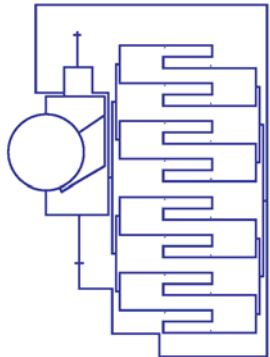
2. Pour PDMS over mold  
- polydimethylsiloxane: “soft lithography”



Thick layer (poured)

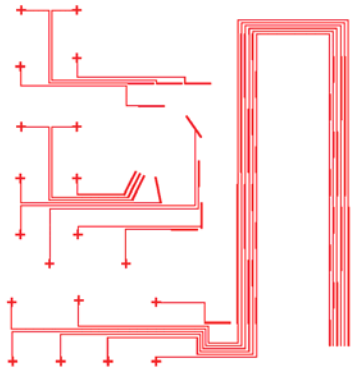


Thin layer (spin-coated)



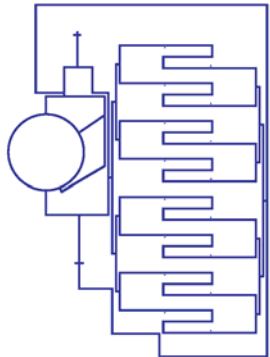
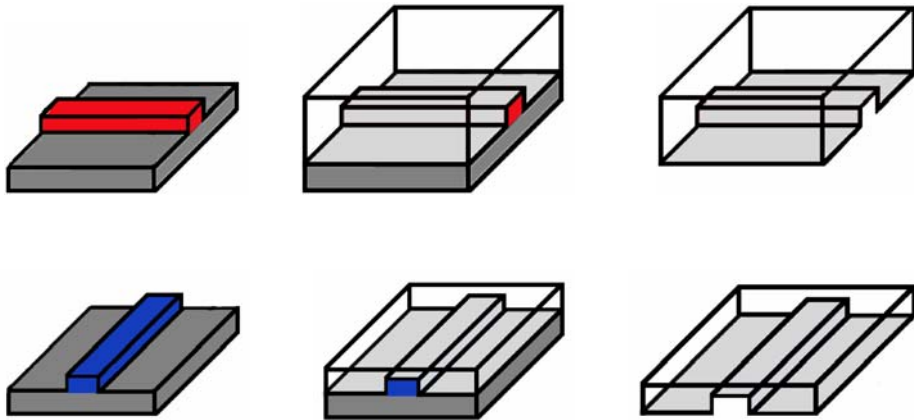
**Flow  
Layer**

# Primitive 1: A Valve (Quake et al.)



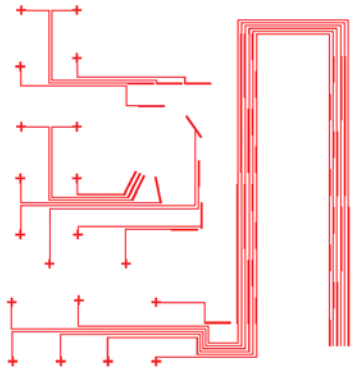
**Control  
Layer**

3. Bake at 80° C (primary cure),  
then release PDMS from mold



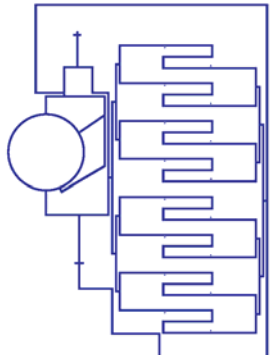
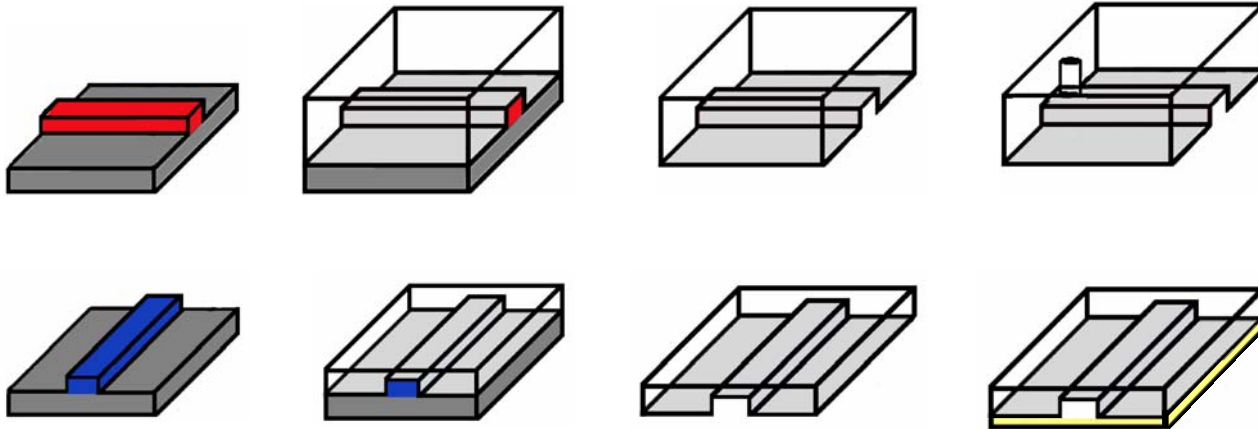
**Flow  
Layer**

# Primitive 1: A Valve (Quake et al.)



**Control  
Layer**

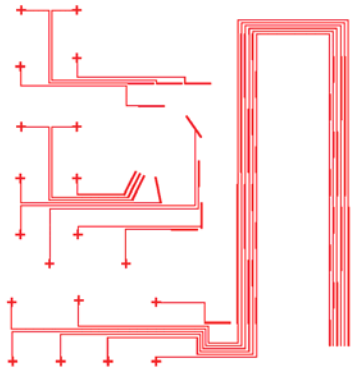
- 4a. Punch hole in control channel
- 4b. Attach flow layer to glass slide



**Flow  
Layer**

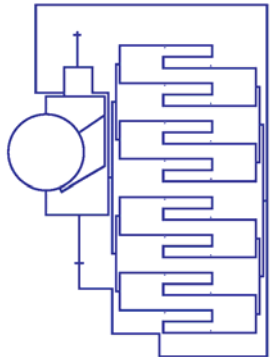
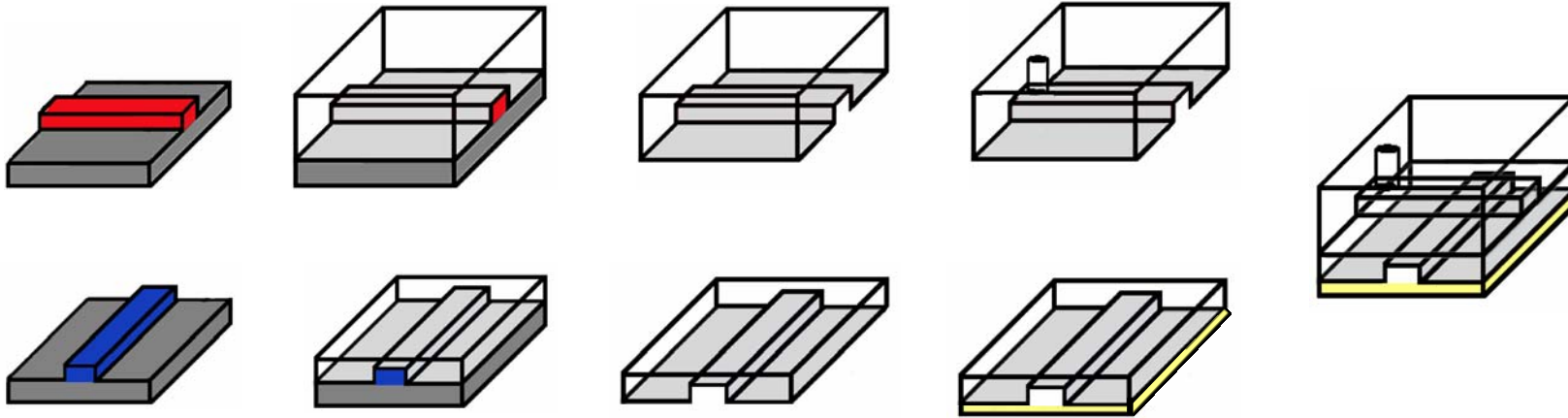


# Primitive 1: A Valve (Quake et al.)



Control  
Layer

5. Align flow layer over control layer

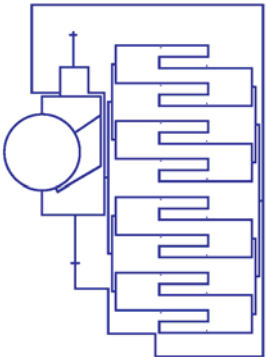
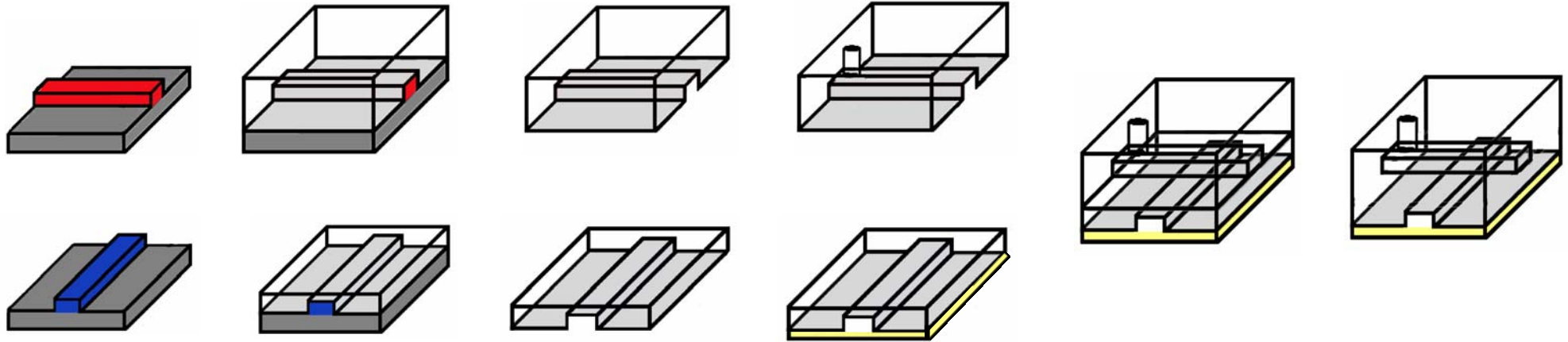
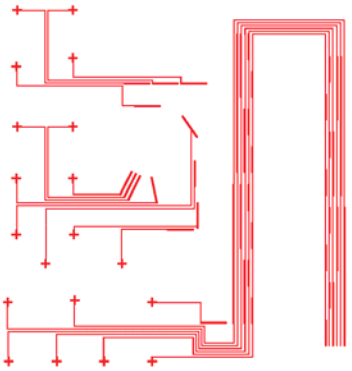


Flow  
Layer

# Primitive 1: A Valve (Quake et al.)

Control  
Layer

6. Bake at 80° C (secondary cure)



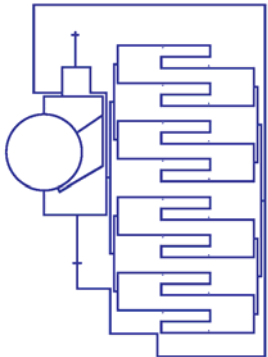
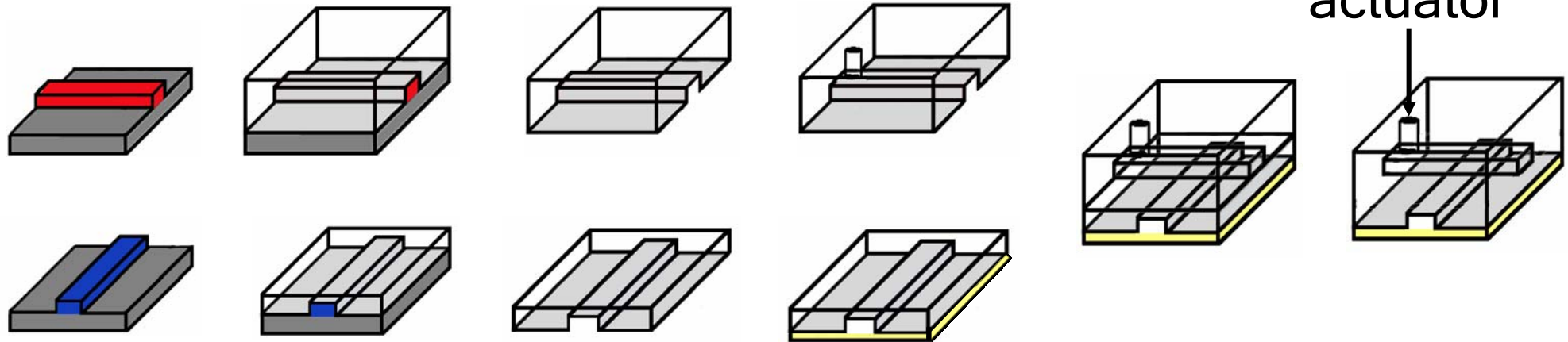
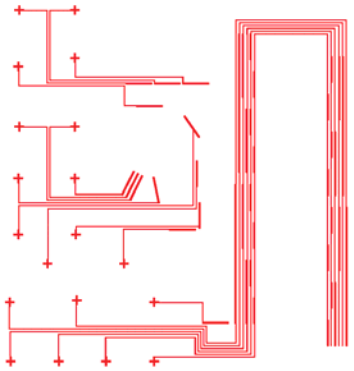
Flow  
Layer

