

# Performance of a Robust WDM Network with Token Based Reservations and a Limited Number of Lasers at a Station<sup>1</sup>

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## Abstract

*The performance of a symmetric Robust WDM network that uses token-passing on the signaling channel and has a limited number of lasers per station is modeled and analyzed for circuit-switched connections. Robust WDM networks use a reservation interval during which all stations cease their WDM transmissions so that the station holding the token may establish a connection with its intended destination. The network performance is analyzed for different network parameters. Simulation results are used to evaluate the accuracy of the model.*

## 1. Introduction

In recent years, wavelength division multiplexing (WDM) has emerged as the most promising solution to satisfy the increasing need for larger bandwidth [9]. WDM exploits the enormous capacity of the single mode fiber by dividing the available wavelength into smaller, more manageable, multiple wavelengths to carry out more than one transmissions at a time; thereby offering a potential aggregate throughput in Terabits per second range. It has intrigued a large number of researchers in the industry and academia resulting in prototypes such as Rainbow-I & II [10], STARNET [4], and LIGHTNING [5].

WDM architectures are based on transmitters and receivers that can be precisely tuned to predetermined, fixed wavelengths. Wavelength of a laser shifts with temperature and the output power of the laser can also change even though a constant input current is applied. Wavelength and power stabilization of laser transmitters is a very critical and expensive task. For this reason the commercial exploitation of WDM systems has not made great progress. This is especially true for short-haul (SH) local area network (LAN) environment where the cost of

the fiber and its installation would be considerably less in comparison to the cost of suitable transmitter sources.

Robust WDM network, a network being implemented at Colorado State University and University of Colorado, is an approach that allows relaxed manufacturing and operating wavelength tolerances [1]. Robust WDM networks can be implemented based on several different medium access protocols [7]. This paper evaluates a reservation type, token based medium access protocol for a Robust WDM network with circuit-switched connections.

In [2], we modeled and analyzed a symmetric Robust WDM circuit-switched network where each station can access all the  $c$  channels of the network. In this paper, we investigate a more realistic case where each station has only a limited number of lasers ( $c_s$ ) and hence can access only  $c_s$  channels that are randomly spread over the total network channels ( $c$ ).

Section 2 provides a description of Robust WDM network and the token based MAC protocol, Section 3 details the performance model, Section 4 discusses the test results and its comparison with the simulation results, and Section 5 concludes the paper.

## 2. Robust WDM Network

The network architecture, as it is illustrated in Figure 1, is based on a passive star, where each node has an array of lasers, one of which is dynamically selected at the transmission time [7,11,12,13].

The time is divided into slots, each of which consists of two subslots, namely the transmission interval ( $T_t$ ) and the reservation interval ( $T_r$ ). The WDM transmissions and the reservation intervals are interlaced, as shown in Figure 2. High-speed WDM transmissions are allowed only during the transmission intervals. Several stations, up to the total number of channels ( $c$ ), may transmit simultaneously

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during a transmission interval, as long as they are on different channels (wavelengths). During a reservation interval, all stations stop their high-speed WDM transmissions and one station is allowed to establish a connection with its intended destination. Although the use of the reservation interval, during which no WDM transmissions take place, decreases the performance of the network, this protocol and the implementation have many advantages over the traditional WDM techniques in the areas of robustness and cost effectiveness. The reasoning for using reservation intervals is described in [7,11,12].

A station is considered 'full' if it has an incomplete, pending or being served, connection request; otherwise, it is 'empty'. In addition, a station is 'active' if its WDM transmission starts or continues in the current slot; otherwise, it is 'idle'. The reservation interval may also be used to acknowledge the ability of the receiver to lock on to the signal and to setup a reverse link if required.

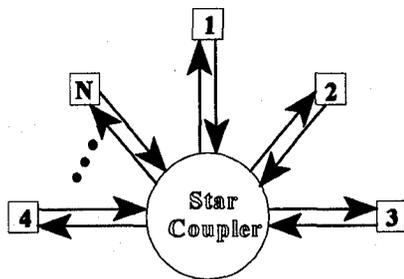


Figure 1: A generic WDM Star network.

A token-passing scheme is used to assign one of the waiting stations to the next reservation interval. The token travels on a separate low-speed control channel, visiting the stations in sequence. A station holds the token only if it is idle and has a request for a connection. Once an available channel is found, the station starts its WDM transmission at the beginning of the next transmission interval, and passes the token to the next station. The time to pass the token, the changeover time, is  $\epsilon$ . If the new station is active, or idle and empty, it does not hold the token but sends it to the next station. Each reservation interval is followed by a transmission interval in which all the WDM links resume their operation.

Thus, the sequence of events that take place at a station is as follows. First, the station receives a request for a connection. The node waits until it is visited by the token. The station holds the token for a random time  $h$ , with mean  $H=E[h]$ , until it gets an available channel (free wavelength) to setup a circuit-switched connection. Only then, does it transmit the token, on the signaling channel, to the downstream station as well as start the WDM transmission corresponding to the request. When the connection ends, the station awaits the next arrival, and the pattern repeats.