# Primitive 1: A Valve (Quake et al.)

Control  
Layer

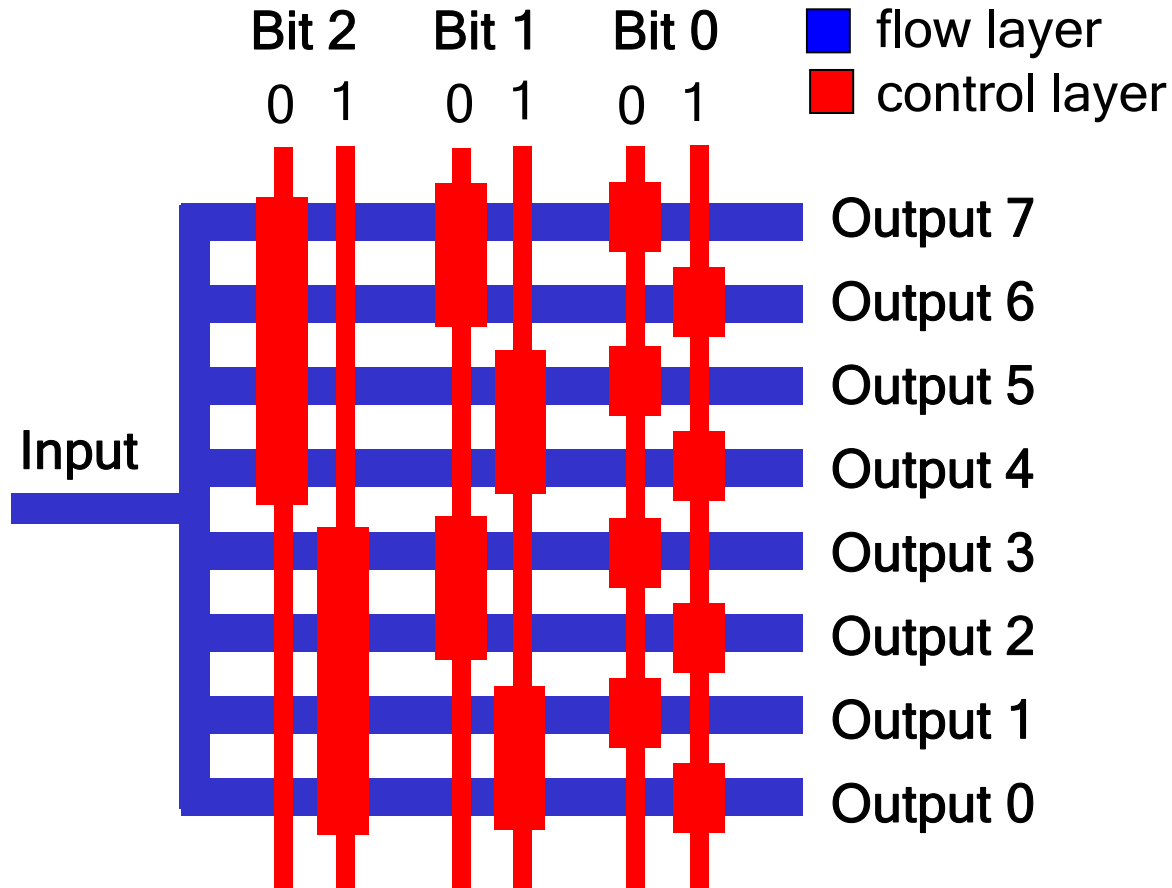
7. When pressure is high, control channel pinches flow channel to form a valve

pressure  
actuator

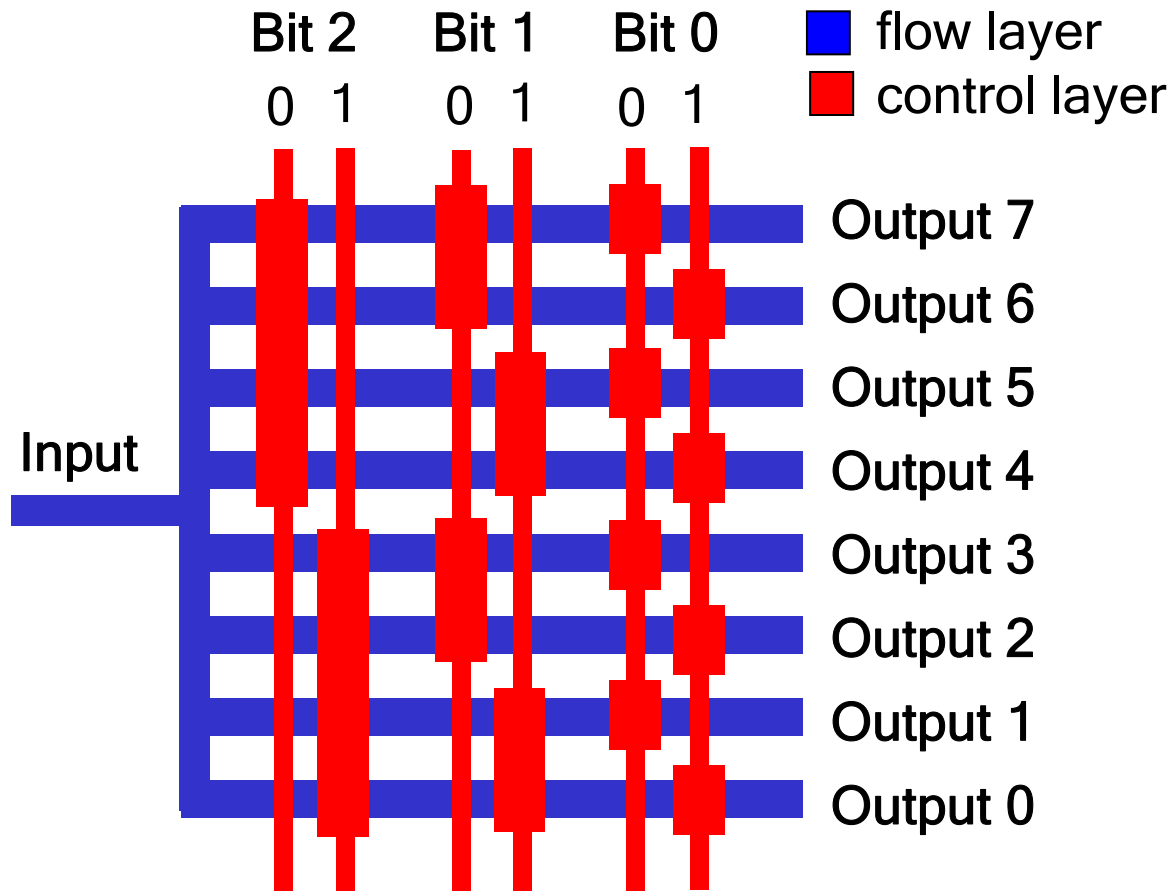


Flow  
Layer

# Primitive 2: A Multiplexer (Thorsen et al.)



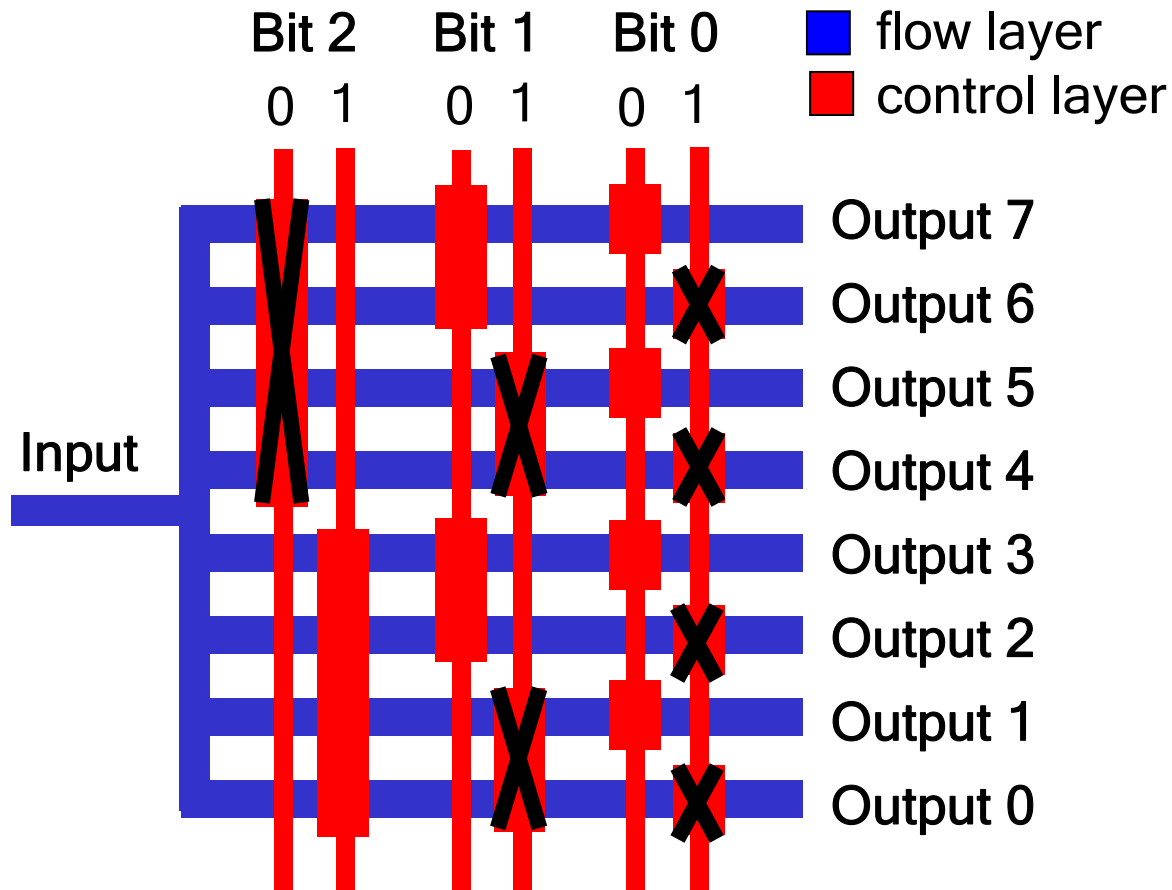
# Primitive 2: A Multiplexer (Thorsen et al.)



Example: select 3 = 011

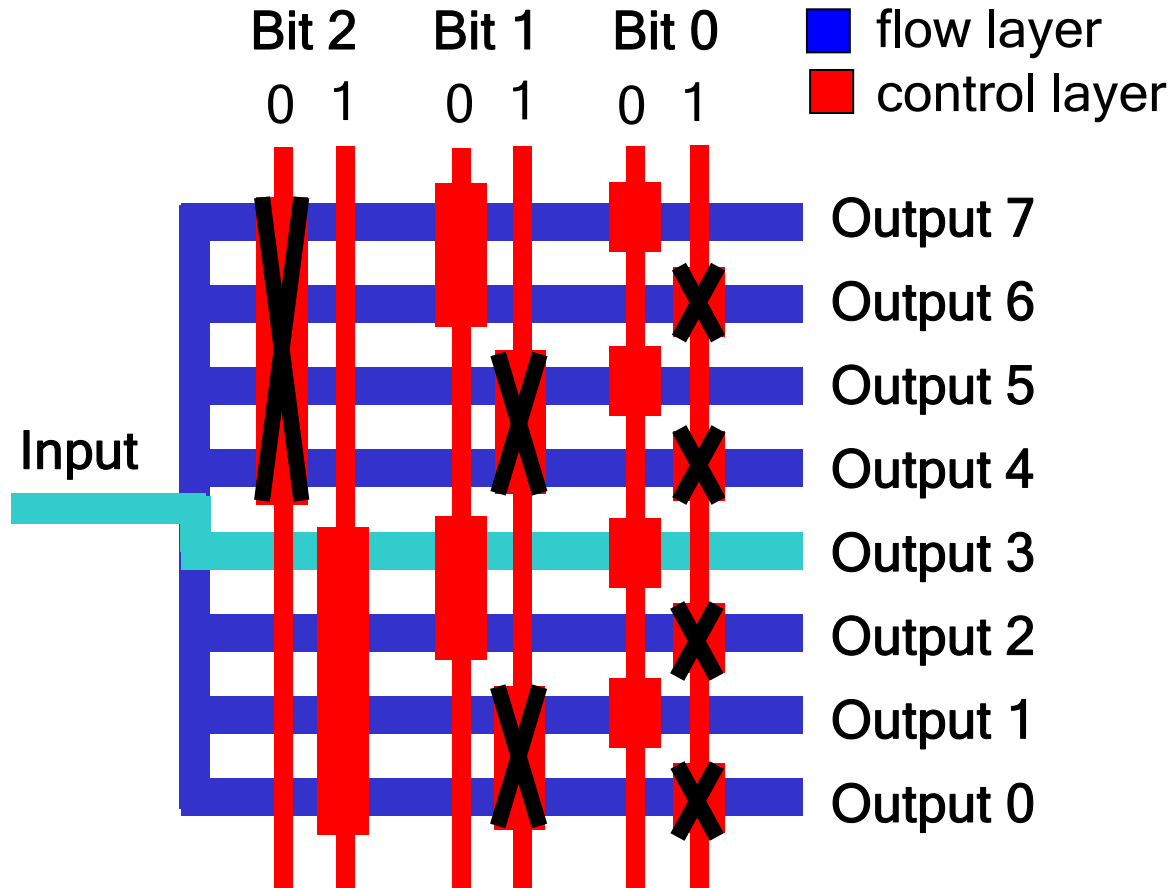


# Primitive 2: A Multiplexer (Thorsen et al.)



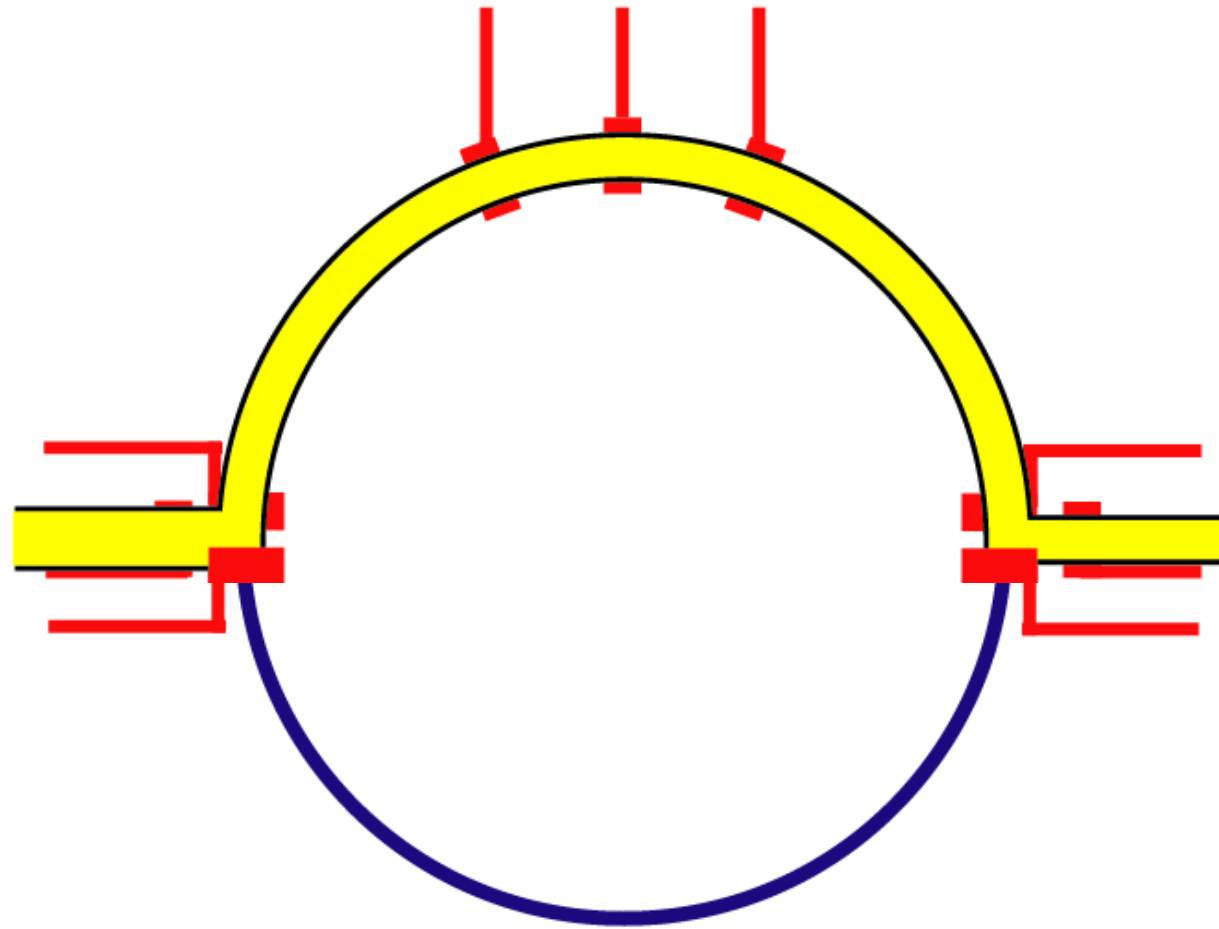
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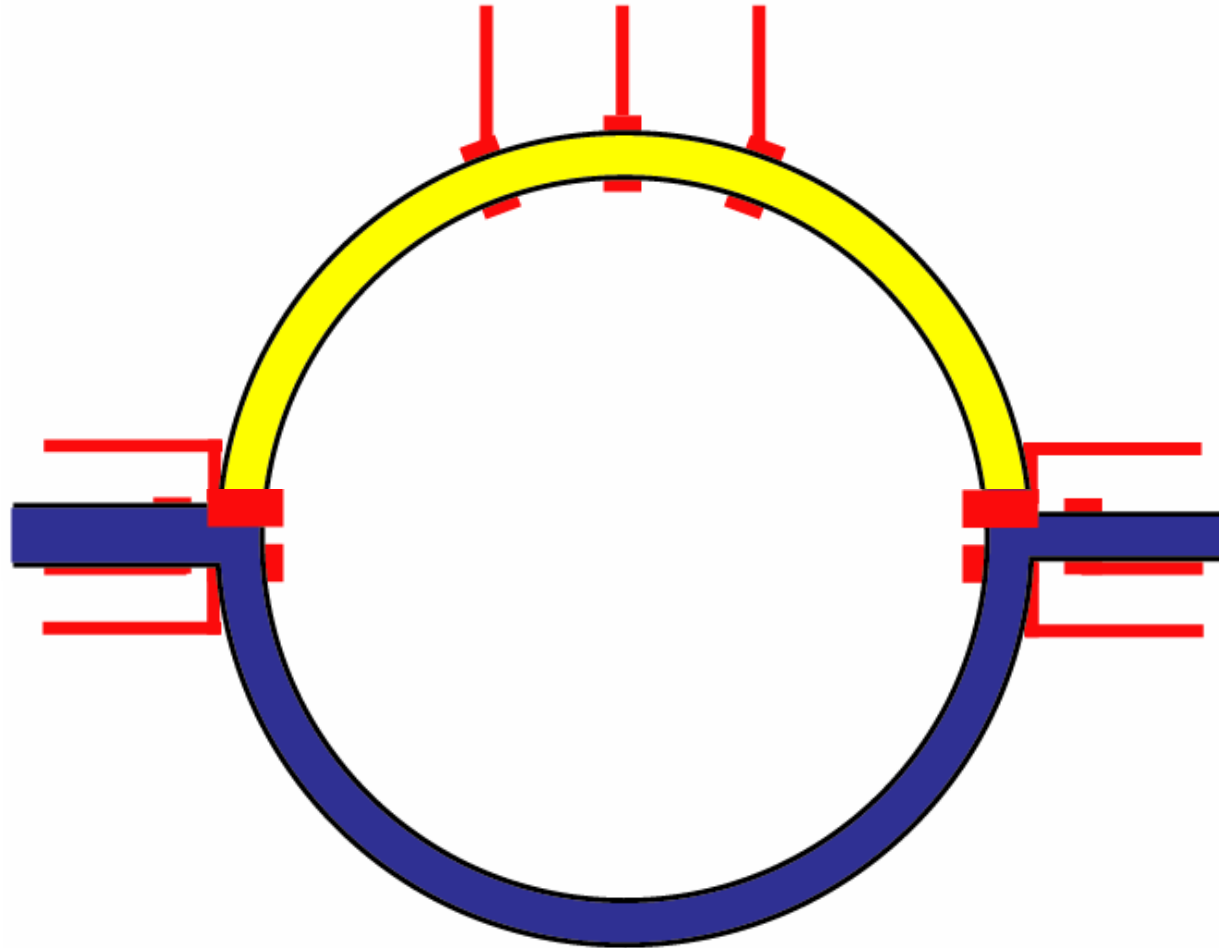
Example: select 3 = 011

# Primitive 3: A Mixer (Quake et al.)



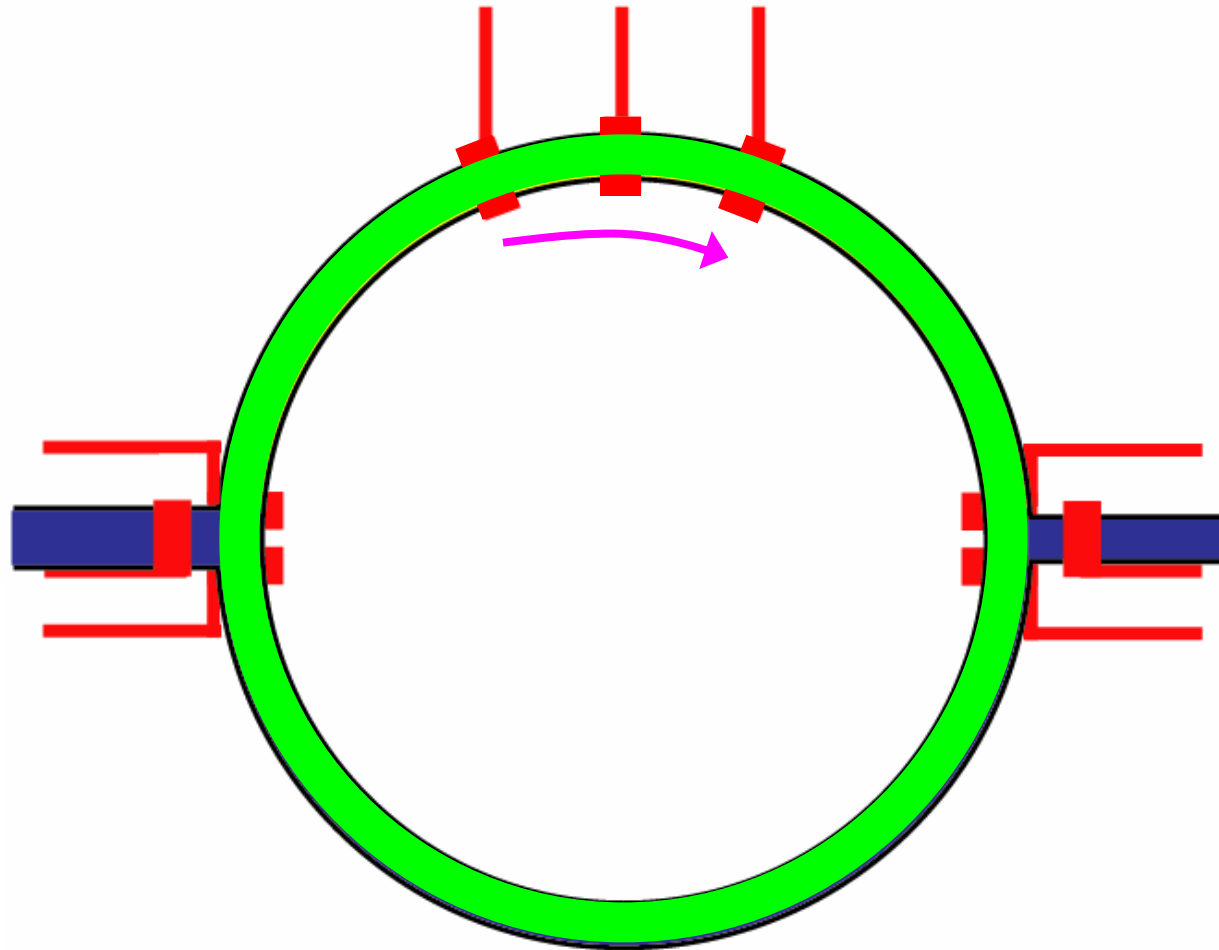
1. Load sample on top

# Primitive 3: A Mixer (Quake et al.)



1. Load sample on top
2. Load sample on bottom

# Primitive 3: A Mixer (Quake et al.)



1. Load sample on top
2. Load sample on bottom
3. Peristaltic pumping

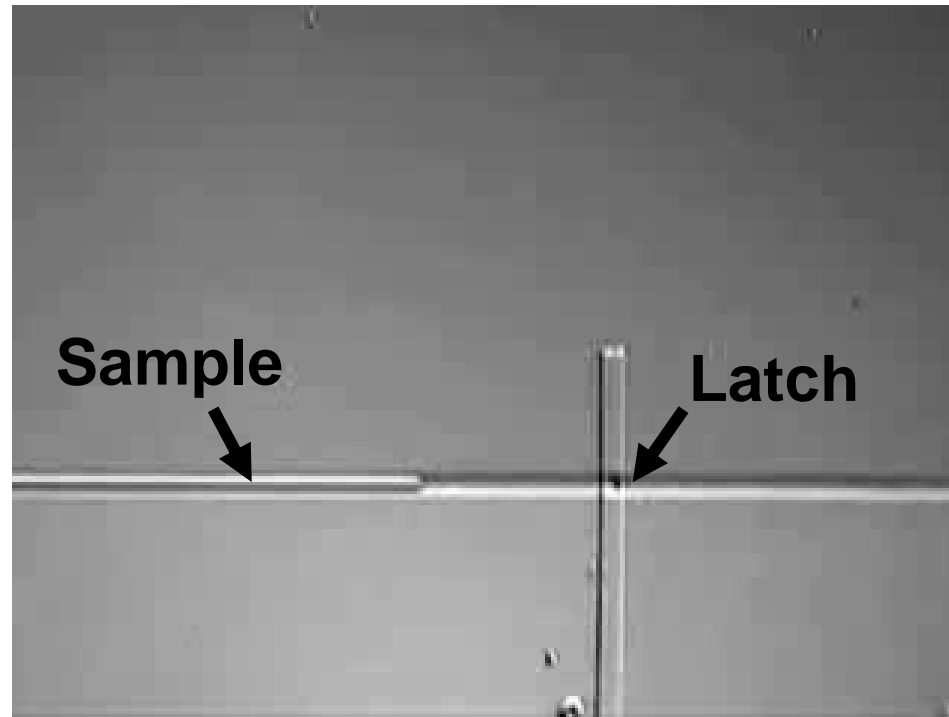


*Rotary Mixing*



# Primitive 4: A Latch (Our contribution)

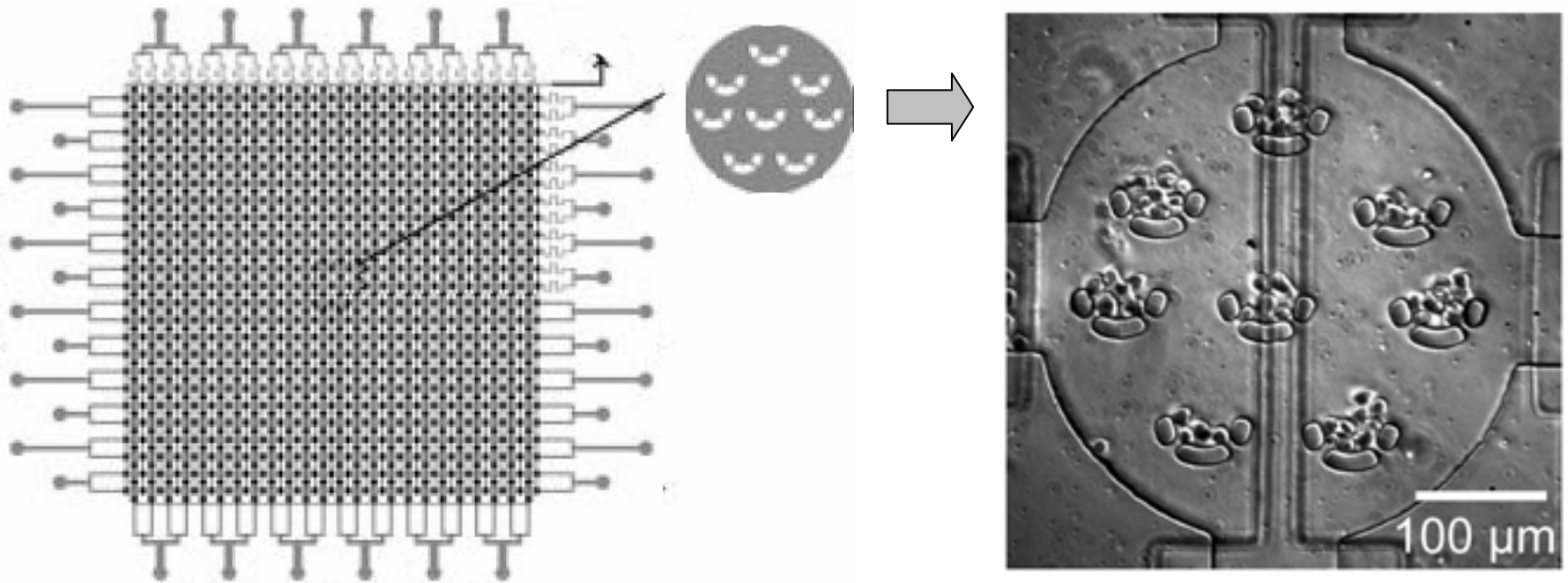
- **Purpose: align sample with specific location on device**
  - Examples: end of storage cell, end of mixer, middle of sensor



- **Latches are implemented as a partially closed valve**
  - Background flow passes freely
  - Aqueous samples are caught

# Primitive 5: Cell Trap

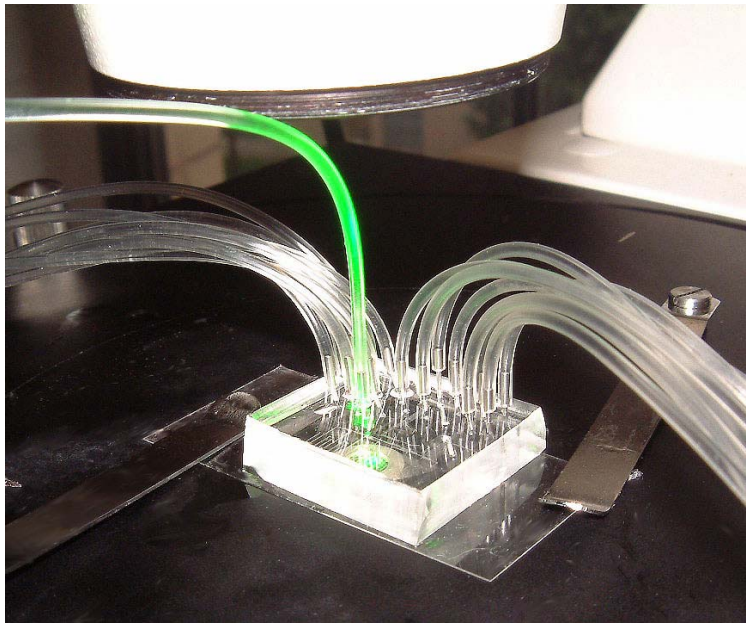
- **Several methods for confining cells in microfluidic chips**
  - U-shaped weirs
  - Holographic optical traps
  - C-shaped rings / microseives
  - Dielectrophoresis
- **In our chips: U-Shaped Microseives in PDMS Chambers**



*Source: Wang, Kim, Marquez, and Thorsen, Lab on a Chip 2007*

# Primitive 6: Imaging and Detection

- As PDMS chips are translucent, contents can be imaged directly
  - Fluorescence, color, opacity, etc.