By an available channel we mean an unused wavelength, e.g.,  $\lambda_i$  in Figure 2, that is accessible to the station, rather than a predefined wavelength [1]. Thus, the spacing between adjacent channels may change and need not be constant. In this protocol, a node can be forced to re-select another laser after transmitting for a certain maximum time; hence, the protocol is able to tolerate slow variation of the laser wavelength. However, in our model, the variation of laser wavelengths with time is not considered

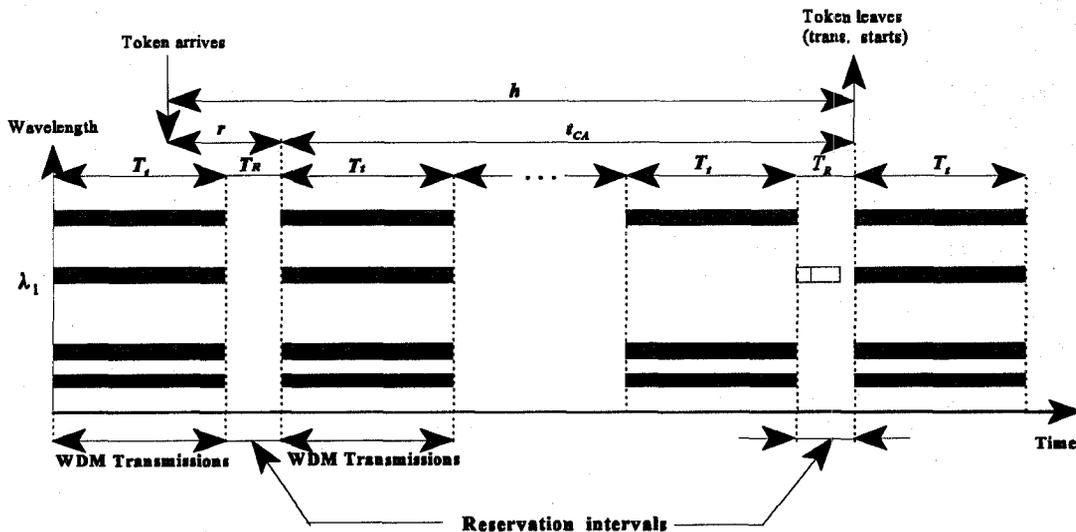


Figure 2: Interlaced WDM transmissions and reservation intervals.

### 3. The performance model

#### Assumptions

- \* The network consists of ( $N$ ) stations and ( $c$ ) transmission channels.
- \* Each station has  $c_s$  lasers ( $c_s \leq c$ ), the wavelengths of which are non-overlapping and randomly distributed among the  $c$ -channels.
- \* A symmetric network is considered where arrival rate, service time distribution as well as the node characteristics are the same for all the stations.
- \* Requests for connections arrive at stations according to independent Poisson processes (mean  $\lambda_s$  arrivals per sec per station).
- \* A station can handle only one connection request at a time. New requests arriving before the station completes a prior request are lost.
- \* The service times of connections are independent, independent of the arrival process and is geometrically distributed, with parameter  $p$ ; i.e., the transmission continues in the next slot with probability  $p$ .
- \* The token changeover time ( $e$ ), from a station to another, is constant.
- \* Only simplex WDM transmissions are considered.

#### Analysis

Consider the token as a server that serves a station for a time  $h$  as shown in Figure 2.  $h$  is the time from the arrival of the token at a station till the connection is established. Since the token serves a station for only one request at a time, the serve-at-most-one discipline can be considered. In [6], the cyclic queueing model was analyzed by defining the server vacation model, where the server periodically leaves the queue, taking a vacation. This is similar to the model of  $N$  queues served in a cyclic order when the vacation is interpreted as the time interval from when the server leaves a queue until it returns to that queue after visiting the other ( $N-1$ ) queues. In [8], it was viewed that a vacation occurs every time the server executes a changeover between queues.

Assuming that the token changeover times ( $e$ ) is constant;  $e^{(2)} = e^2$ , the waiting time ( $W_Q$ ) can be stated using the results given in [6,8] as follows:

$$W_Q = \left[ \frac{1-p}{1-p-\lambda e} \right] \left[ \frac{(N-1)e}{2(1-p)} + \frac{\lambda H^{(2)}}{2(1-p)} + \frac{e}{2} + H \right] \quad (1)$$

where,

$W_Q$  ..... mean of the total waiting time, measured from the instant of a connection request arrival to the time when the connection is established.