- Feedback can be used to drive the experiment



# Fluidic Abstraction Layers

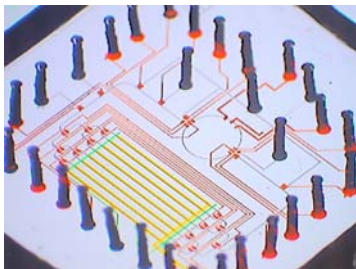
## Protocol Description Language

- readable code with high-level mixing ops

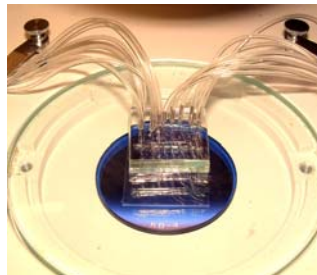


## Fluidic Instruction Set Architecture (ISA)

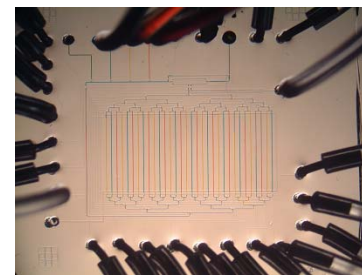
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chip 1



chip 2



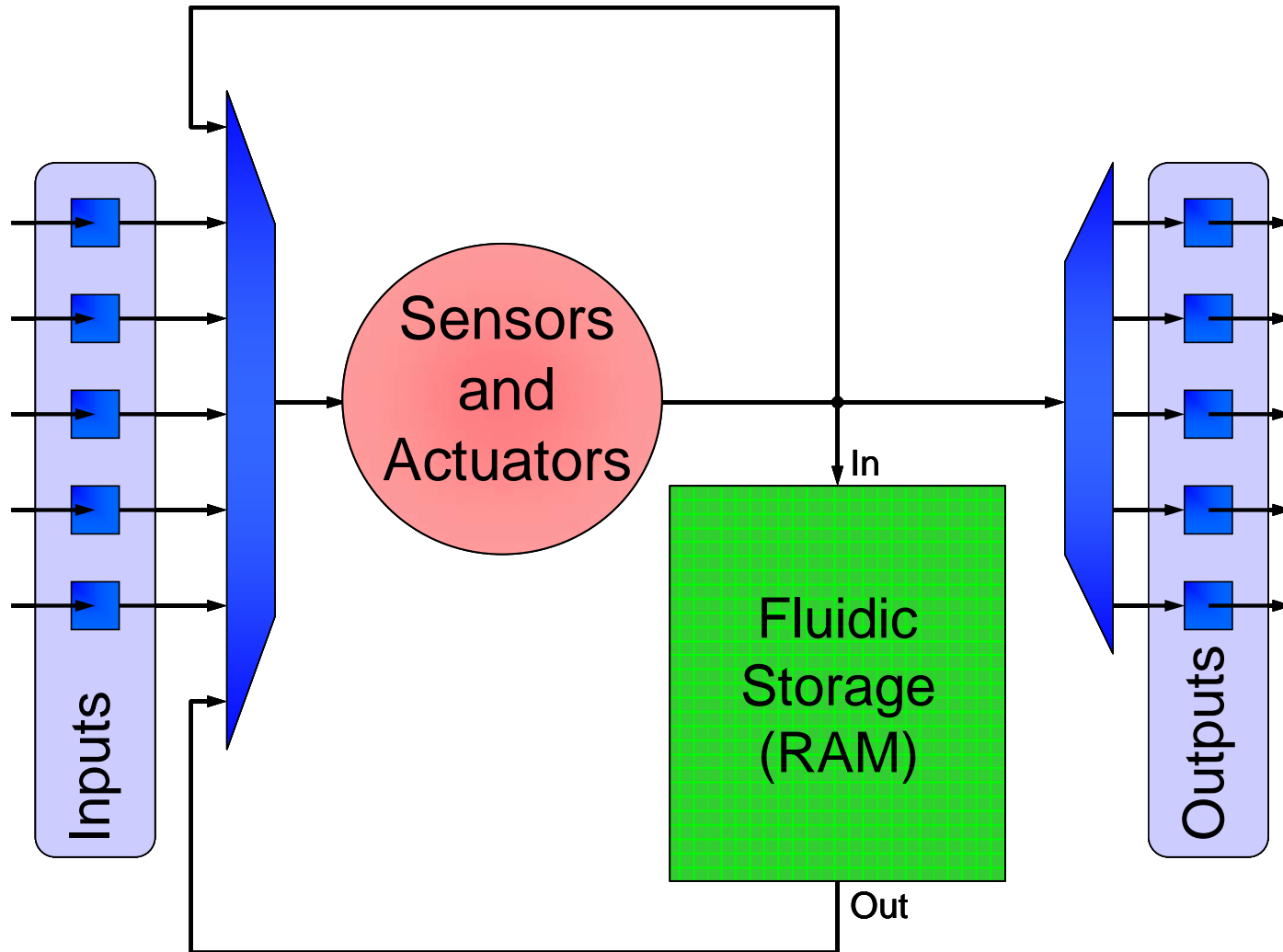
chip 3



## Fluidic Hardware Primitives

- valves, multiplexers, mixers, latches

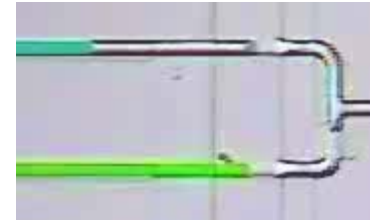
# Toward “General Purpose” Microfluidic Chips



# Abstraction 1: Digital Architecture

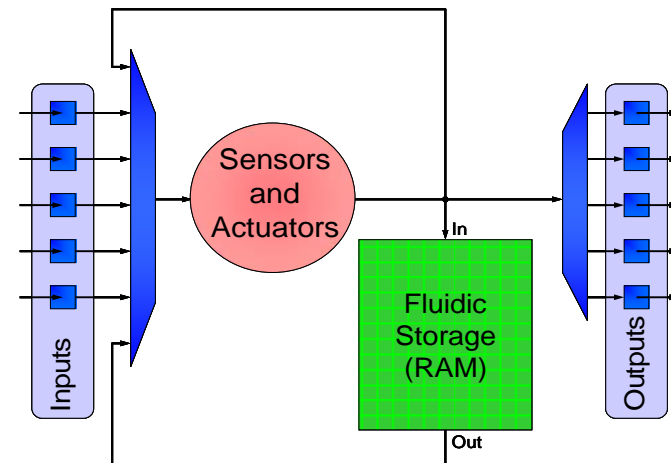
- **Recent techniques can control independent samples**

- Droplet-based samples [\[Fair et al.\]](#)
- Continuous-flow samples [\[Our contribution\]](#)
- Microfluidic latches [\[Our contribution\]](#)



- **In abstract machine, all samples have unit volume**

- Input/output a sample
- Store a sample
- Operate on a sample



- **Challenge for a digital architecture: fluid loss**

- No chip is perfect – will lose some volume over time
- Causes: imprecise valves, adhesion to channels, evaporation, ...
- How to maintain digital abstraction?

# Maintaining a Digital Abstraction

## Electronics

Soft error  
Handling?



Randomized  
Gates [Palem]



Replenish charge  
(GAIN)



Loss of charge

**High-Level  
Language**

**Instruction Set  
Architecture (ISA)**

**Hardware**

## Microfluidics

Expose loss in language ✓  
- User deals with it



Expose loss in ISA ✓  
- Compiler deals with it



Replenish fluids?  
- Maybe (e.g., with water)  
- But may affect chemistry

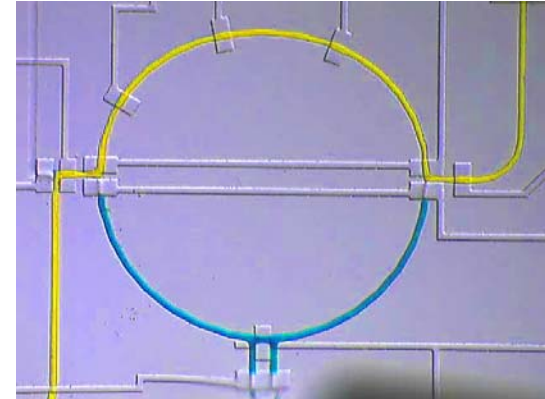


Loss of fluids



# Abstraction 2: Mix Instruction

- **Microfluidic chips have various mixing technologies**
  - Electrokinetic mixing [Levitan et al.]
  - Droplet mixing [Fair et al.]
  - Rotary mixing [Quake et al.]
- **Common attributes:**
  - Ability to mix two samples in equal proportions, store result
- **Fluidic ISA: **mix**** (int src<sub>1</sub>, int src<sub>2</sub>, int dst)



- Ex: mix(1, 2, 3)

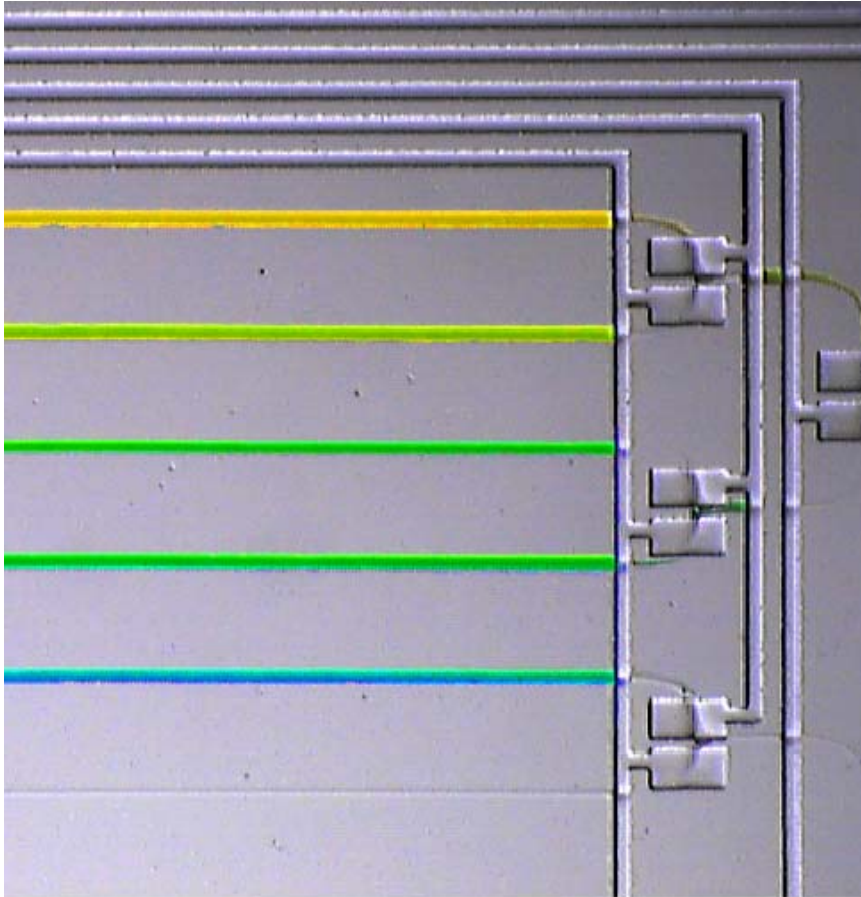
Storage Cells	
1	
2	
3	
4	

Mixer


- To allow for lossy transport, only 1 unit of mixture retained



# Gradient Generation in Fluidic ISA



# Gradient Generation in Fluidic ISA



```
wait(2000);  
setValve(14, HIGH); setValve(2, LOW);  
wait(1000);  
setValve(4, HIGH); setValve(12, LOW);  
setValve(16, HIGH); setValve(18, HIGH);  
setValve(19, LOW);  
wait(2000);  
setValve(0, LOW); setValve(1, LOW);  
setValve(2, LOW); setValve(3, HIGH);  
setValve(4, LOW); setValve(5, HIGH);  
setValve(6, HIGH); setValve(7, LOW);  
setValve(8, LOW); setValve(9, HIGH);  
setValve(10, HIGH); setValve(11, LOW);  
setValve(12, LOW); setValve(13, LOW);  
setValve(14, LOW); setValve(15, HIGH);  
setValve(16, HIGH); setValve(17, LOW);  
setValve(18, HIGH); setValve(19, LOW);
```

## Direct Control

- 450 valve actuations
- only works on 1 chip

*abstraction*

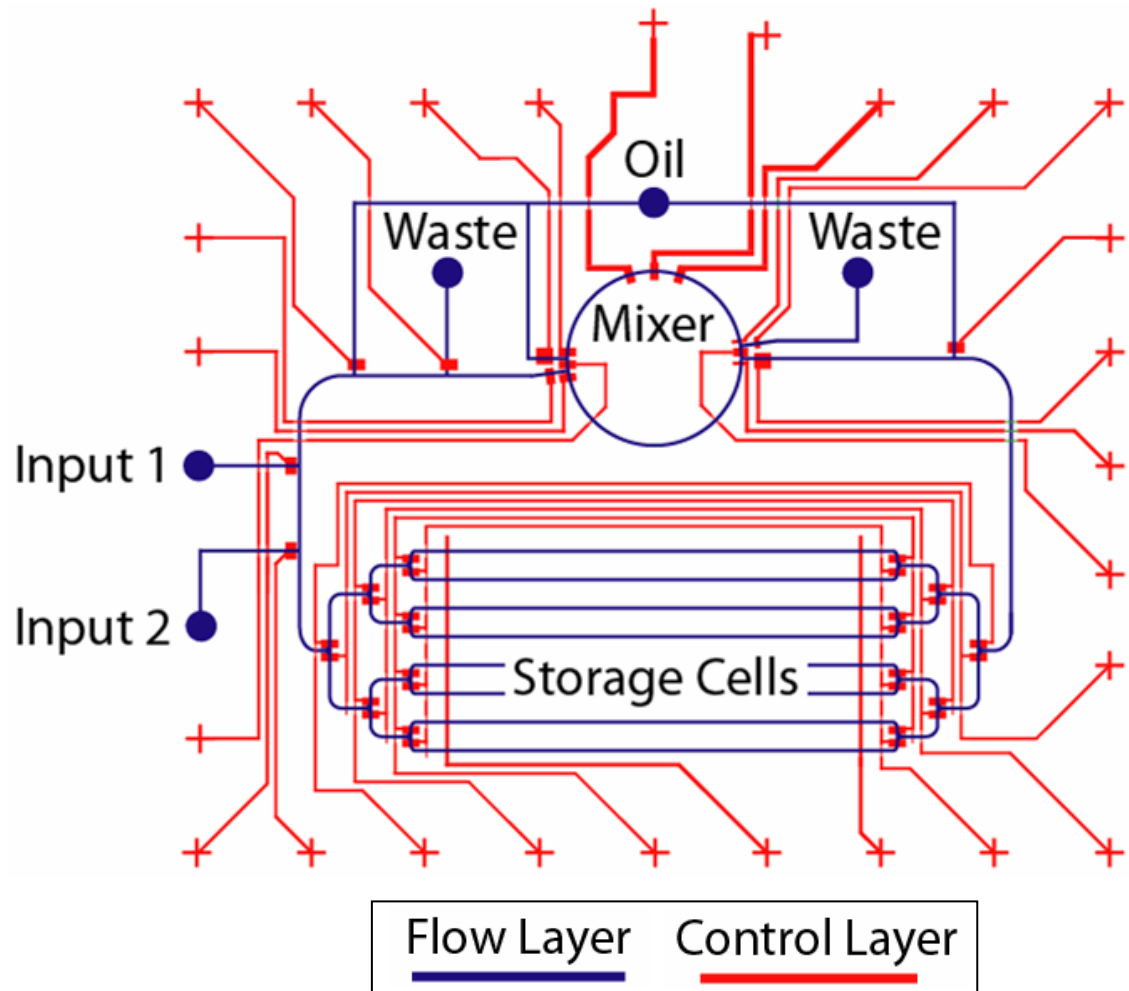


```
input(0, 0);  
input(1, 1);  
input(0, 2);  
mix(1, 2, 3);  
input(0, 2);  
mix(2, 3, 1);  
input(1, 3);  
input(0, 4);  
mix(3, 4, 2);  
input(1, 3);  
input(0, 4);  
mix(3, 4, 5);  
input(1, 4);  
mix(4, 5, 3);  
mix(0, 4);
```

## Fluidic ISA

- 15 instructions
- portable across chips

# Implementation: Oil-Driven Chip



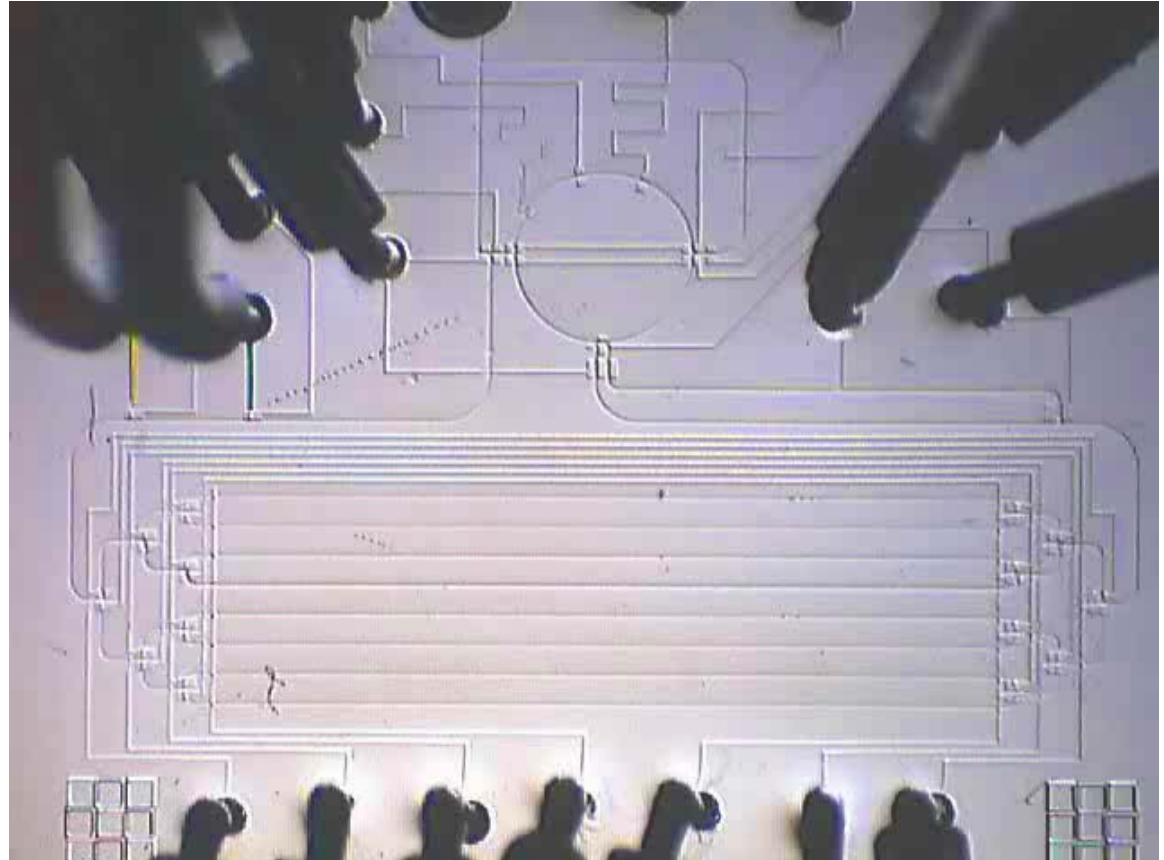
	Inputs	Storage Cells	Background Phase	Wash Phase	Mixing
Chip 1	2	8	Oil	—	Rotary

# Implementation: Oil-Driven Chip

```
mix ( $S_1$ ,  $S_2$ , D) {
```

- ➔ 1. Load  $S_1$
- 2. Load  $S_2$
- 3. Rotary mixing
- 4. Store into D

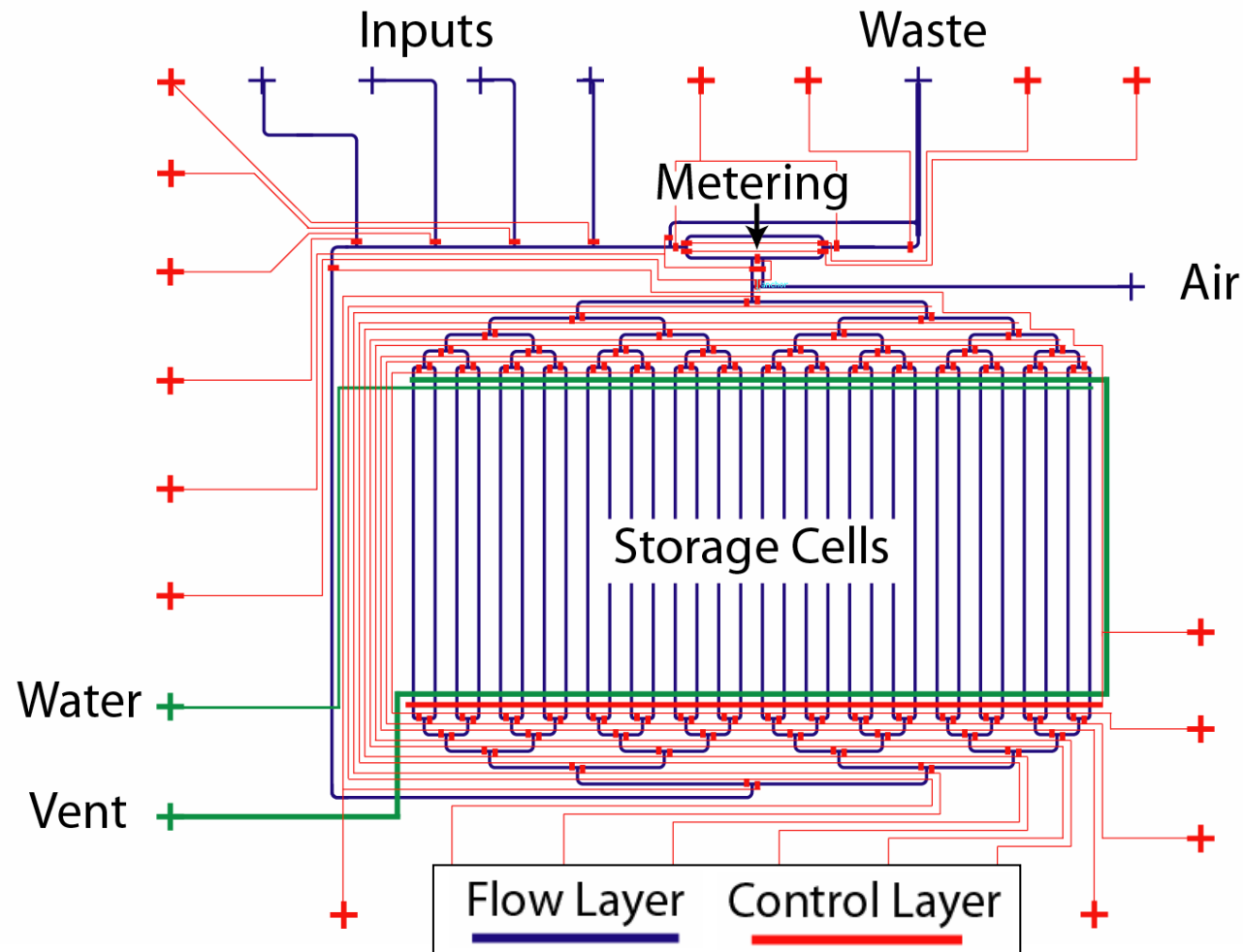
```
}
```



*50x real-time*

	Inputs	Storage Cells	Background Phase	Wash Phase	Mixing
Chip 1	2	8	Oil	—	Rotary

# Implementation 2: Air-Driven Chip

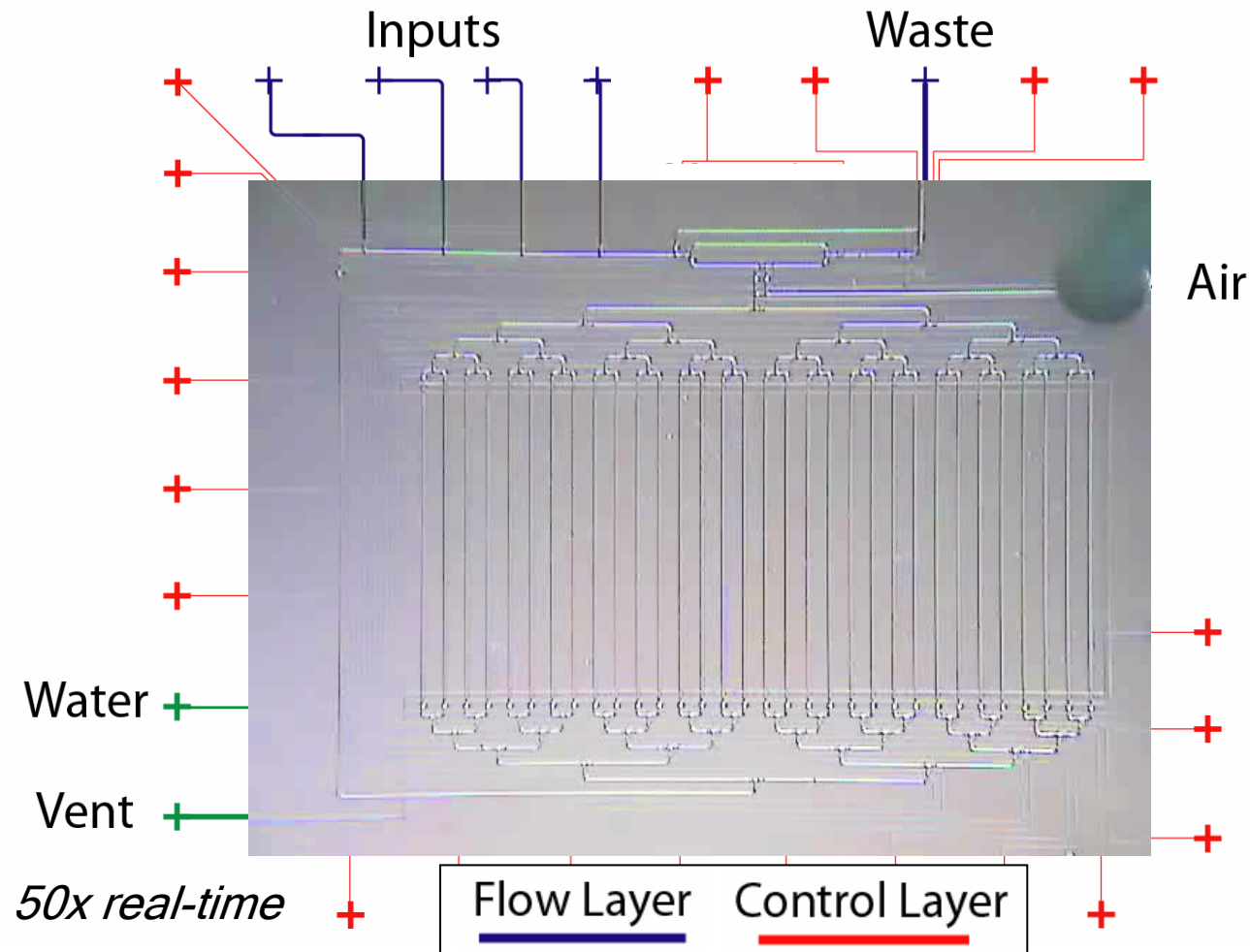


	Inputs	Storage Cells	Background Phase	Wash Phase	Mixing
Chip 1	2	8	Oil	—	Rotary
Chip 2	4	32	Air	Water	In channels

# Implementation 2: Air-Driven Chip

```

mix ( $S_1$ ,  $S_2$ ,  $D$ ) {
  1. Load  $S_1$ 
  2. Load  $S_2$ 
  3. Mix / Store into  $D$ 
  4. Wash  $S_1$ 
  5. Wash  $S_2$ 
}
    
```



	Inputs	Storage Cells	Background Phase	Wash Phase	Mixing
Chip 1	2	8	Oil	—	Rotary
Chip 2	4	32	Air	Water	In channels

# Fluidic Abstraction Layers

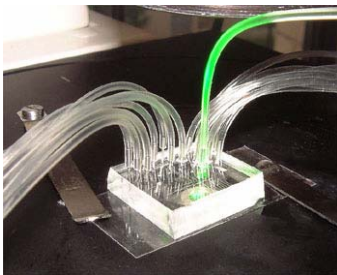
## Protocol Description Language

- readable code with high-level mixing ops

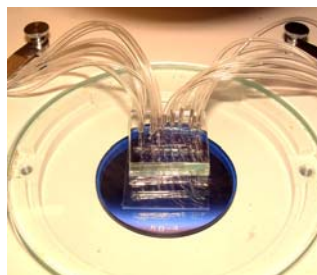


## Fluidic Instruction Set Architecture (ISA)

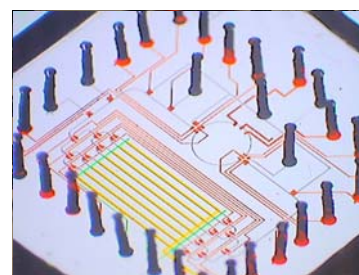
- primitives for I/O, storage, transport, mixing



chip 1



chip 2



chip 3



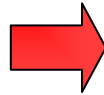
## Fluidic Hardware Primitives

- valves, multiplexers, mixers, latches

# Abstraction 1: Managing Fluid Storage

## Fluidic ISA

```
input(0, 0);
input(1, 1);
input(0, 2);
mix(1, 2, 3);
input(0, 2);
mix(2, 3, 1);
input(1, 3);
input(0, 4);
mix(3, 4, 2);
input(1, 3);
input(0, 4);
mix(3, 4, 5);
input(1, 4);
mix(4, 5, 3);
mix(0, 4);
```



```
Fluid[] out = new Fluid[8];
Fluid yellow, blue, green;
out[0] = input(0);
yellow = input(0);
blue = input(1);
green = mix(yellow, blue);
yellow = input(0);
out[1] = mix(yellow, green);
yellow = input(0);
blue = input(1);
out[2] = mix(yellow, blue);
yellow = input(0);
blue = input(1);
green = mix(yellow, blue);
blue = input(1);
out[3] = mix(blue, green);
out[4] = input(1);
```