- $N$  ..... number of stations in the network.
- $H, H^{(2)}$  first and second moments of the service time (visit period of the token).
- $e$  ..... mean token changeover time.
- $\lambda$  ..... total effective arrival rate to the network [arrivals / sec].
- $\rho$  ..... total token (server) utilization.
- $\lambda_s$  ..... rate of connection request arrivals to a node.
- Let  $P_{ES} = \text{Prob} \{ \text{the station under consideration is empty} \}$ , then:

$$\lambda = N \lambda_s P_{ES} \quad (2)$$

$$\rho = \lambda H \quad (3)$$

#### $H$ and $H^{(2)}$

From Figure 2, assuming that  $r$  and  $t_{CA}$  are independent,  $H$  and  $H^{(2)}$  can be obtained as follows:

$$H = E[r + t_{CA}] = R + T_{CA} \quad (4)$$

$$H^{(2)} = E[(r + t_{CA})^2] = R^{(2)} + 2RT_{CA} + (T_{CA})^{(2)} \quad (5)$$

$$T_{CA} = \sum_{i=0}^{\infty} i.S.P_{CA}(i) \quad (6)$$

$$(T_{CA})^{(2)} = \sum_{i=0}^{\infty} (i.S)^2 P_{CA}(i) \quad (7)$$

$R, R^{(2)}$  ..... first and second moments of the residual time ( $r$ ), where  $r$  is measured from the instant of the token arrival to a station till the beginning of the next transmission interval. Expressions for  $R$  and  $R^{(2)}$  can be found in [3].

$T_{CA}, (T_{CA})^{(2)}$  ... first and second moments of the time  $t_{CA}$ , measured from the beginning of the transmission interval next to the token arrival to the moment when the token leaves the station.

$S = (T_t + T_r)$  ..... slot time.

Assuming that the time for which a station may use a channel, i.e., the duration of a connection, is geometrically distributed with a mean value  $L$  slots/connection,

$q = \text{Prob} \{ \text{at the beginning of a slot, the station under consideration gives up the channel, i.e., the station becomes 'idle'} \} = 1/L$

$p = \text{Prob} \{ \text{at the beginning of a slot, the station under consideration keeps the channel for another slot} \} = 1 - q$

Let ( $t=0$ ) correspond to the beginning instant of the transmission interval next to the token arrival, where ( $t$ ) is a time expressed in slots; and consider only the simplex WDM transmissions.

Let  $C_t$  be the set of  $c_s$  channels accessible by the station that is holding the token and  $C_o$  be the set of  $c_s$  channels accessible by the station under consideration.

$N > c_s$ :

For  $i > 0$ :

$P_{CA}(i) = \text{Prob} \{ \text{there is a channel available, exactly at } t=i \text{ and not before that} \}$

$$P_{CA}(i) = P(E \cap F) = P(E/F) \cdot P(F)$$

$P(E/F) = \text{Prob} \{ \text{there is a channel available, exactly at } t=i \mid \text{no channel is available before that} \}$   
 $= \text{Prob} \{ \text{exactly at } t=i, \text{ a channel or more of the } c_s \text{ busy channels become(s) free} \mid \text{all the } c_s \text{ channels were busy for } i\text{-successive slots from } t=0 \}$

$$= 1 - p^{c_s}$$

This follows from the geometric distribution assumption for connection duration.

$P(F) = \text{Prob} \{ \text{no channel is available before } t=i \}$

$c_s$  busy channels at  $t=0$ , may include a new one that became busy right at that moment. This condition needs to be excluded, i.e., we are interested only in the case where all the  $c_s$  channels are busy at  $t=-1$  and have continued for another slot. Hence,

$P(F) = \text{Prob} \{ \text{all the } c_s \text{ channels in } C_0 \text{ are busy at } t=-1 \text{ and all of them continue for } (i+1) \text{ successive slots} \}$   
 $= \text{Prob} \{ \text{all the } c_s \text{ busy channels keep busy for } (i+1) \text{ successive slots} \mid \text{all of them were at } t=-1 \}$   
 $\cdot \text{Prob} \{ \text{all the } c_s \text{ channels are busy at } t=-1 \}$

$$P(F) = p^{c_s(i+1)} P_{CSB}$$

$P_{CSB} = \text{Prob} \{ \text{all the } c_s \text{ channels, accessible by the station, are busy at the beginning of a transmission interval} \}$

Hence, for  $N > c_s$ , and  $i > 0$ :

$$P_{CA}(i) = (1 - p^{c_s}) p^{c_s(i+1)} P_{CSB} \quad (8)$$

Substituting from equation (8) into equations (6) and (7), we get  $T_{CA}$  and  $(T_{CA})^{(2)}$ , respectively, as follows:

$$T_{CA} = \frac{(p^{c_s})^2}{1 - p^{c_s}} S P_{CSB} \quad (9)$$

$$(T_{CA})^{(2)} = \frac{(p^{c_s})^2 (1 + p^{c_s})}{(1 - p^{c_s})^2} S^2 P_{CSB} \quad (10)$$