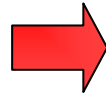
## 1. Storage Management

- **Programmer uses location-independent Fluid variables**
  - Runtime system assigns & tracks location of each Fluid
  - Comparable to automatic memory management (e.g., Java)



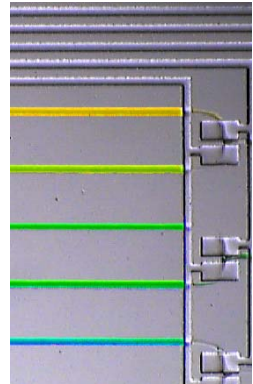
# Abstraction 2: Fluid Re-Generation

```
Fluid[] out = new Fluid[8];  
Fluid yellow, blue, green;  
out[0] = input(0);  
yellow = input(0);  
blue = input(1);  
green = mix(yellow, blue);  
yellow = input(0);  
out[1] = mix(yellow, green);  
yellow = input(0);  
blue = input(1);  
out[2] = mix(yellow, blue);  
yellow = input(0);  
blue = input(1);  
green = mix(yellow, blue);  
blue = input(1);  
out[3] = mix(blue, green);  
out[4] = input(1);
```



```
Fluid[] out = new Fluid[8];  
Fluid yellow = input(0);  
Fluid blue = input(1);  
Fluid green = mix(yellow, blue);  
  
out[0] = yellow;  
out[1] = mix(yellow, green);  
out[2] = green;  
out[3] = mix(blue, green);  
out[4] = blue;
```

## 2. Fluid Re-Generation



- **Programmer may use a Fluid variable multiple times**
  - Each time, a physical Fluid is consumed on-chip
  - Runtime system re-generates Fluids from computation history

# Custom Re-Generation

- **Some species cannot be regenerated by repeating history**
  - e.g., if selective mutagenesis has evolved unique sequence
- **Users can extend Fluid class, specify how to regenerate**
  - e.g., run PCR to amplify sequence of interest

```
class DNASample extends Fluid {  
  
    // Return array of fluids that are equivalent to this fluid  
    Fluid[] regenerate() {  
        Fluid amplified = performPCR(this, cycles, primer1, primer2, ...);  
        Fluid[] diluted = dilute(amplified, Math.pow(2, cycles));  
        return diluted;  
    }  
  
    // Return minimum quantity of this fluid needed to generate others  
    int minQuantity() {  
        return 1;  
    }  
}
```

# Unique Fluids Prohibit Re-Generation

- **Some Fluids may be unique, with no way to amplify**
  - E.g., products of cell lysis
- **Users can express this constraint using a UniqueFluid:**

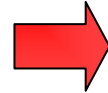
```
class UniqueFluid extends Fluid {  
    Fluid[] regenerate() {  
        throw new EmptyFluidException();  
    }  
}
```

```
UniqueFluid f = lysisProduct();  
UniqueFluid[] diluted = dilute(f);  
for (int i=0; i<diluted.length; i++) {  
    analyze(diluted[i]);  
}
```

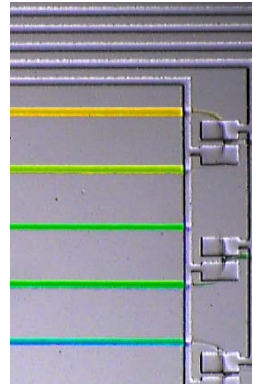
- **Can compiler verify that unique fluids used only once?**
    - Unique (linear) types is a rich research area in prog. languages  
[\[Wadler\]](#) [\[Hogg\]](#) [\[Baker\]](#) [\[Minsky\]](#) [\[Boyland\]](#) [\[Fahndrich & DeLine\]](#)
    - But solutions often require annotations & do not handle arrays
    - Practical approach: verify in simple cases, warn about others
- Opportunity for programming language research**

# Abstraction 3: Arbitrary Mixing

```
Fluid[] out = new Fluid[8];  
Fluid yellow = input(0);  
Fluid blue = input(1);  
Fluid green = mix(yellow, blue);  
  
out[0] = yellow;  
out[1] = mix(yellow, green);  
out[2] = green;  
out[3] = mix(blue, green);  
out[4] = blue;
```



```
Fluid[] out = new Fluid[8];  
Fluid yellow = input (0);  
Fluid blue = input (1);  
  
out[0] = yellow;  
out[1] = mix(yellow, 3/4, blue, 1/4);  
out[2] = mix(yellow, 1/2, blue, 1/2);  
out[3] = mix(yellow, 1/4, blue, 3/4);  
out[4] = blue;
```



## 2. Fluid Re-Generation

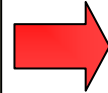
## 3. Arbitrary Mixing

- **Allows mixing fluids in any proportion, not just 50/50**
  - Fluid **mix** (Fluid  $F_1$ , float  $p_1$ , Fluid  $f_2$ , float  $F_2$ )
    - Returns Fluid that is  $p_1$  parts  $F_1$  and  $p_2$  parts  $F_2$
  - Runtime system translates to 50/50 mixes in Fluidic ISA
  - Note: some mixtures only reachable within error tolerance  $\varepsilon$

# Abstraction 3: Arbitrary Mixing

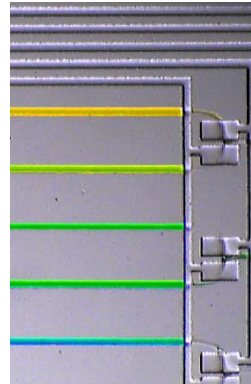
```
Fluid[] out = new Fluid[8];  
Fluid yellow = input (0);  
Fluid blue = input (1);  
  
out[0] = yellow;  
out[1] = mix(yellow, 3/4, blue, 1/4);  
out[2] = mix(yellow, 1/2, blue, 1/2);  
out[3] = mix(yellow, 1/4, blue, 3/4);  
out[4] = blue;
```

## 3. Arbitrary Mixing



```
Fluid[] out = new Fluid[8];  
Fluid yellow = input (0);  
Fluid blue = input (1);  
  
for (int i=0; i<=4; i++) {  
    out[i] = mix(yellow, 1-i/4, blue, i/4);  
}
```

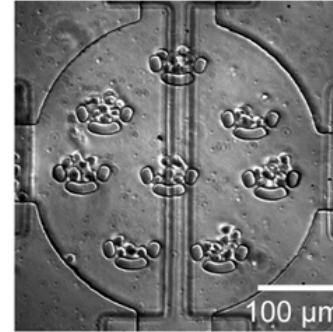
## 4. Parameterized Mixing



- **Allows mixing fluids in any proportion, not just 50/50**
  - Fluid **mix** (Fluid  $F_1$ , float  $p_1$ , Fluid  $f_2$ , float  $F_2$ )
    - Returns Fluid that is  $p_1$  parts  $F_1$  and  $p_2$  parts  $F_2$
  - Runtime system translates to 50/50 mixes in Fluidic ISA
  - Note: some mixtures only reachable within error tolerance  $\varepsilon$


# Abstraction 4: Cell Traps

- Unlike fluids, cells adhere to a specific location on chip
  - To interact with cells, need to move Fluids to their location
- CellTrap abstraction establishes a fixed chamber on chip
  - Fundamental capability: fill with a given fluid (incl. cell culture)



```
class CellTrap {  
    // establish a new, empty location on chip  
    CellTrap();  
  
    // replace contents of cell trap with new fluid; return old contents  
    UniqueFluid drainAndRefill(Fluid newContents);  
  
    // regenerate contents of cell trap; return drained fluid as needed  
    Fluid drainAndRegenerate();  
}
```

# Abstraction 4: Cell Traps



```
CellTrap celltrap = new CellTrap();           // setup cell culture
for (int i=0; i<N; i++)
    celltrap.drainAndRefill(cellCulture);

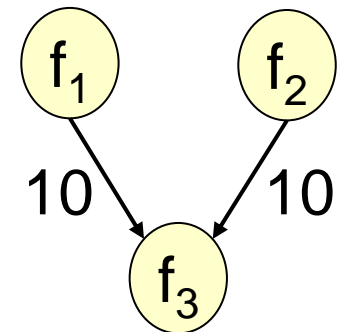
celltrap.drainAndRefill(distilledWater);       // analyze cell metabolites
Fluid metabolites = drainAndRegenerate();
analyzeWithIndicators(metabolites);

celltrap.drainAndRefill(antibodyStain);        // stain cells for imaging
```

- **Must schedule all uses of metabolites before staining**
- Otherwise, runtime error
  - Like unique variables, difficult to verify safety in general case
  - But thanks to language, compiler can give useful warnings

# Abstraction 5: Timing Constraints

- **Precise timing is critical for many biology protocols**
  - Minimum delay: cell growth, enzyme digest, denaturing, etc.
  - Maximum delay: avoid precipitation, photobleaching, etc.
  - Exact delay: regular measurements, synchronized steps, etc.
- **Simple API for indicating timing constraints:**
  - fluid.**useBetween**(N, M)                      – celltrap.**useBetween**(N, M)
  - Schedule next use of a Fluid (or drain of a CellTrap) between N and M seconds from time of the call
  - Also becomes part of Fluid's regeneration history
- **Note: may *require* parallel execution**
  - Fluid f1 = mix(...); f1.useBetween(10, 10);
  - Fluid f2 = mix(...); f2.useBetween(10, 10);
  - Fluid f3 = mix(f1, f2);





# Scheduling the Execution

- **Scheduling problem has two parts:**
  1. Given dependence graph, find a good schedule
  2. Extract dependence graph from the program

# 1. Finding a Schedule

## Abstract scheduling problem:

- Given task graph  $G = (V, E)$  with  $[\min, \max]$  latency per edge
- Find shortest schedule  $(V \mapsto \mathbb{Z})$  respecting latency on each edge

### → Case 1: Unbounded parallelism

- Can express as system of linear difference constraints
- Solve optimally in polynomial time

### → Case 2: Limited parallelism

- Adds constraint: only  $k$  vertices can be scheduled at once
- Can be shown to be NP-hard (reduce from PARTITION)
- Rely on greedy heuristics for now

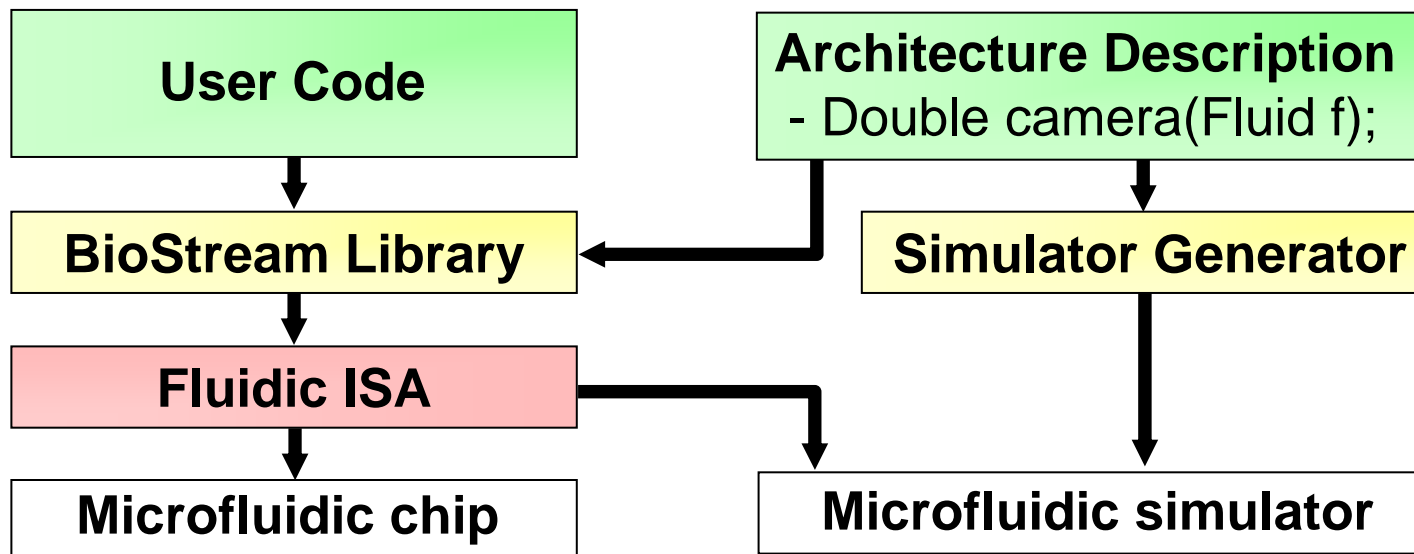
## 2. Extracting Dependence Graph

- **Static analysis difficult due to aliasing, etc.**
  - Requires extracting precise producer-consumer relationships
- **Opportunity:**  
**Perform scheduling at runtime, using lazy evaluation**
  - Microfluidic operations are slow → computer can run ahead
  - Build dependence graph of all operations up to decision point
- **Hazard: constraints that span decision points**
  - Dynamic analysis cannot look into upcoming control flow
  - We currently prohibit such constraints – leave as open problem

# BioStream Protocol Language

- **Implements the abstractions**
  - Full support for storage management, fluid re-generation, arbitrary mixing
  - Partial support for cells, timing
- **Implemented as a Java library**
  - Allows flexible integration with general-purpose Java code
- **Targets microfluidic chips or auto-generated simulator**

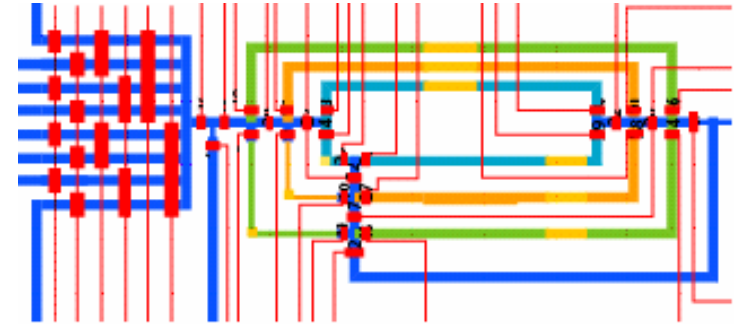
```
Fluid yellow = input (0);  
Fluid blue = input (1);  
Fluid[] out = new Fluid[8];  
for (int i=0; i<=4; i++)  
    out[i] = mix(yellow, 1-i/4,  
                blue, i/4);
```



# Applications in Progress

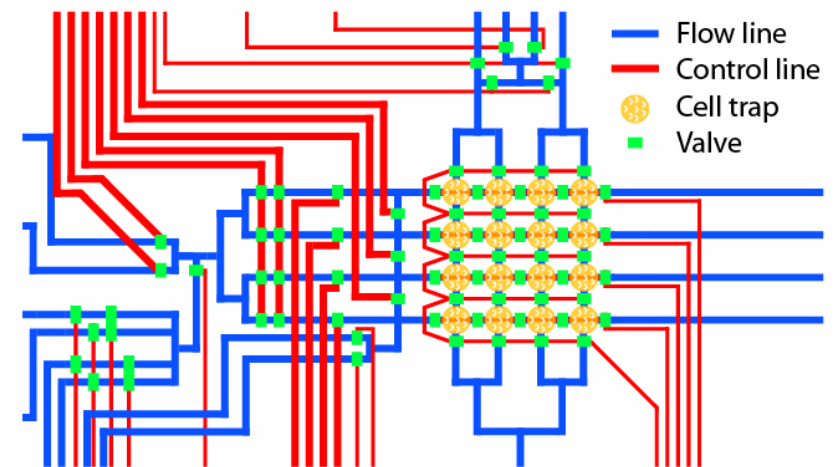
## 1. What are the best indicators for oocyte viability?