For  $N \leq c_s$ :

$$P_{CA}(i) = 1 \quad ; \text{ for } i=0 \\ = 0 \quad ; \text{ otherwise}$$

From equations (6) and (7), for  $N \leq c_s$ :

$$T_{CA} = (T_{CA})^{(2)} = 0 \quad (11)$$

### Evaluation of $P_{CSB}$

To find  $P_{CSB}$ , the discrete-time Markov chain, shown in Figure 3, is used. Each state represents the number of busy channels ( $n$ ) in  $C_0$  at the beginning of a transmission interval. The state  $n=c_s$ , represents the case where all the  $c_s$  channels of the station are busy due to other active stations,

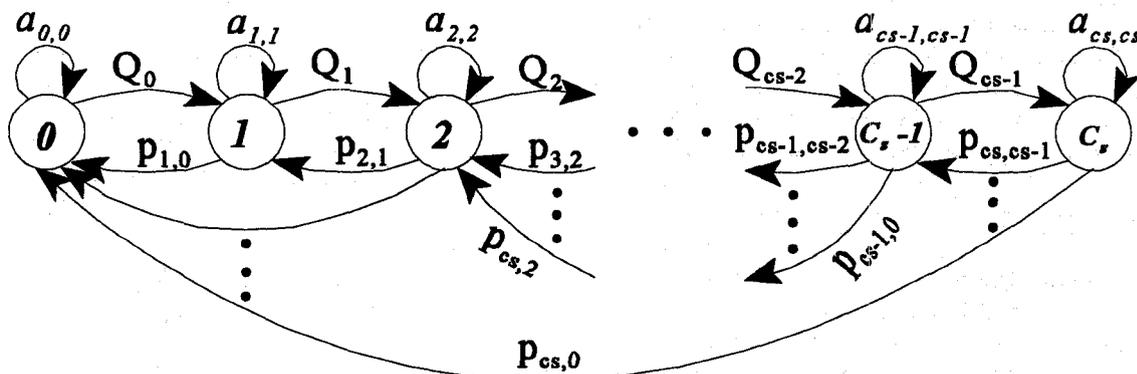


Figure 3: Markov chain for the number of  $j$ -busy channels.

i.e., no channel is available to the station under consideration. In the token-passing scheme only the station that is holding the token can start its transmission when there is a channel available. Thus, the number of the active stations and accordingly the number of busy channels can increase by at most one. On the other hand an arbitrary number of active stations may quit at the same time and hence the number of the busy channels can decrease by any number.

The steady-state probabilities can be obtained by solving (12) and (13). Thus,  $P_{CSB}(p_{cs})$  which corresponds to being in state  $c_s$  in the Markov chain, can be obtained.

$$\pi = \pi P \quad (12)$$

$$\sum_{i=0}^{c_s} p_j = 1 \quad (13)$$

where,  $\pi = [p_0 \ p_1 \ p_2 \ \dots \ p_{cs}]$   
 $p_j = \text{Prob} \{j \text{ channels, in } C_o, \text{ are busy at the beginning of a transmission interval}\}$   
 $P = [p_{ij}]$  the matrix of the transition probabilities ( $i, j = 0, 1, 2, \dots, c_s$ ).  
 $P_{n,n+1} = Q_n \quad (n < c_s)$ ;  
 $Q_n = \text{Prob} \{(n+1) \text{ channels, in } C_o, \text{ are busy in current slot} \mid n \text{ channels in } C_o \text{ were busy in previous slot}\}$   
 $= \text{Prob} \{\text{all the } n\text{-busy channels from previous slot continue to be busy in current slot}\}$   
 $\cdot \text{Prob} \{\text{one of the stations from the other } (N-n) \text{ stations is holding the token, has access to one or more of the } (c_s-n) \text{ free channels and selects one of these channels}\}$

$$Q_n = p^n \cdot P_{HT}(n) \cdot P_{as}(n) \quad \text{for } n \geq 0 ;$$

where,  
 $P_{HT}(n_1) = \text{Prob} \{\text{a station is holding the token} \mid n_1 \text{ channels, in } C_o, \text{ were busy in previous slot}\}$   
 $P_{as}(n_2) = \text{Prob} \{\text{the station that is holding the token has access to one or more of the } (c_s-n_2) \text{ free channels of the station under consideration in current slot and selects one of them}\}$

$a_{n,n} = p_{n,n} = \text{Prob} \{n \text{ channels in } C_o \text{ are busy in current slot} \mid n \text{ channels in } C_o \text{ are busy in previous slot}\}$   
 $= \text{Prob} \{\text{the number of continuing busy channels in } C_o = n \mid \text{all of them were busy during previous slot}\}$   
 $\cdot \text{Prob} \{\text{there is no station among the other } (N-n) \text{ stations that is holding the token or (there is a station holding the token and it cannot access and select one of these channels)}\}$   
 $+ \text{Prob} \{\text{the number of continuing busy channels in } C_o = (n-1) \mid n \text{ channels in } C_o \text{ were busy}$

during the previous slot}  
 $\cdot \text{Prob} \{\text{there is a station among the other } (N-n) \text{ stations that is holding the token, has access to one or more of the other } (c_s-n+1) \text{ free channels and selects one of them}\}$

$$a_{n,n} = p^n \cdot [(1 - P_{HT}(n)) + (1 - P_{as}(n))] + [np^{n-1}q] \cdot [P_{HT}(n)P_{as}(n-1)] \quad \text{for } 0 \leq n \leq c_s ;$$

Similarly:

$P_{n,m} = \text{Prob} \{m \text{ channels in } C_o \text{ are busy in current slot} \mid n \text{ channels in } C_o \text{ were busy in previous slot}\}$

$$P_{n,m} = \left[ \binom{n}{m} p^m q^{n-m} \right] [(1 - P_{HT}(n)) + P_{HT}(n) (1 - P_{as}(m))] + \left[ \binom{n}{m-1} p^{m-1} q^{n-m+1} \right] \cdot [P_{HT}(n)P_{as}(m-1)] \quad \text{for } m > 0 ;$$

$$P_{n,0} = q^n [(1 - P_{HT}(n)) + P_{HT}(n)(1 - P_{as}(0))]$$

**Evaluation of  $P_{as}(n_2)$  and  $P_{HT}(n_1)$**

$$P_{as}(n_2) = \sum_j \pi_1 P_{jBz} \quad (14)$$

$P_{jBz} = \text{Prob} \{\text{the station has } j \text{ busy channels in } C_i\}$   
 $\pi_1 = \text{Prob} \{\text{the station that is holding the token has access to one or more of the free channels in } C_o \text{ and selects one of them} \mid \text{it has } j\text{-busy channels}\}$

$$\pi_1 = \sum_{k=y_1}^{y_2} \pi_2 \cdot \pi_3$$

$\pi_2 = \text{Prob} \{\text{the station that is holding the token selects one of the } k \text{ free channels common with } C_o \mid \text{it has access to these } k \text{ channels and it has } j \text{ busy channels}\}$

$$\pi_2 = \frac{k}{(c_s - j)}$$

$\pi_3 = \text{Prob} \{\text{the station that is holding the token has access to } k \text{ channels, from the } (c_s-n) \text{ free channels in } C_o \mid \text{it has } j\text{-busy channels}\}$

$$\pi_3 = \binom{c-n}{k} \binom{(c-j)-(c-n)}{(c-j)-k} / \binom{c-j}{c-j}$$

Since the number of busy channels in  $C_i$  ( $j$ ) is limited between  $z_1$  and  $z_2$ ,  $P_{jBz}$  can be obtained from the Markov chain, Figure 3, as follows:

$$P_{jBz} = P_{jB} / \sum_{i=z_1}^{z_2} P_{iB}$$

$P_{jB} = \text{Prob} \{ \text{the station has } j \text{ busy channels} \mid z_1=0 \text{ and } z_2=c_s \}$

Figure 4 illustrates different scenarios of selecting  $C_o$  and  $C_i$  from the total  $c$  channels to evaluate the limits of  $j$  and  $k$  which are needed in the above equations. Assume that the station under consideration has  $n$  busy channels in  $C_o$ , the set of  $c_s$  channels accessible to it. The station that is holding the token has  $j$  busy channels in  $C_i$ ,  $C_i$  being the set of  $c_i$  channels accessible to it. Let  $k$  be the number of free channels in  $C_i \cap C_o$ , i.e., accessible by both of the stations. Figure 4(a) shows the general relation between  $n, j$ , and  $k$ . To find the lower limit of  $j$  ( $=z_1$ ), Figure 4(b) is used assuming that all the  $n$  busy channels are overlapping with the  $(c-c_s)$  channels that are not in  $C_i$ .  $n$  may be less or greater than the  $(c-c_s)$  channels that are not in  $C_i$ , thus:

$$z_1 = j_{min} = \max \{ 0, [n - (c - c_s)] \}$$

Similarly, Figure 4(c) is used to find the upper limit of  $j$  ( $=z_2$ ), assuming that the  $(c_s - n)$  free channels in  $C_o$  are the only free channels in  $c$ , thus the rest of  $\min(N, c)$  stations are busy.  $n$  cannot exceed  $c_s$ , thus,

$$z_2 = j_{max} = \min \{ c_s, \min [N, (c - (c_s - n))] \}$$

To find the lower limit of  $k$  ( $=y_1$ ), Figure 4(d) is used, assuming that there is an overlap between  $C_o$  and  $C_i$  and that all the  $n$  busy channels are in that overlap, thus:

$$y_1 = \max \{ 0, [(2c_s - c) - n] \}$$

Figure 4(e) is used to find the upper limit of  $k$  ( $=y_2$ ), assuming a complete coincidence between  $C_o$  and  $C_i$ , thus:

$$y_2 = \min \{ (c_s - n), (c_s - j) \}$$

$P_{HT}(n_1) = \text{Prob} \{ \text{a station or more, from the other } (N - n_1) \text{ stations, is (are) idle and full} \mid n_1 \text{ channels, out of } C_o, \text{ were busy in the previous slot} \}$