- With Mark Johnson's and Todd Thorsen's groups
- During in-vitro fertilization, monitor cell metabolites and select healthiest embryo for implantation



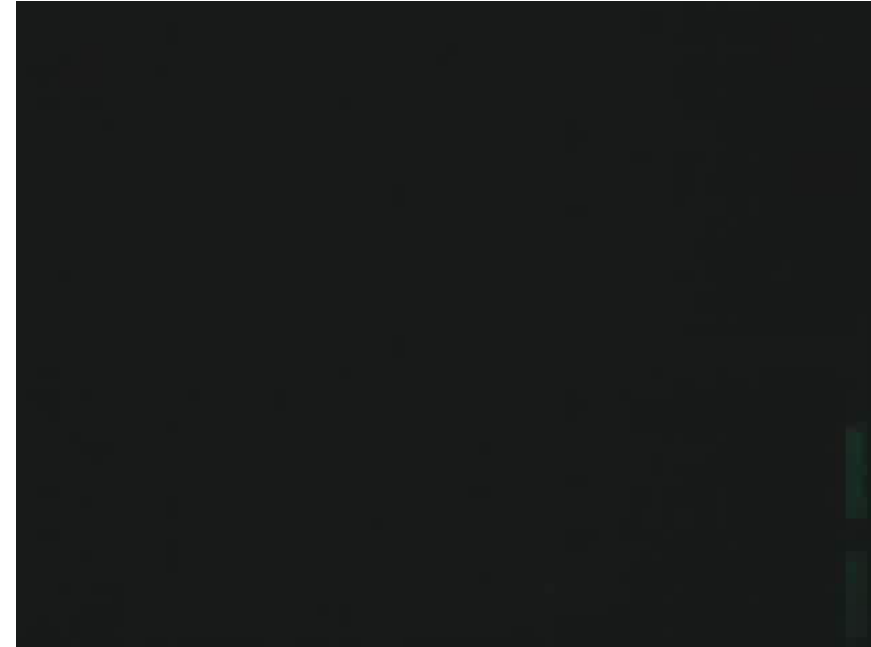
## 2. How do mammalian signal transduction pathways respond to complex inputs?

- With Jeremy Gunawardena's and Todd Thorsen's groups
- Isolate cells and stimulate with square wave, sine wave, etc.

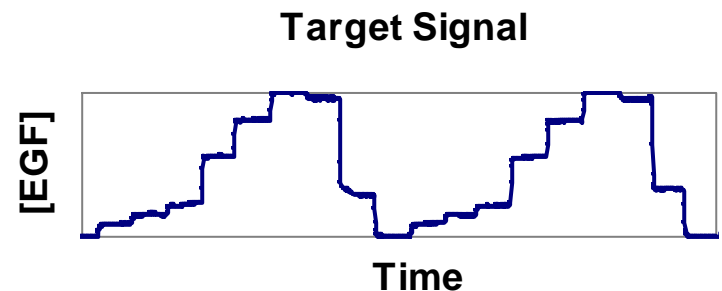


# Generating Complex Signals

```
CellTrap cells = new CellTrap();  
... // setup cell culture  
while (true) {  
    float target = targetSignal(getTime());  
    Fluid f = mix(EGF, target,  
                  WATER, 1-target);  
    cells.drainAndFill(f);  
    cells.useAfter(10*SEC);  
}
```



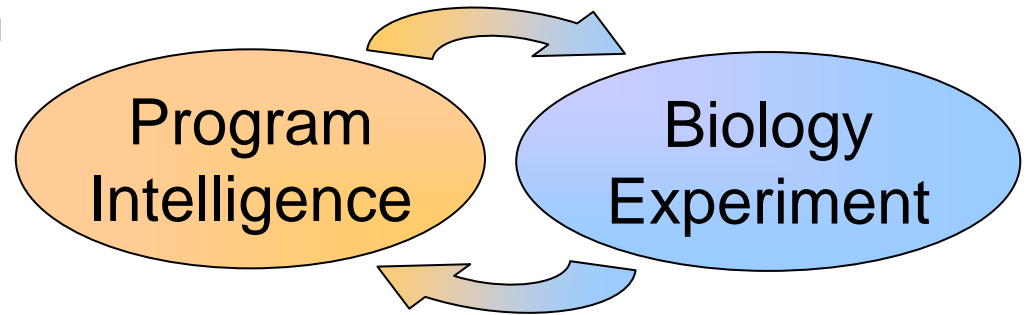
*Video courtesy David Craig*



# Additional Applications

- **Killer apps: react to feedback, redirect the experiment**

- Recursive-descent search
- Fixed-pH reaction
- Directed evolution
- Long, complex protocols



- **Application to biological computation**

- Many emerging technologies:  
DNA computing, cellular signaling, biomolecular automata, ...
- But not yet able to assemble, sustain, and adapt themselves
- Microfluidics provides a scaffold to explore underlying biology

# **Compiler Optimizations**



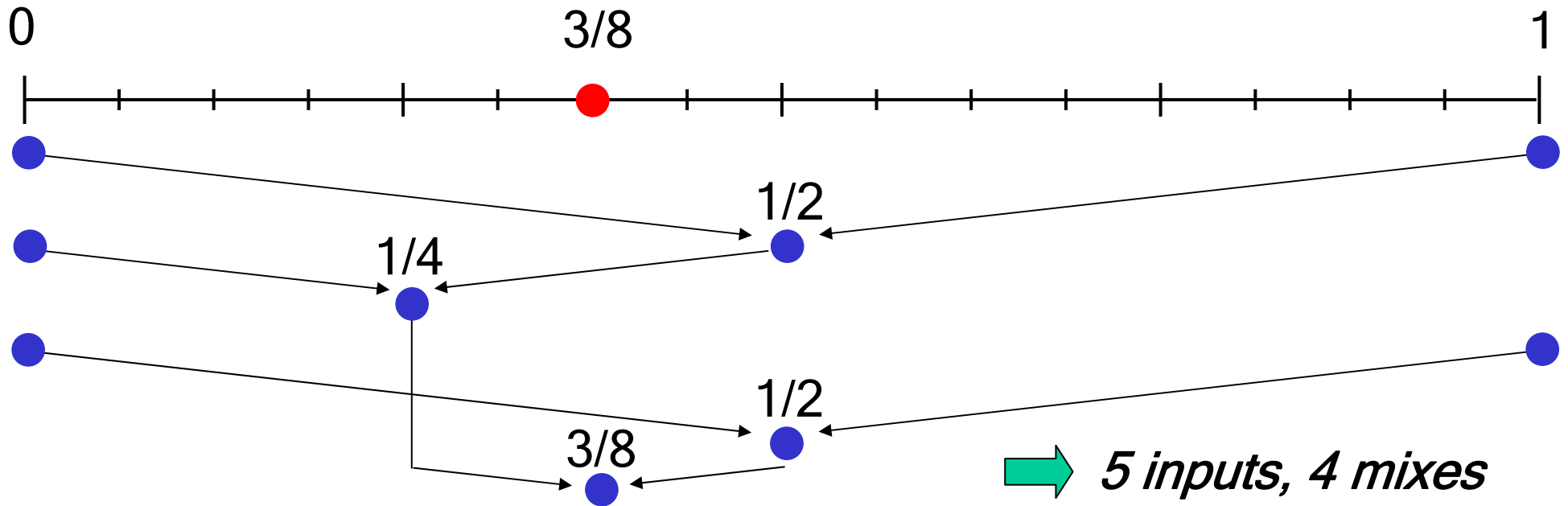
# Algorithms for Efficient Mixing

- **Mixing is fundamental operation of microfluidics**
  - Prepare samples for analysis
  - Dilute concentrated substances
  - Control reagent volumes

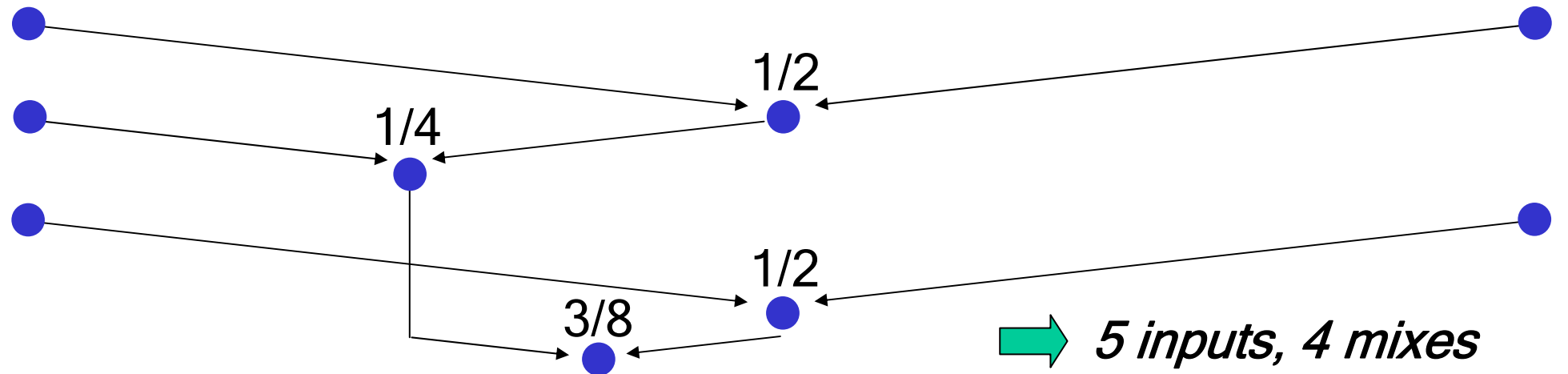
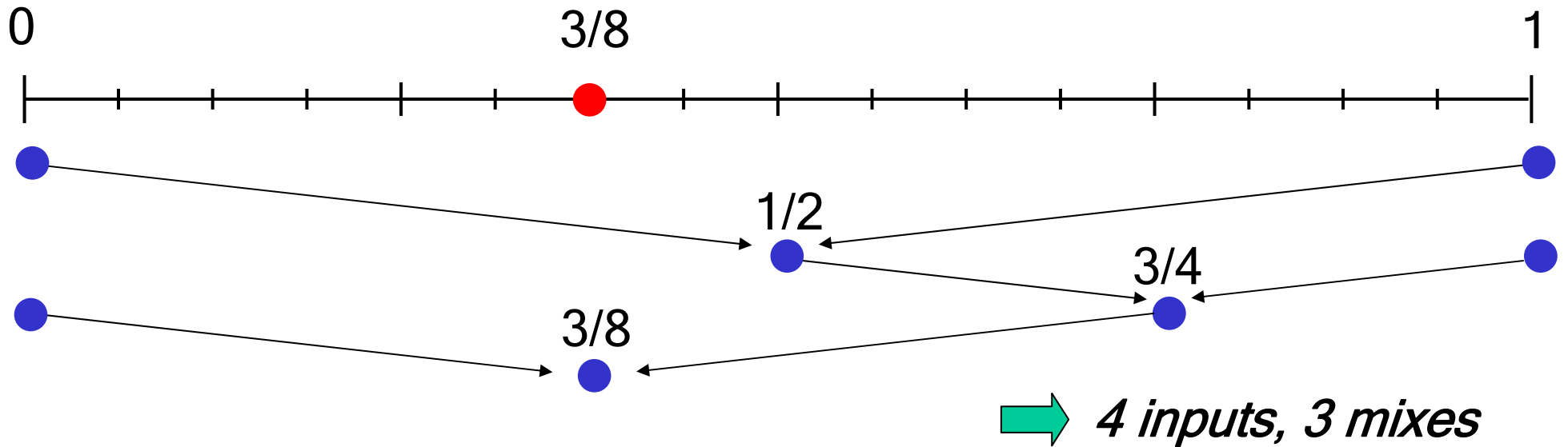
➡ Analogous to ALU operations on microprocessors
- **How to synthesize complex mixture using simple steps?**
  - Many systems support only 50/50 mixers
  - Should minimize number of mixes, reagent usage
  - Note: some mixtures only reachable within error tolerance  $\varepsilon$

➡ Interesting scheduling and optimization problem

# Why Not Binary Search?



# Why Not Binary Search?

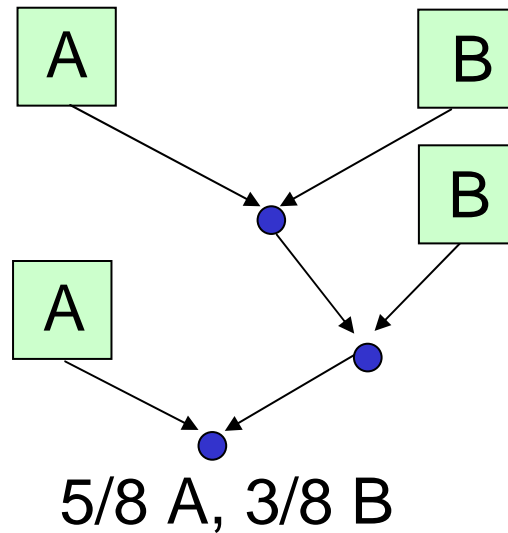


# Min-Mix Algorithm

- **Simple algorithm yields minimal number of mixes**
  - For any number of reagents, to any reachable concentration
  - Also minimizes reagent usage on certain chips

# Min-Mix Algorithm: Key Insights

1. The mixing process can be represented by a tree.



# Min-Mix Algorithm: Key Insights

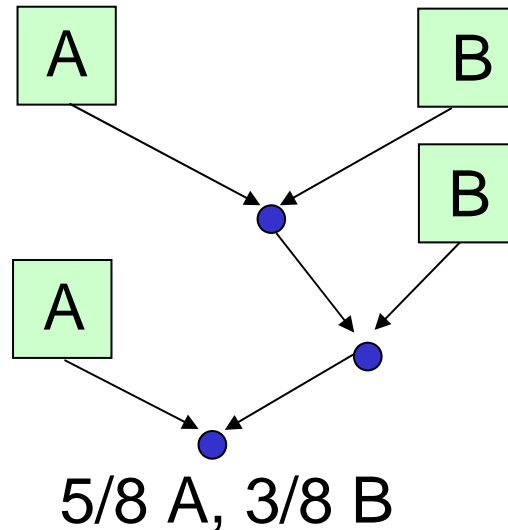
1. The mixing process can be represented by a tree.