The  $(N - n_1)$  stations, in the above probability, can be divided into two groups,  $s_1$  and  $s_2$ , where the  $s_1$  stations are known to be idle while the  $s_2$  stations may be either idle or active. From Figure 4(c):

$$s_1 = [(N - n_1) - (c - c_s)] \quad ; \text{ if } (N - n_1) > (c - c_s) \\ = 0 \quad ; \text{ if } (N - n_1) \leq (c - c_s)$$

Thus:  $s_1 = \max \{ 0, [(N - n_1) - (c - c_s)] \}$

$$s_2 = (N - n_1) - s_1$$

$P_{HT}(n_1) = 1 - [ \text{Prob} \{ \text{none of the } s_1 \text{ idle stations is full} \} \cdot \text{Prob} \{ \text{none of the } s_2 \text{ (idle/active) stations is idle and full} \} ]$

$$P_{HT}(n_1) = 1 - (\pi_4)^{s_1} (\pi_5)^{s_2} \quad (15)$$

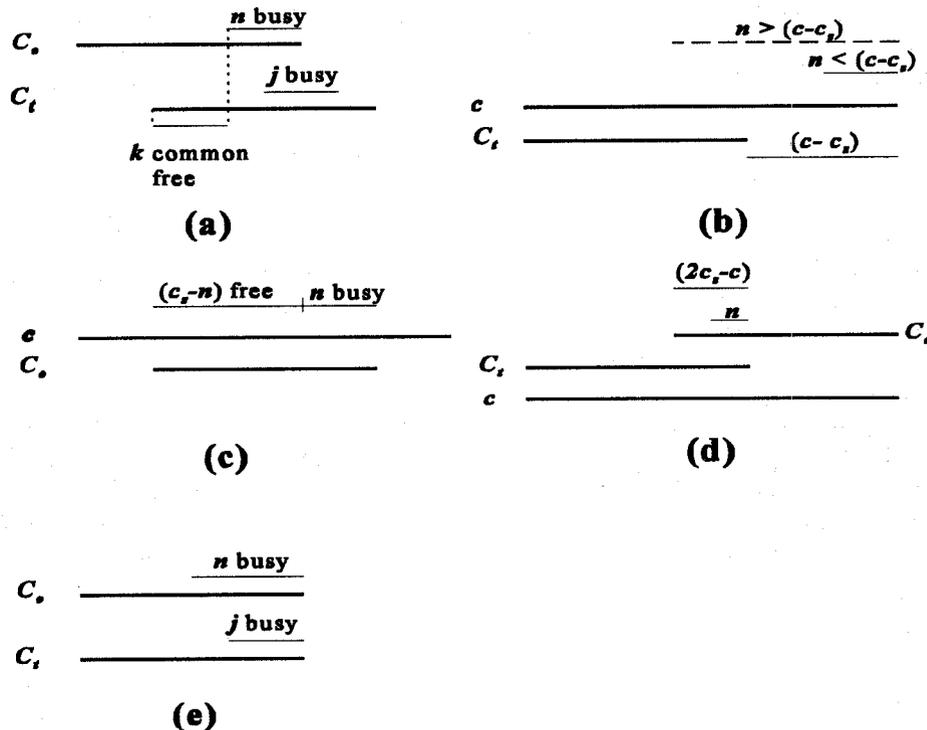


Figure 4: Relations between  $c$ ,  $C_o$ , and  $C_i$ .

$\pi_4 = \text{Prob} \{ \text{the station was empty at the beginning of the previous slot } (E) \mid \text{it was idle } (I) \}$   
 . Prob {no arrival to the station during the previous slot}

$$\pi_4 = P_{EI} e^{-\lambda_s S}$$

$$\pi_5 = 1 - P_{IF}$$

$P_{IF} = \text{Prob} \{ \text{a station is idle and full} \}$

Evaluation of  $P_{EI}$ ,  $P_{IF}$ ,  $\lambda$  and  $\rho$

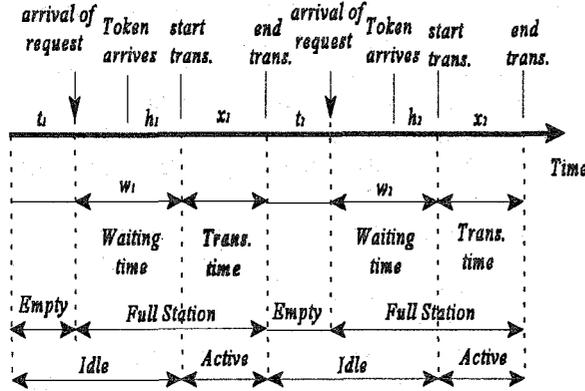


Figure 5: The different events that take place at a station.