<b>d</b>	<b><math>2^{-d}</math></b>
----------	----------------------------

3	1/8
---	-----

2	1/4
---	-----

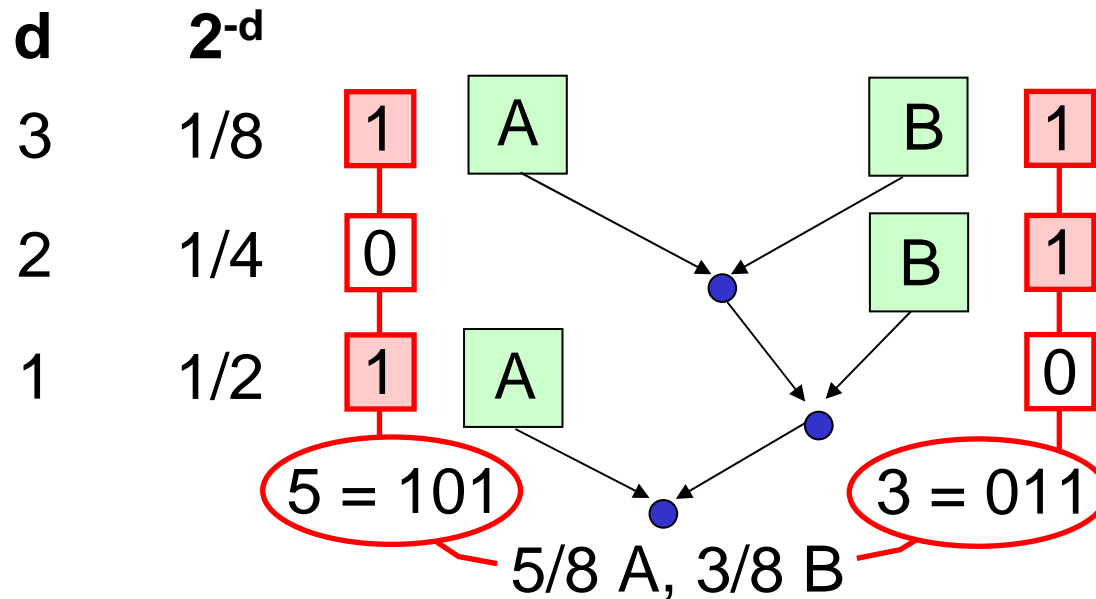
1	1/2
---	-----



2. The contribution of an input sample to the overall mixture is  $2^{-d}$ , where  $d$  is the depth of the sample in the tree

# Min-Mix Algorithm: Key Insights

1. The mixing process can be represented by a tree.



2. The contribution of an input sample to the overall mixture is  $2^{-d}$ , where  $d$  is the depth of the sample in the tree
3. In the optimal mixing tree, a reagent appears at depths corresponding to the binary representation of its overall concentration.

# Min-Mix Algorithm

- **Example: mix 5/16 A, 7/16 B, 4/16 C**

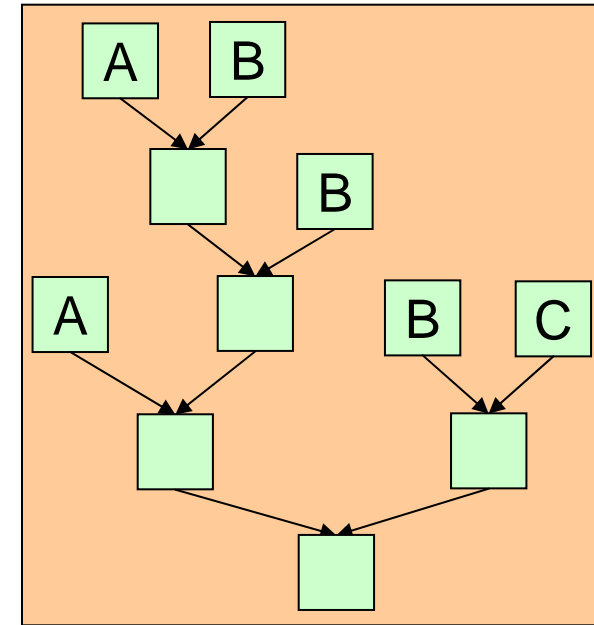
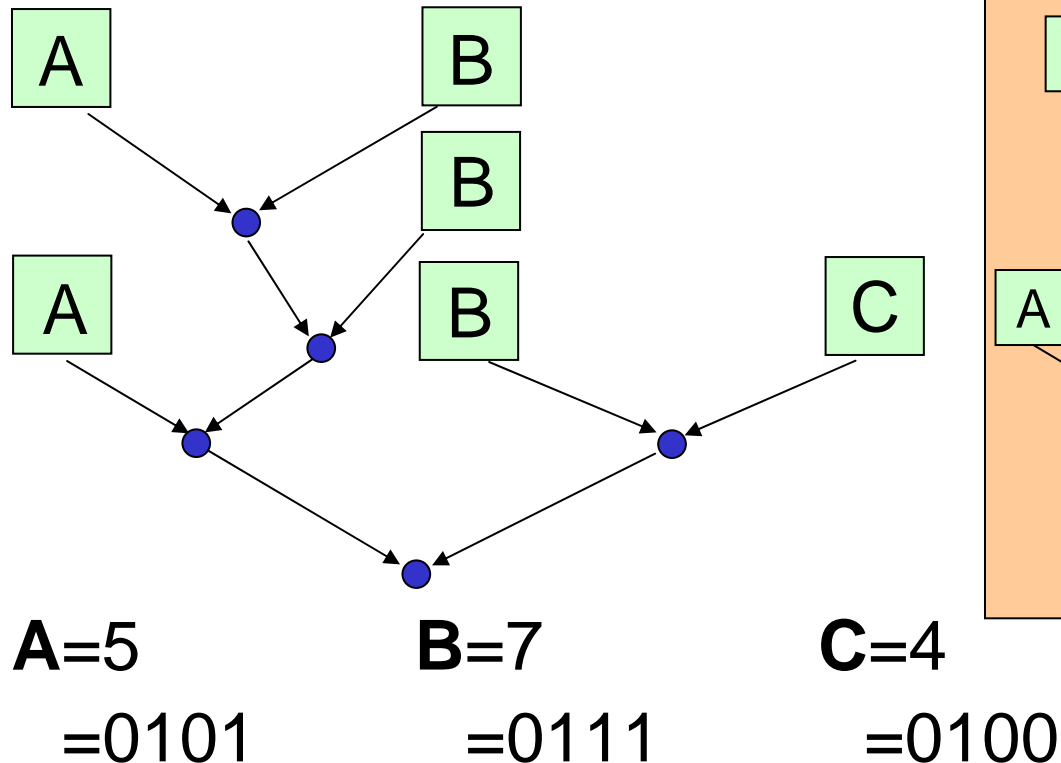
**d**      $2^{-d}$

4     1/16

3     1/8

2     1/4

1     1/2



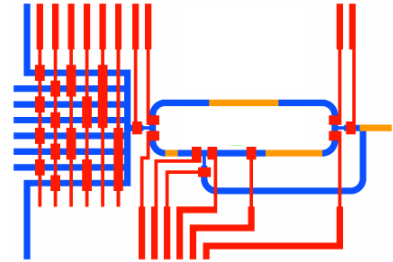
- **In paper: pseudocode, proof of correctness / optimality**



**Work In Progress**

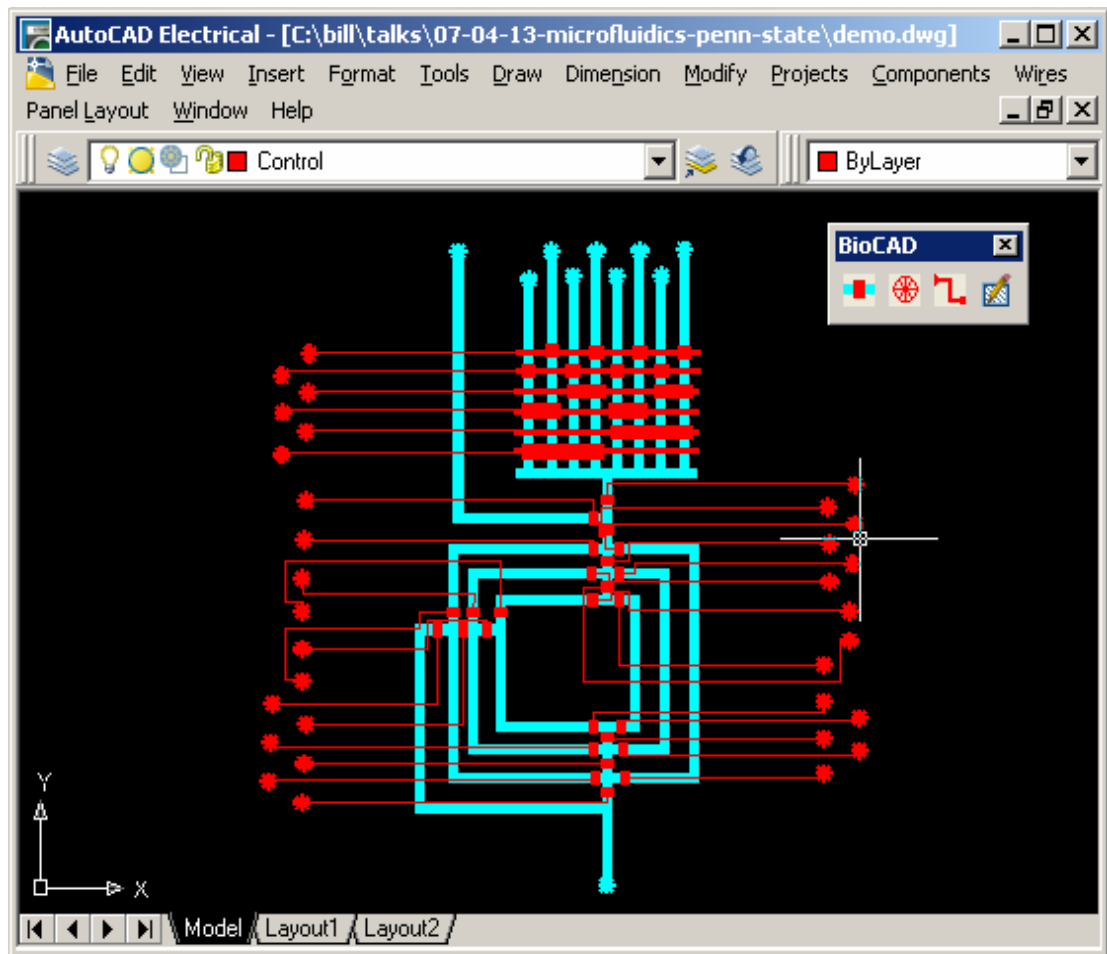
# CAD Tools for Microfluidic Chips

- **Microfluidic design tools are in their infancy**
  - Most groups use Adobe Illustrator or AutoCAD
  - Limited automation; every line drawn by hand
- **Due to fast fabrication, redesign is very frequent**
  - Student can do multiple design cycles per week



# First Step: Automatic Routing

- **First target: automate the routing of control channels**
  - Connecting valves to pneumatic ports is very tedious
  - Simple constraints govern the channel placement
- **AutoCAD plugin automates this task**
  - Developed With Nada Amin

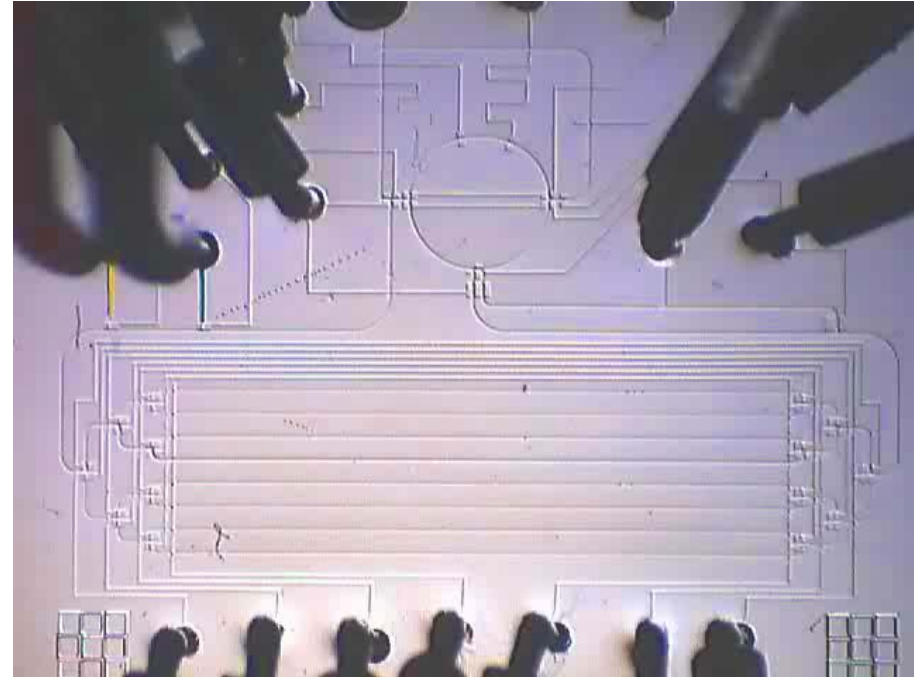


# Related Work

- **Aquacore – builds on our work, ISA + architecture** [Amin et al.]
- **Automatic generation / scheduling of biology protocols**
  - Robot scientist: generates/tests genetic hypotheses [King et al.]
  - EDNAC computer for automatically solving 3-SAT [Johnson]
  - Compile SAT to microfluidic chips [Landweber et al.] [van Noort]
  - Mapping sequence graphs to grid-based chips [Su/Chakrabarty]
- **Custom microfluidic chips for biological computation**
  - DNA computing [Grover & Mathies] [van Noort et al.] [McCaskill] [Livstone, Weiss, & Landweber] [Gehani & Reif] [Farfel & Stefanovic]
  - Self-assembly [Somei, Kaneda, Fujii, & Murata] [Whitesides et al.]
- **General-purpose microfluidic chips**
  - Using electrowetting, with flexible mixing [Fair et al.]
  - Using dielectrophoresis, with retargettable GUI [Gascoyne et al.]
  - Using Braille displays as programmable actuators [Gu et al.]

# Conclusions

- **Abstraction layers for programmable microfluidics**
  - General-purpose chips
  - Fluidic ISA
  - BioStream language
  - Mixing algorithms
- **Vision for microfluidics: everyone uses standard chip**
- **Vision for software: a defacto language for experimental science**
  - Download a colleague's code, run it on your chip
  - Compose modules and libraries to enable complex experiments that are impossible to perform today



**<http://cag.csail.mit.edu/biostream>**

# **Extra Slides**

# How Can Computer Scientists Contribute?

- **Applying the ideas from our field to a new domain**
  - Sometimes requires deep adaptations (e.g., digital gain)
- **Our contributions:**
  - First soft-lithography digital architecture with sample alignment
  - First demonstration of portability: same code, multiple chips
  - New high-level programming abstractions for microfluidics
  - First  $O(\lg n)$  mixing algorithm for lossy unit volumes (vs  $O(n)$ )
- **Open problems:**
  - Adapt unique (linear) types to microfluidics
  - Sound scheduling under timing constraints
  - Dynamic optimization of *slow* co-processors (lazy vectorization?)
  - Mixing algorithms for different ISA's (e.g., lossless mixing)
  - Generate a CAD layout from a problem description