$t_i \dots$  time between the end of transmission of request  $(i-1)$  and the instant of next connection request arrival  $i$ .  
 $E[t_i] = 1/\lambda_s$ , assuming Poisson arrival process.  
 $h_i \dots$  token holding time until the WDM transmission of the connection request  $i$  is started.  $E[h_i] = H$ .  
 $x_i \dots$  transmission time of request  $i$ ;  $E[x_i] = X$ .  
 $w_i \dots$  waiting time of connection request  $i$ ;  $E[w_i] = W_Q$ .  
 $\lambda_s \dots$  arrival rate to a station.

In Figure 5, consider the station is initially empty. Assuming Poisson arrivals, the mean time until the next connection request arrival is  $(1/\lambda_s)$ ; and only then does the station become full. After a random waiting time whose mean value is  $W_Q$  the corresponding transmission starts. The transmission time is an independent random variable and independent of the arrival process, with mean value  $X$ . Then, the next connection request arrival occurs after a time whose mean is  $(1/\lambda_s)$ , and so fourth.

Considering a cycle of events in Figure 5, we get  $P_{EI}$ ,  $P_{IF}$  and  $P_{ES}$  as follows:

$$P_{EI} = 1/(1+\lambda_s W_Q) \quad (16)$$

$$P_{IF} = \lambda_s W_Q / [1+\lambda_s(W_Q+X)] \quad (17)$$

$$P_{ES} = 1 / [1+\lambda_s(W_Q+X)] \quad (18)$$

Using equations (2), (3), and (18):

$$\lambda = N\lambda_s / [1+\lambda_s(W_Q+X)] \quad (19)$$

$$\rho = N\lambda_s H / [1+\lambda_s(W_Q+X)] \quad (20)$$

Substituting for  $\lambda$  and  $\rho$  in equation (1) and rearranging,  $W_Q$  is given by:

$$AW_Q^2 + BW_Q + D = 0 \quad (21)$$

where,

$$A = 2\lambda_s \quad (22)$$

$$B = 2 + [2X - 2(N+1)H - 3Ne]\lambda_s \quad (23)$$

$$D = -[Ne + 2H + [(X-H)Ne + NH^{(2)}] + 2H(X-NH)]\lambda_s \quad (24)$$

Use equations (12) and (13) to get  $P_{CSB}$  and (9), (10), and (11) to get  $T_{CA}$  and  $(T_{CA})^{(2)}$ . Use (4) and (5) to obtain  $H$  and  $H^{(2)}$ . Now, it is possible to obtain  $B$  and  $D$  using equations (23) and (24). Hence,  $W_Q$  can be obtained from equation (21).

#### 4. Results

In the following analysis, a network configuration, with fifty stations ( $N=50$ ) and ten transmission channels ( $c=10$ ) with each station having access to five channels ( $c_s=5$ ) is considered. Considering the device tuning time and propagation delays, the reservation intervals ( $T_R$ ) and the token changeover time ( $e$ ) are chosen to be  $1 \mu$  sec and  $0.1 \mu$  sec, respectively. The duration of the transmission intervals ( $T_T=100 \mu$  sec) and the mean connection duration ( $L=100$  slots) are kept constant. In addition, the mean arrival rate to a station ( $\lambda_s$ ) is selected to be either 10 or 100 arrivals/sec, to achieve reasonable values of the network load. These parameters are used in the analysis unless otherwise stated. The normalized network load ( $G$ ) is given by  $G=\lambda X/c$ , where  $X=L(T_T+T_R)$  is the mean transmission time.

Solving equation (21), by iteration, we get two values for the mean waiting time ( $W_Q$ ). In each experiment, we found only one viable value of  $W_Q$ . The remaining solution is either negative or results in nonfeasible values (negative or greater than one) for  $P_{ES}$  and  $\rho$ .

To illustrate the effect of the different parameters on the mean waiting time ( $W_Q$ ), we change one parameter at a time, keeping the others constant. Results obtained by using the model described in this paper are compared with those generated by simulation. The detailed description of the simulator can be found in [14]. In all the following figures the analytic results are plotted with continuous lines; while the simulation values are represented by \*'s.

Figure 6 illustrates the variation of the mean waiting time ( $W_Q$ ) against the rate of request arrivals at a station ( $\lambda_s$ ). At low arrival rates, increasing  $\lambda_s$ , decreases  $P_{ES}$  and increases  $W_Q$ . As  $\lambda_s$  is further increased, more stations become full thus blocking new arrivals and limiting  $W_Q$  to its maximum value.

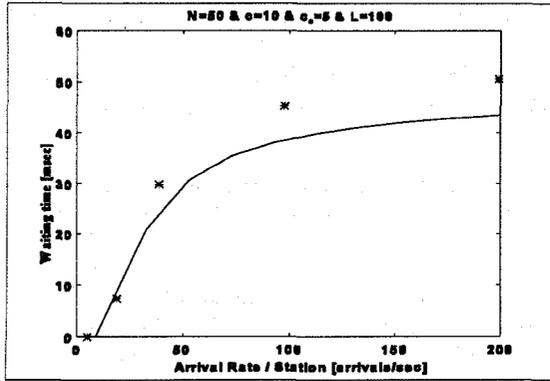


Figure 6: Mean waiting time ( $W_Q$ ) vs arrival rate per station ( $\lambda_s$ ).

The mean waiting time ( $W_Q$ ) with the number of stations in the network ( $N$ ) is illustrated in Figure 7. As long as  $N \leq c$ , the network behaves, on average, as always having a channel available for each station, and hence a request arrival does not wait for more than the residual time ( $r$ ). Increasing  $N$  beyond that, increases the number of full stations that can hold the token and hence increases the token rotation time and hence accordingly  $W_Q$ . Then, the token serves all the stations in sequence and hence  $W_Q$  increases almost linearly with  $N$ .

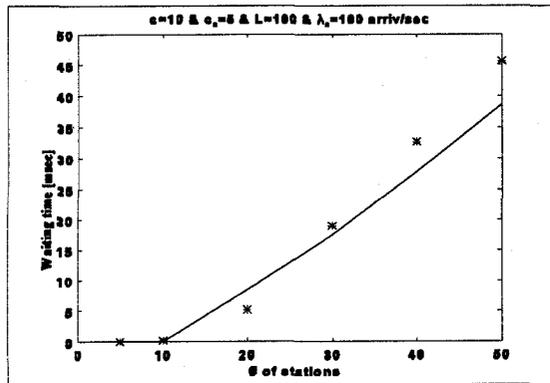


Figure 7: Mean waiting time ( $W_Q$ ) vs number of stations in the network ( $N$ ).

Figure 8 shows the effect of changing the transmission interval ( $T$ ) on the mean waiting time ( $W_Q$ ). Increasing  $T$ ,

increases the slot duration ( $S=T_i+T_R$ ) and hence increases the mean connection duration ( $X=LS$ ) which increases the channel holding time by a transmitting station. Thus, a station holds the token for longer time ( $h$ ) until it gets an available channel and as a result  $W_Q$  increases.

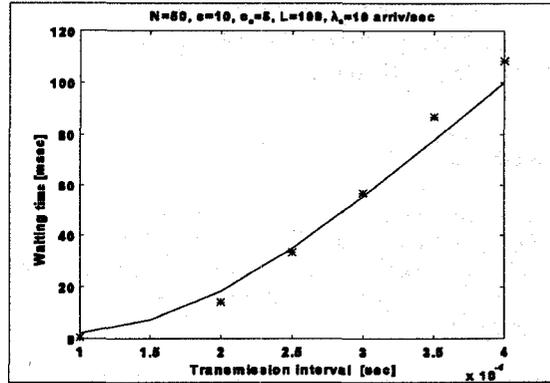


Figure 8: Mean waiting time ( $W_Q$ ) vs transmission interval ( $T$ ).

The relation between the mean waiting time ( $W_Q$ ) and the reservation interval ( $T_R$ ) is illustrated in Figure 9. As mentioned above, increasing  $T_R$ , increases  $S$  which increases  $X$ . Accordingly,  $h$  increases which increases  $W_Q$ . Since  $T_R$  is small, compared with  $T_i$ , its effect on  $W_Q$  is smaller; and within this small range of variation,  $W_Q$  changes almost linearly with  $T_R$ .

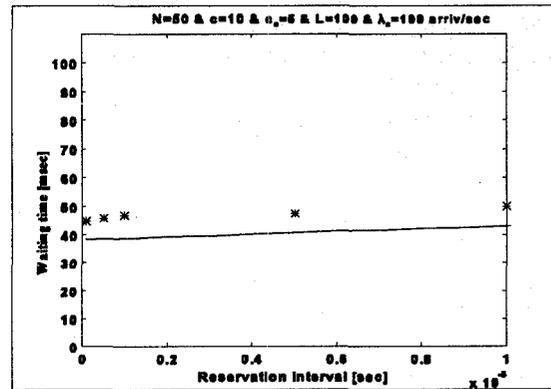


Figure 9: Mean waiting time ( $W_Q$ ) vs reservation interval ( $T_R$ ).

## 5. Conclusion

This paper considers a network with a given number of lasers per station and as a result presents a more realistic scenario compared to the prior model [2] that assumes each

station to have a laser corresponds to each possible channel wavelength.

The mean request waiting time ( $W_Q$ ) was evaluated for the different network parameters. Comparing the results with the simulation's ones indicates that the model can accurately predict the network performance. The model is to be extended to analyze a more realistic network, closely to the one being prototyped at Colorado State University and University of Colorado.

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